

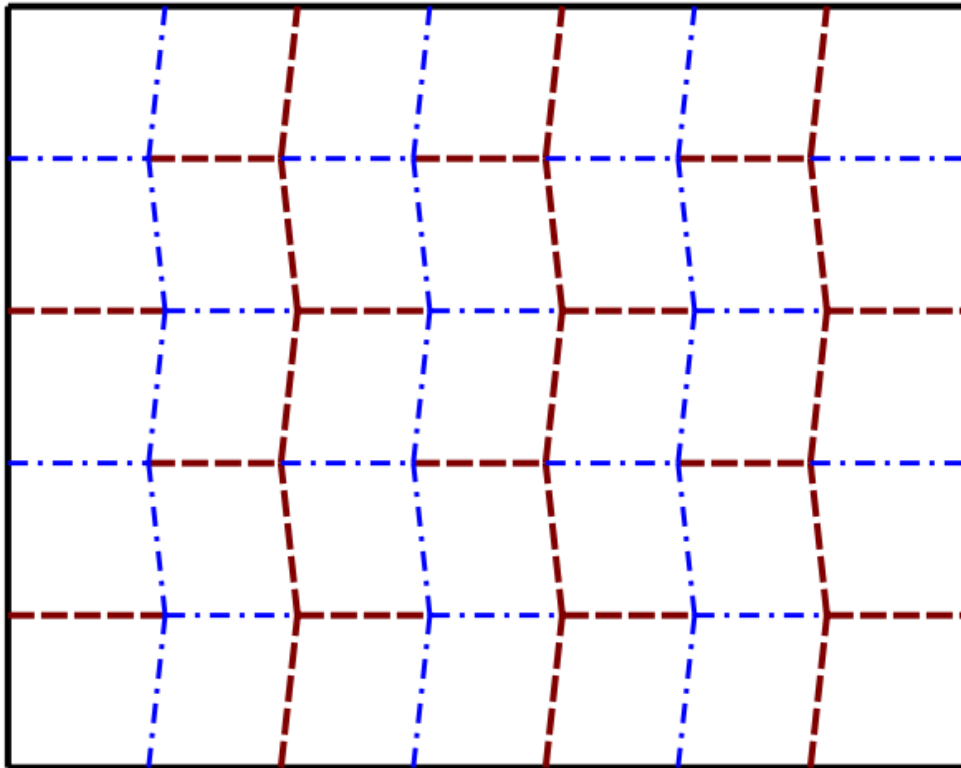
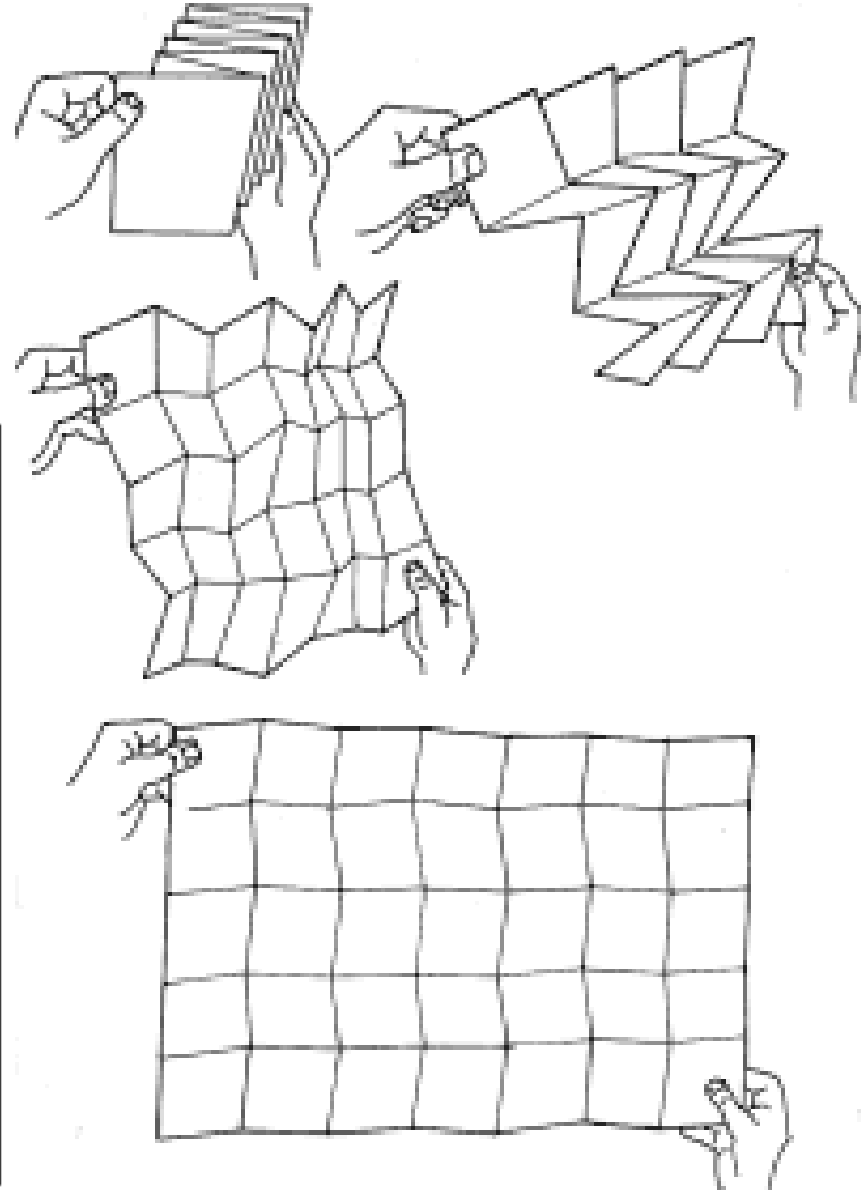
MIT Class 6.S080 (AUS)

# **Mechanical Invention through Computation**

Kinetic Origami

# Miura Ori

Basis of much  
Kinetic origami  
(continuous folding)

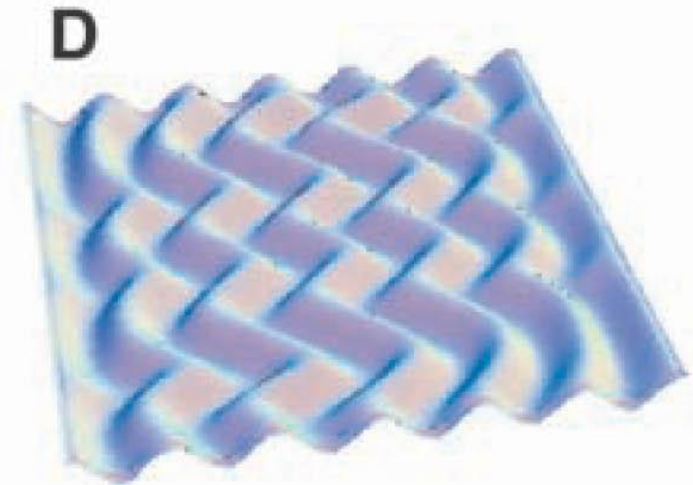
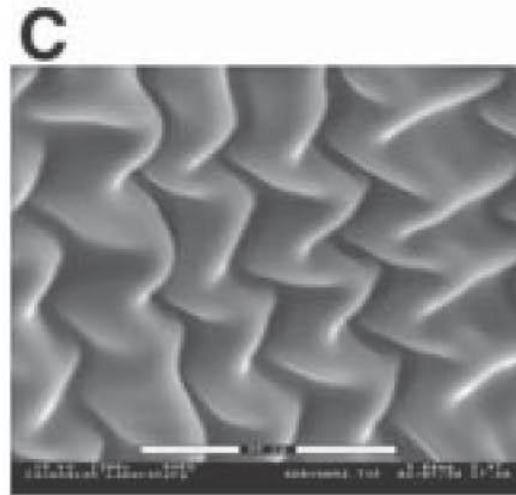
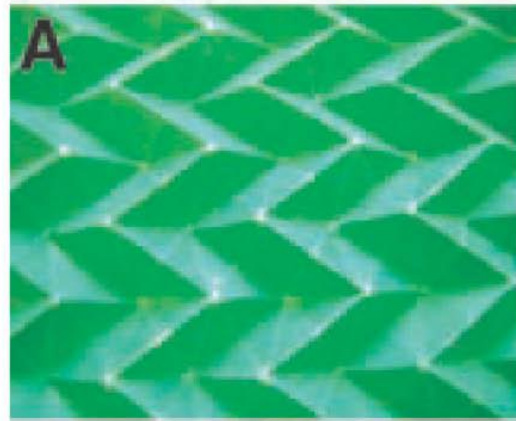


# Miura Ori



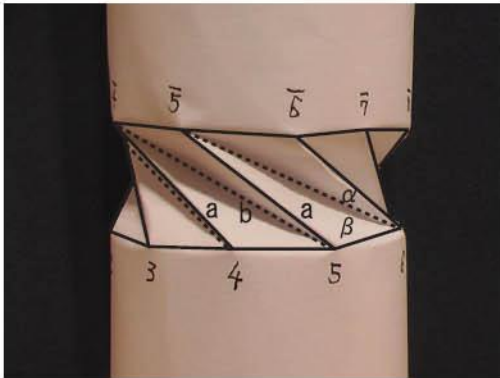
# Miura Ori in Nature (L. Mahadevan, Wyss Institute)

**Fig. 1.** (A) Plan view of a paper Miura-ori pattern (size, 5 cm), showing the periodic mountain-valley folds. The sharp re-entrant creases that come together at kinks allow the whole structure to fold or unfold simultaneously. (B) Hornbeam leaves (length, 5 cm) in the process of blooming show a natural occurrence of Miura-ori. A single row of kinks along the midrib allows a folded leaf to be deployed once the bud opens (2), as seen in the different stages of leaf opening (clockwise from the top). (C) Zigzag Miura-ori patterns in a thin film atop a thick elastic substrate that is compressed biaxially manifest here in a drying slab of gelatin with a thin skin that forms naturally (6), showing the physically driven self-organization of Miura-ori. Scale bar, 35  $\mu\text{m}$ . (D) Simulations of Eq. 1 yield Miura-ori patterns that arise as a modulational instability of the primary (straight) wrinkles (supporting online text).

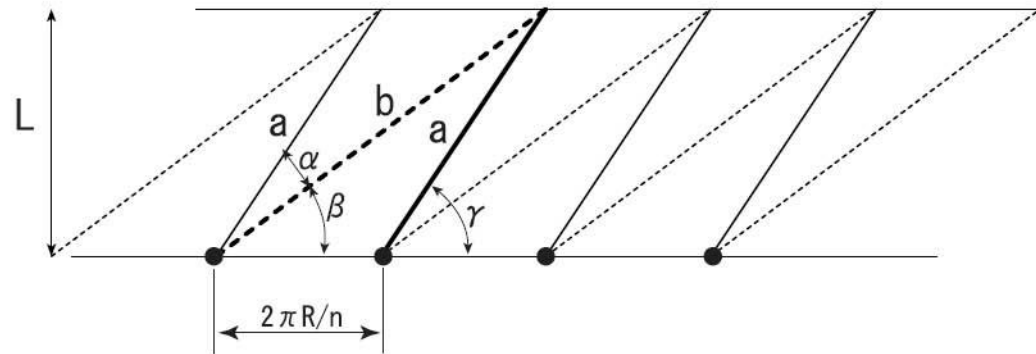




# Buckling of a cylinder



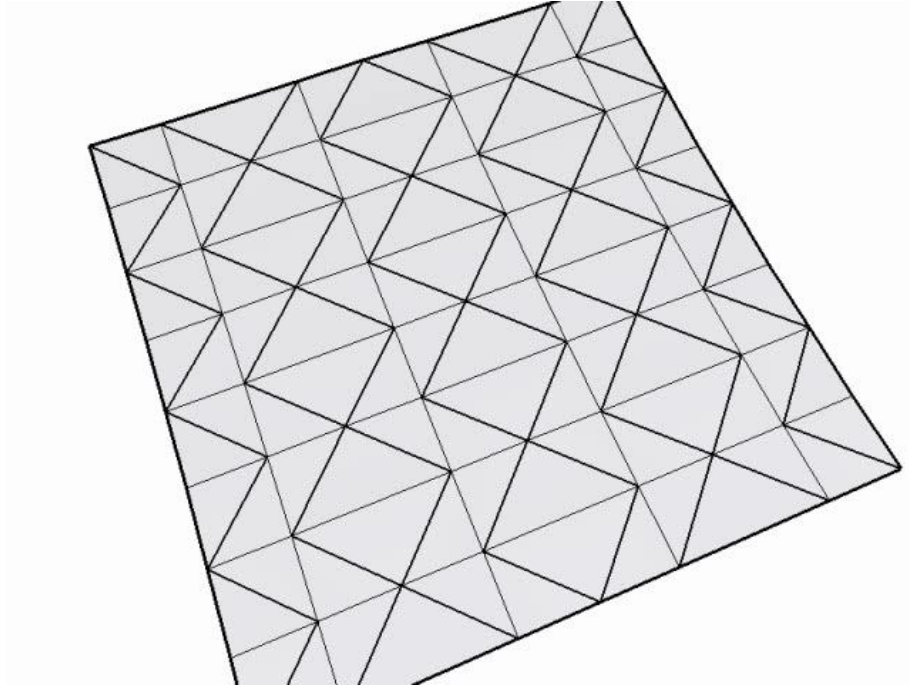
(a) Fold lines and angles of the folding mechanism



(b) Truss Geometry

**Figure 1.** The foldable cylinder based on twist buckling of a paper roll. Large deflections involve work being done primarily against bending, with very little stretching energy included; such behaviour is of interest for example, in the field of deployable structures.

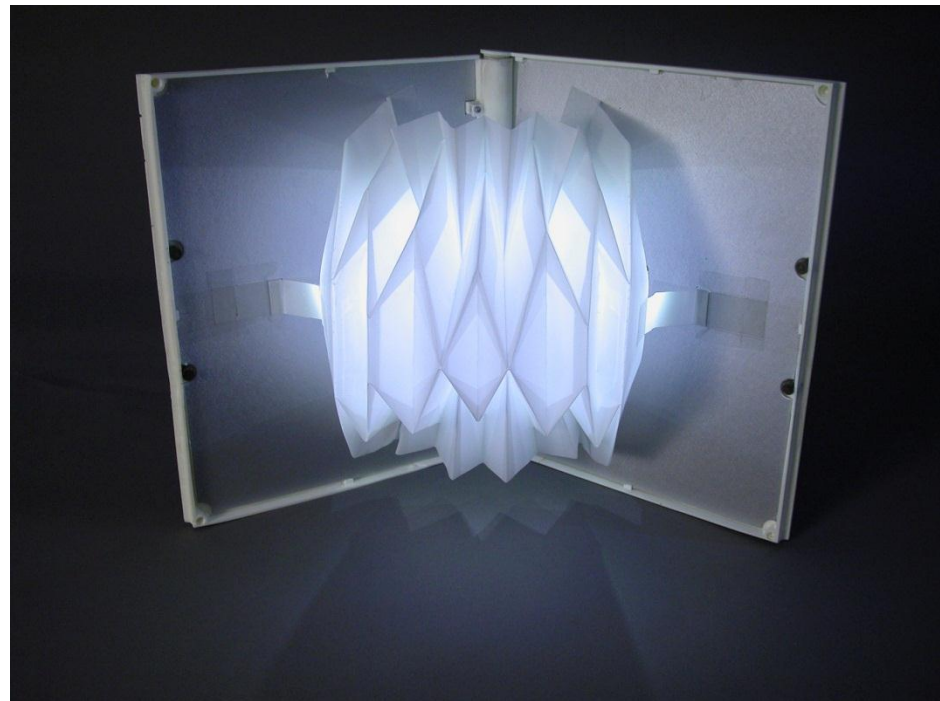
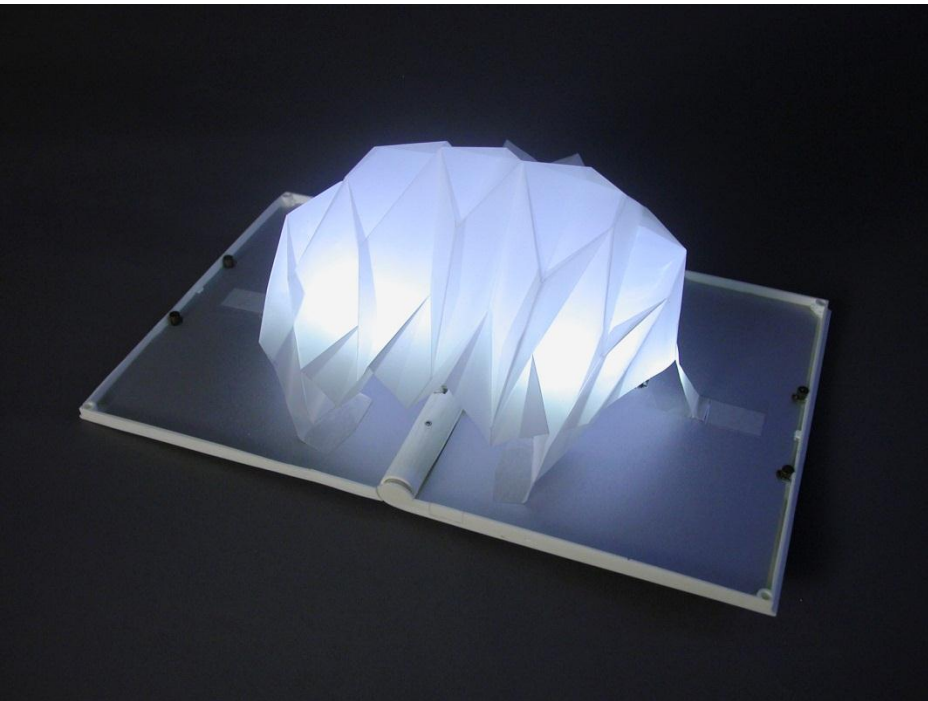
# Curvature in patterned folding



waterbomb tessellation  
("Namako" by Shuzo Fujimoto)



# Kinetic Origami

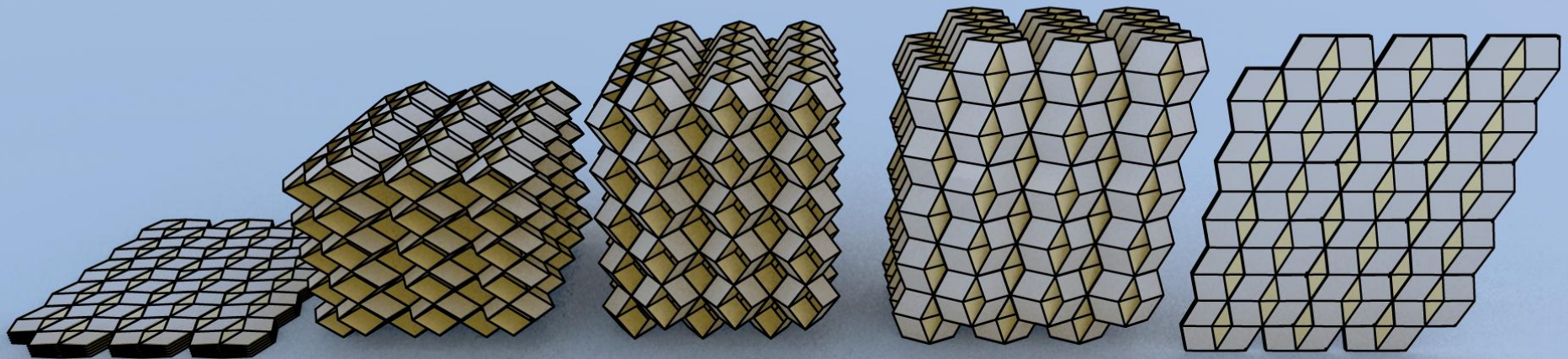




# Space-filling Origami

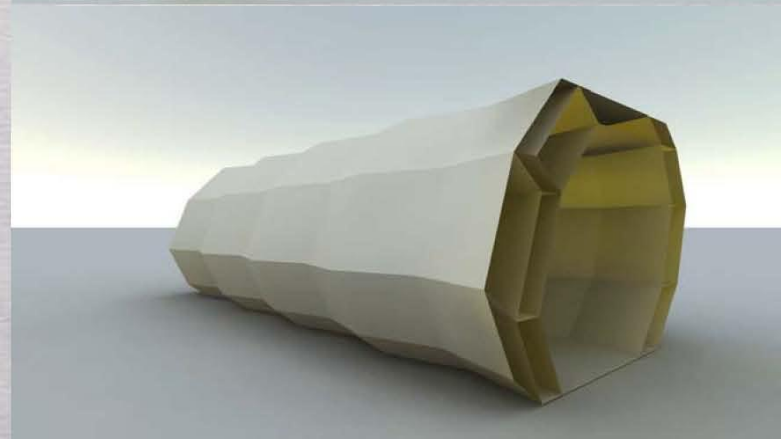
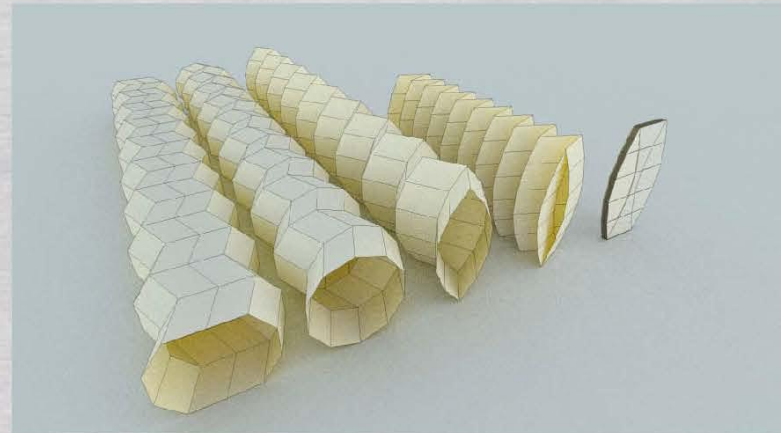
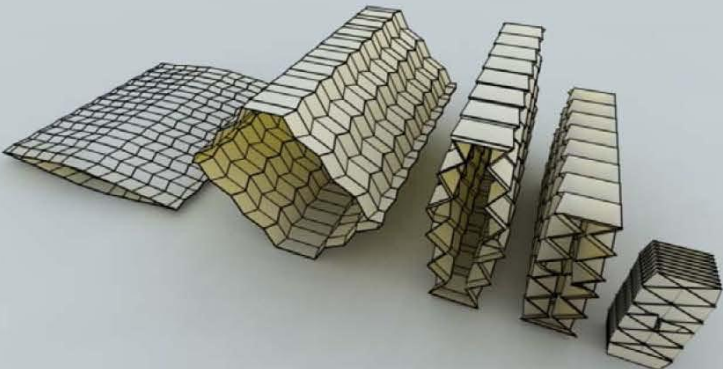
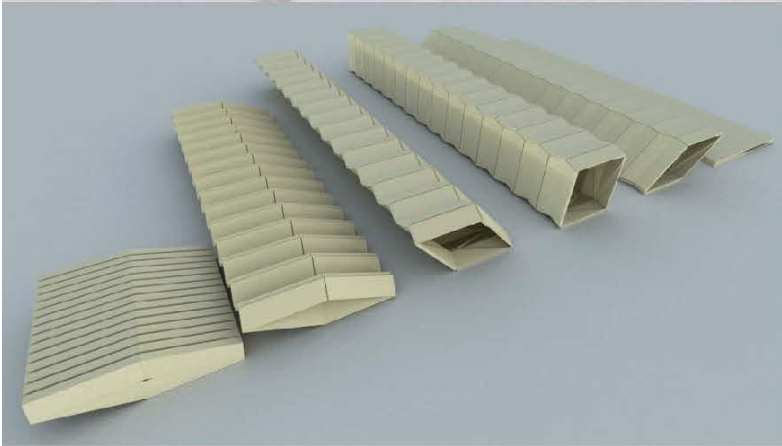
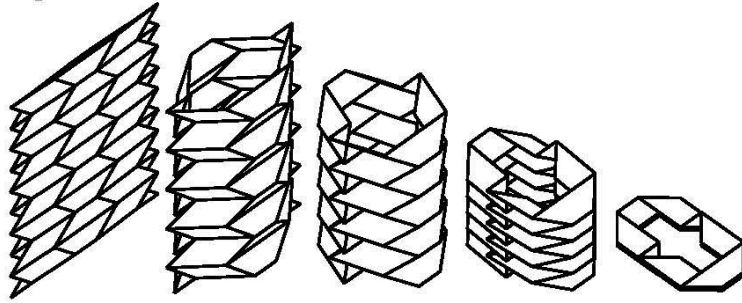
Tomohiro Tachi

University of Tokyo



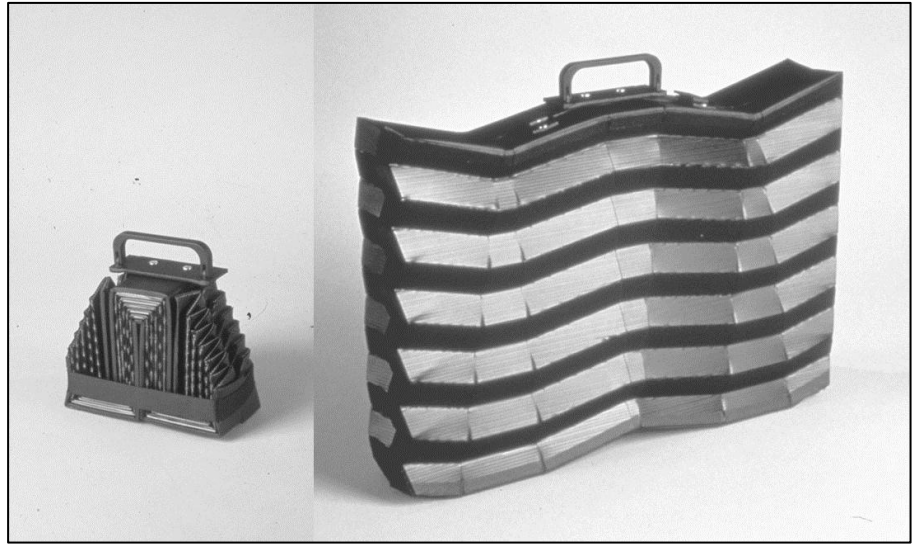
Tomohiro Tachi

# ↳ Symmetric Structure Variations





# Miura folding with thick materials





# Material Thickness in Miura Ori (Hoberman)

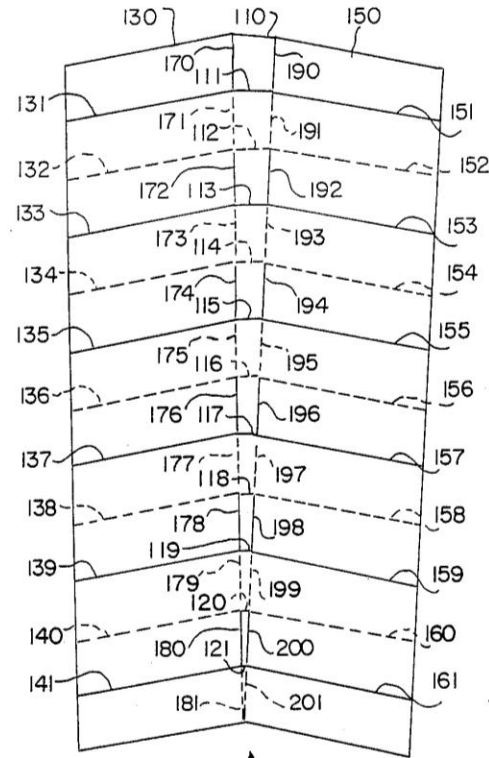
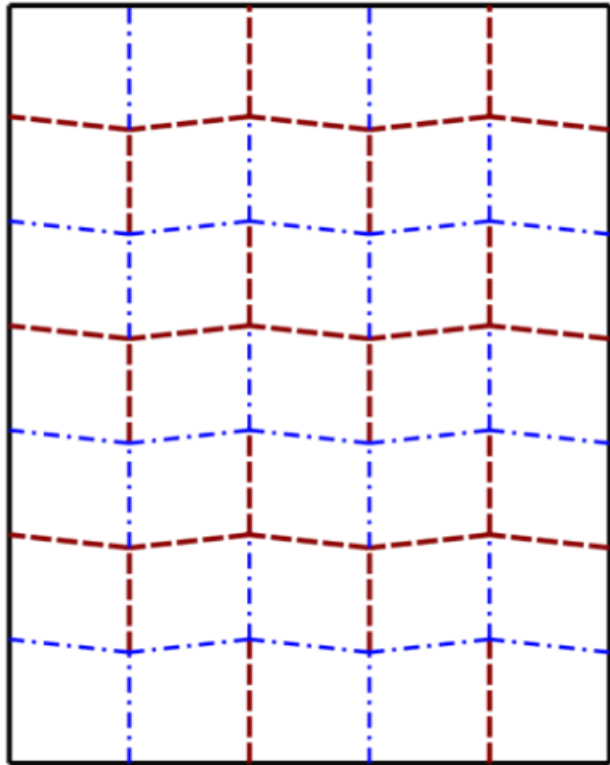


FIG. 1

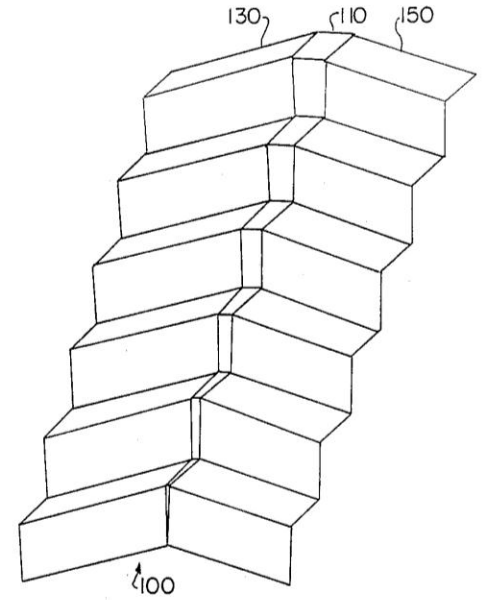


FIG. 2

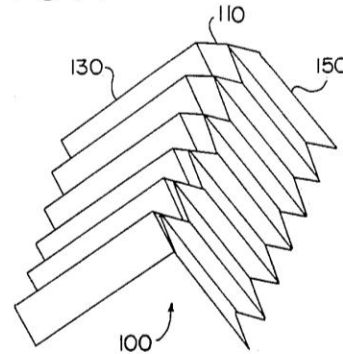


FIG. 3

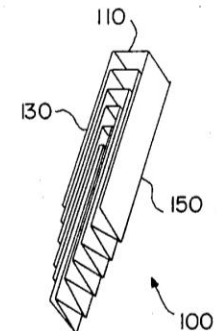


FIG. 4

FIG. 9

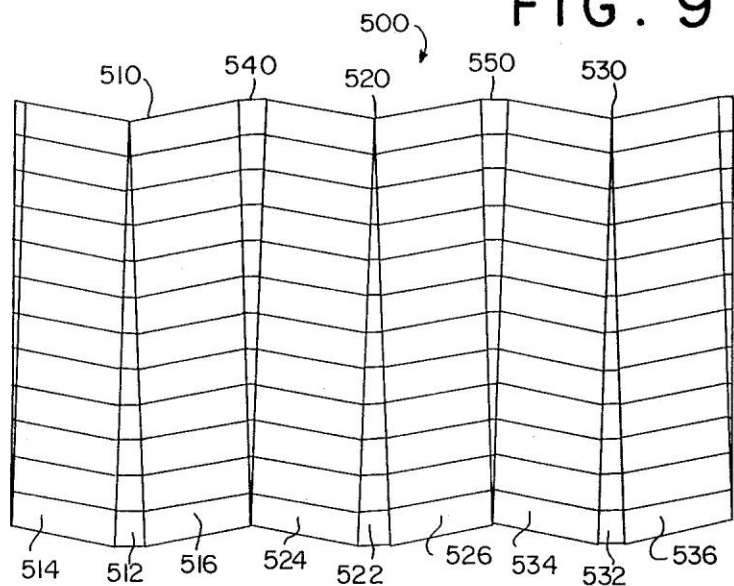


FIG. 10

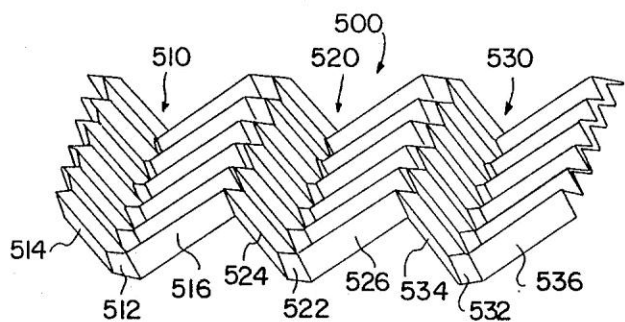
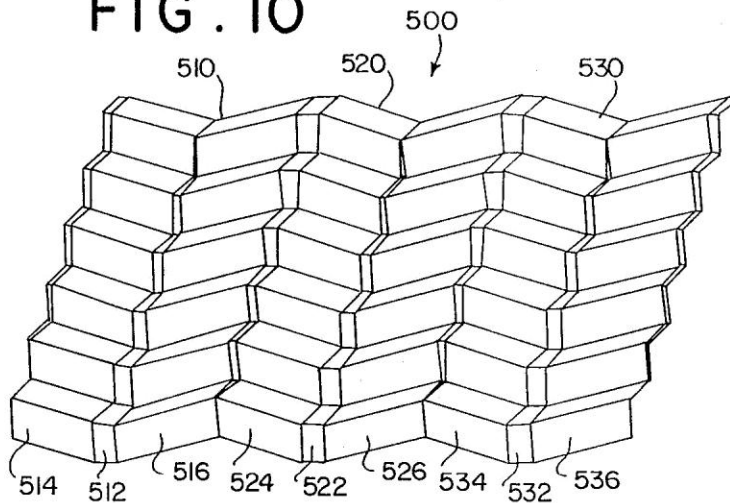
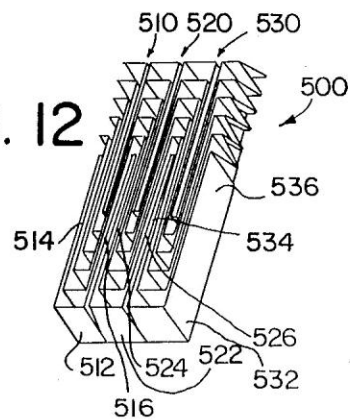
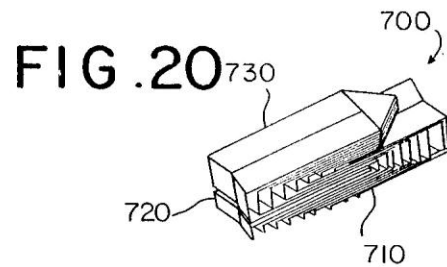
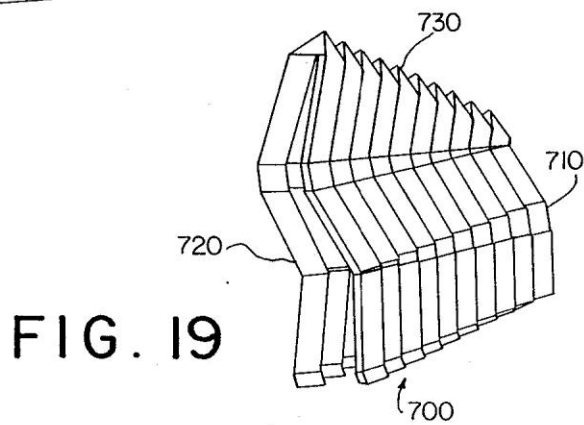
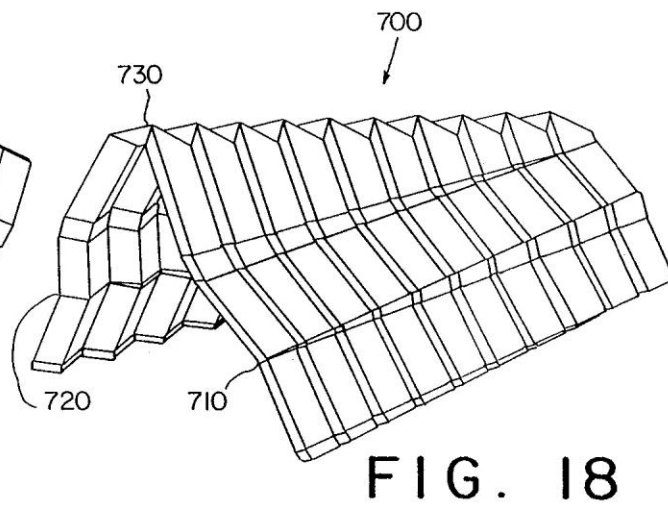
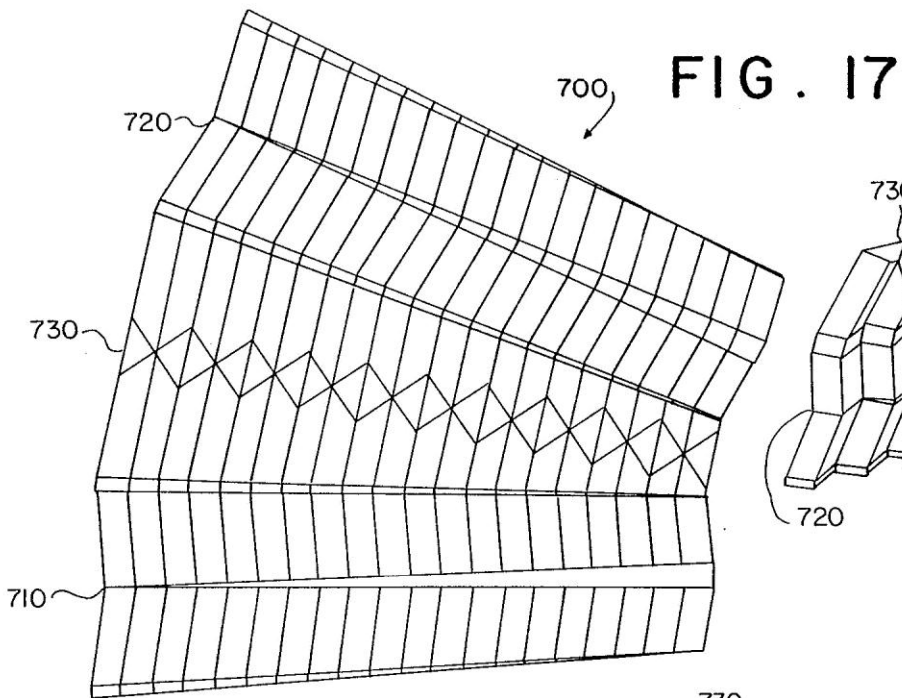
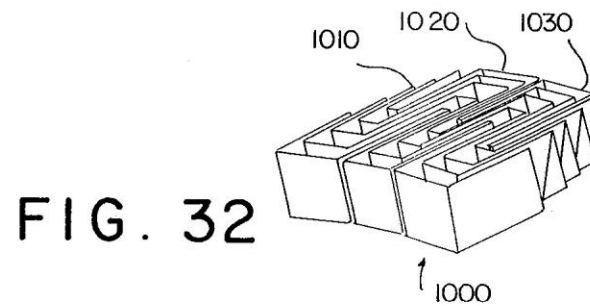
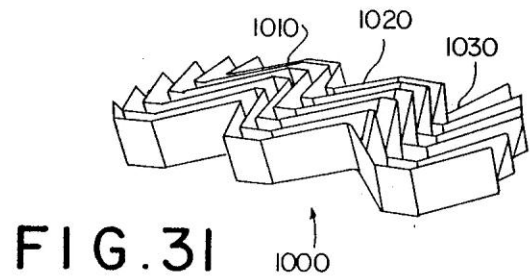
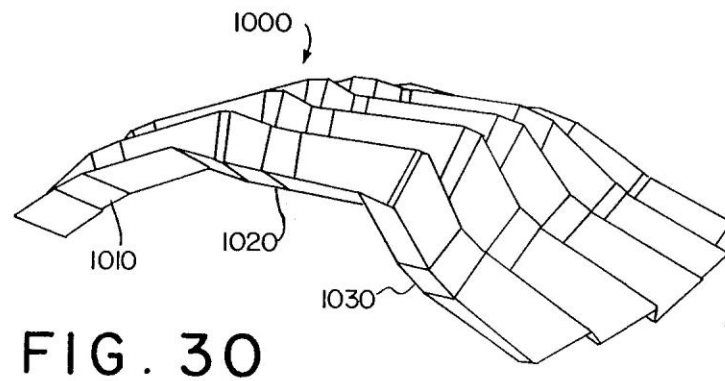
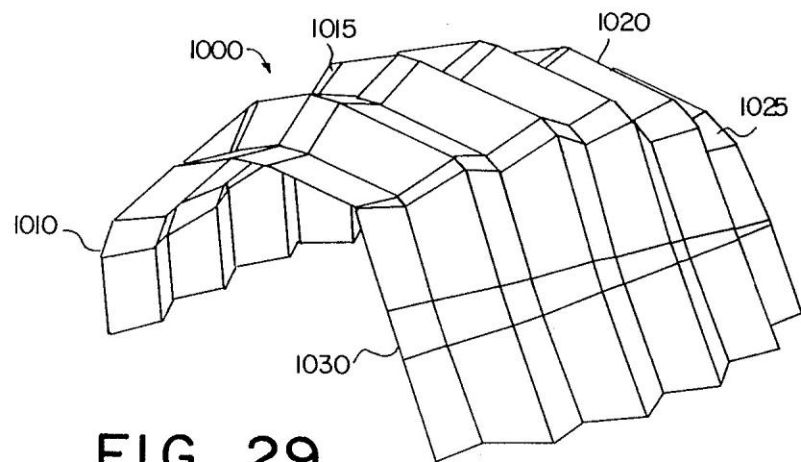


FIG. 11

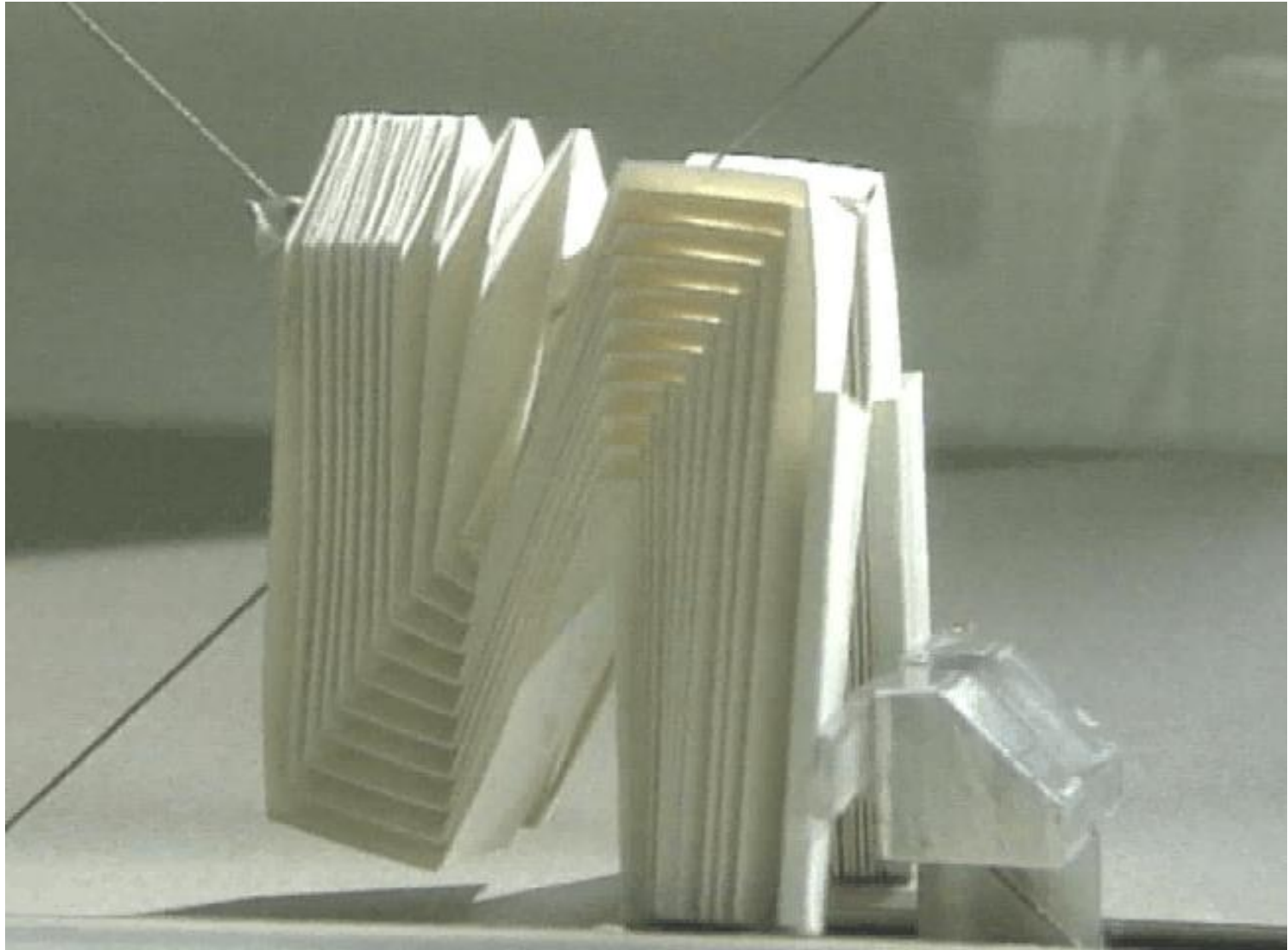
FIG. 12



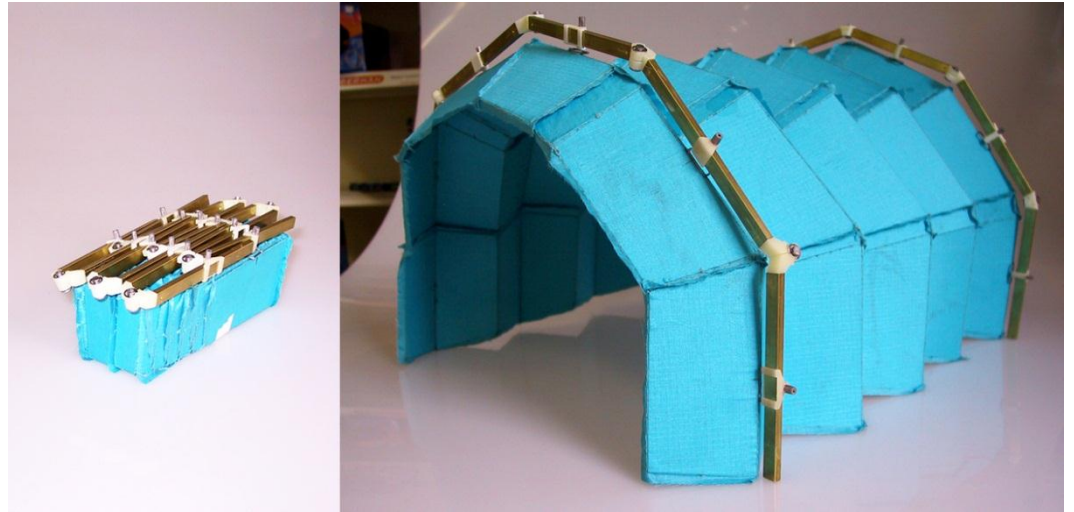




# Origami Mechanisms



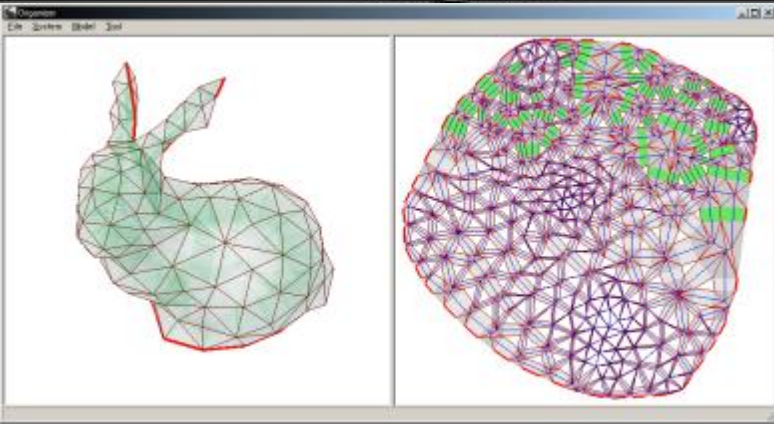
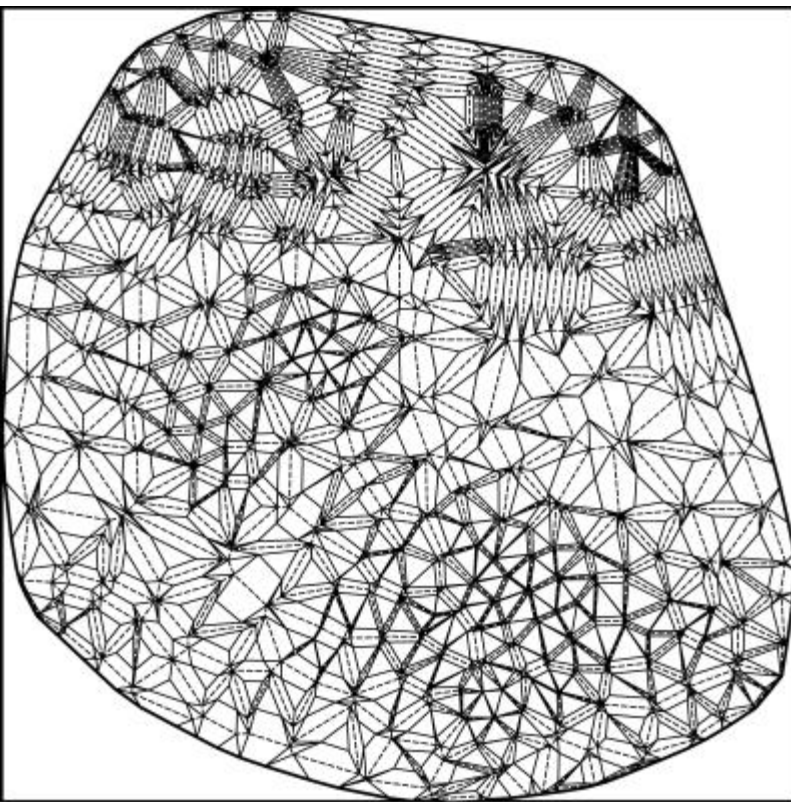
# Origami Mechanisms





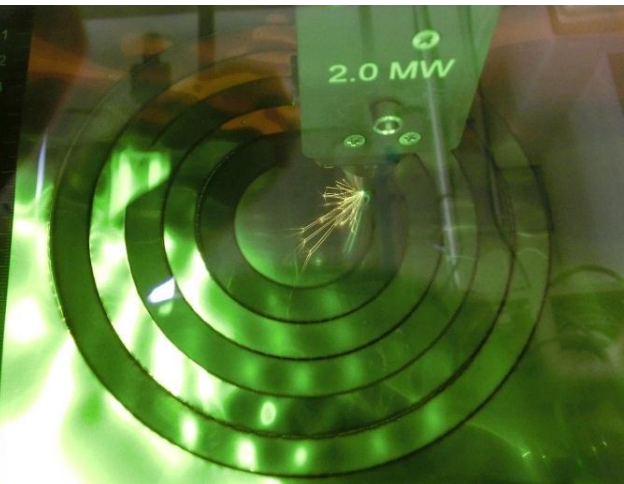
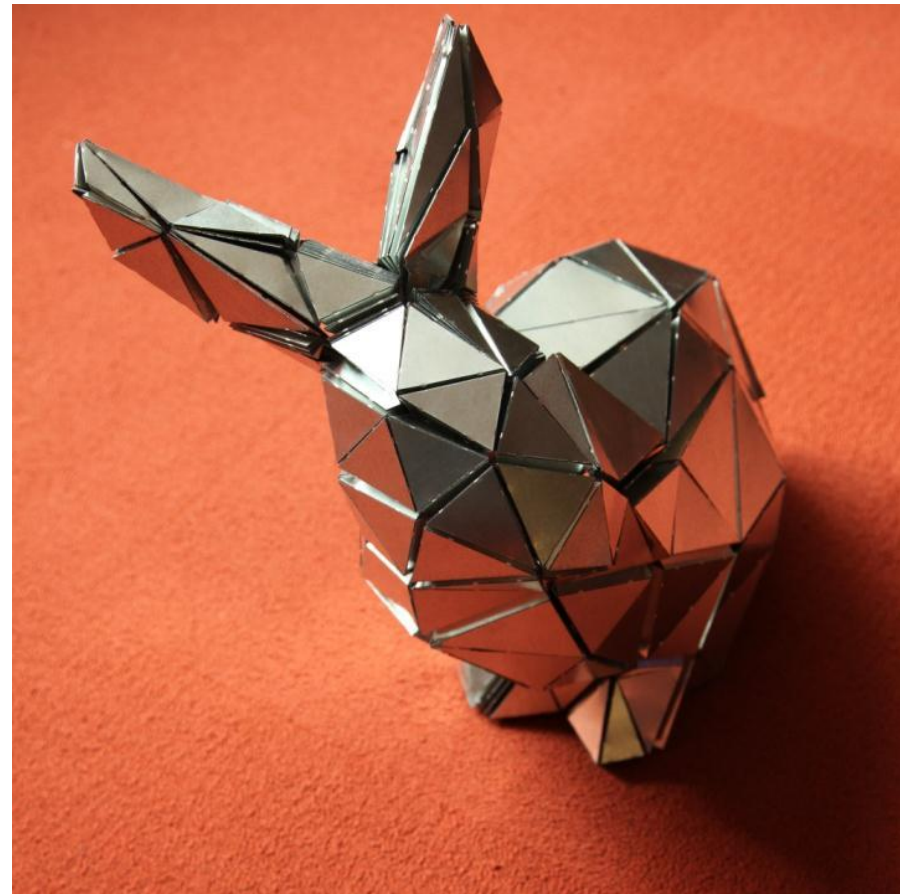
# Origami: Form

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University of Tokyo

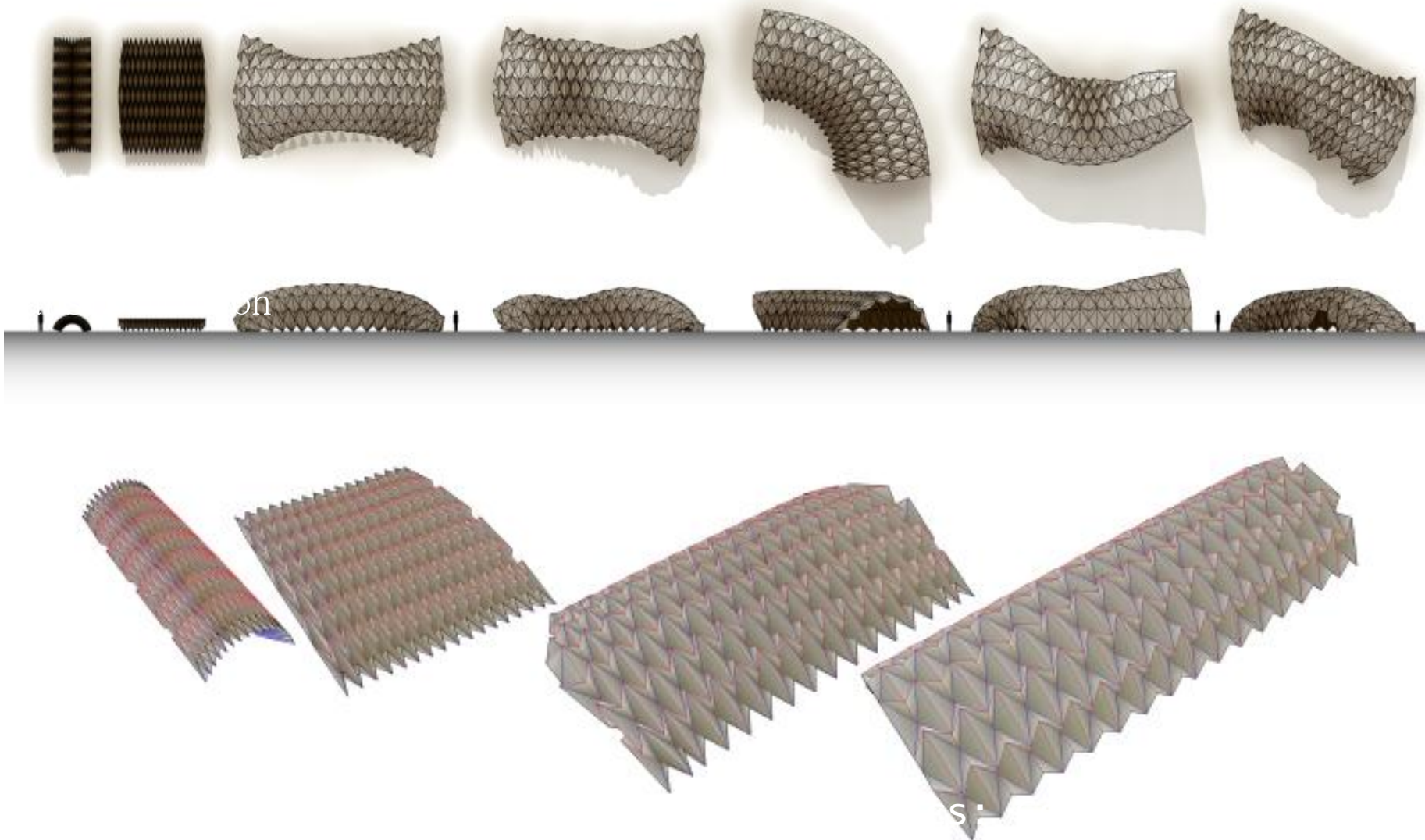




# Origami: Tomohiro Tachi Form University of Tokyo

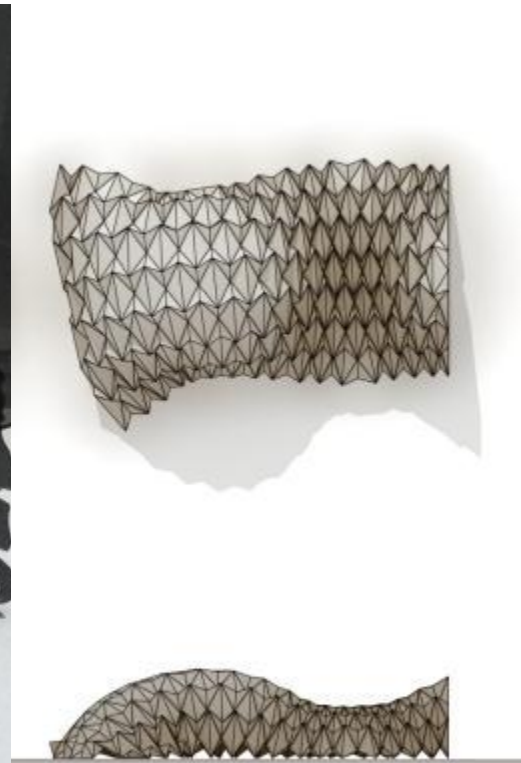
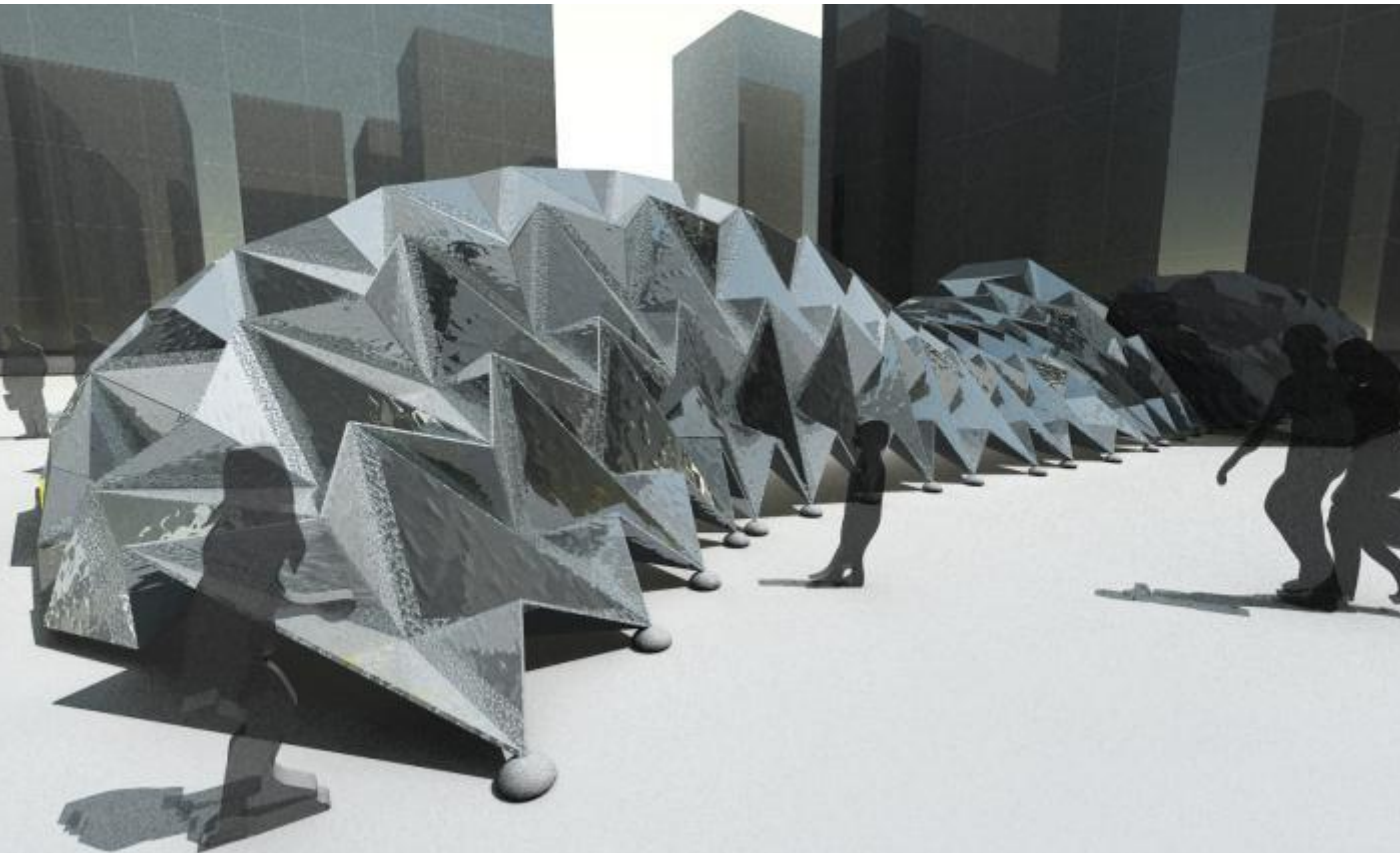


Tomohiro Tachi  
University of Tokyo

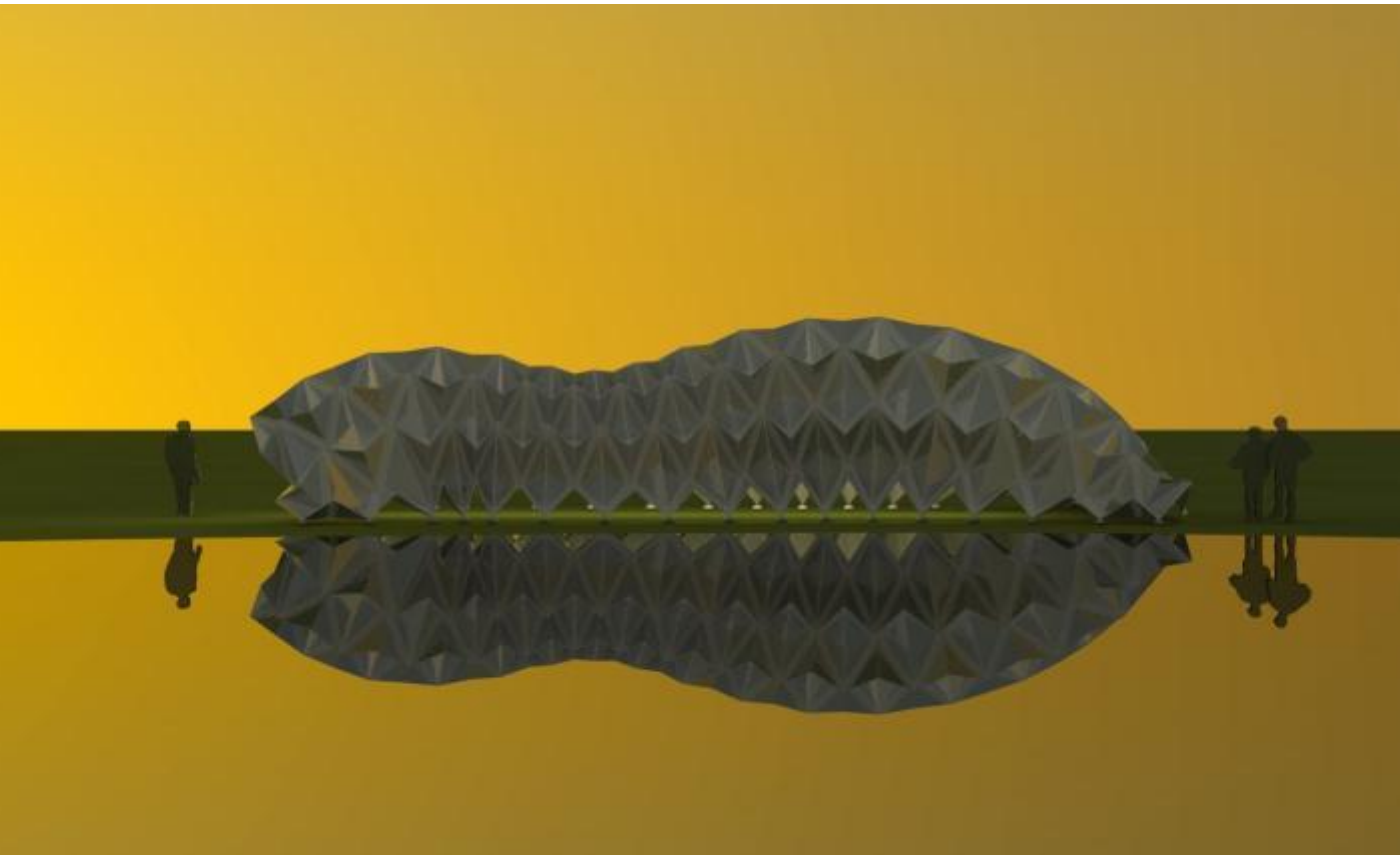




Tomohiro Tachi  
University of Tokyo

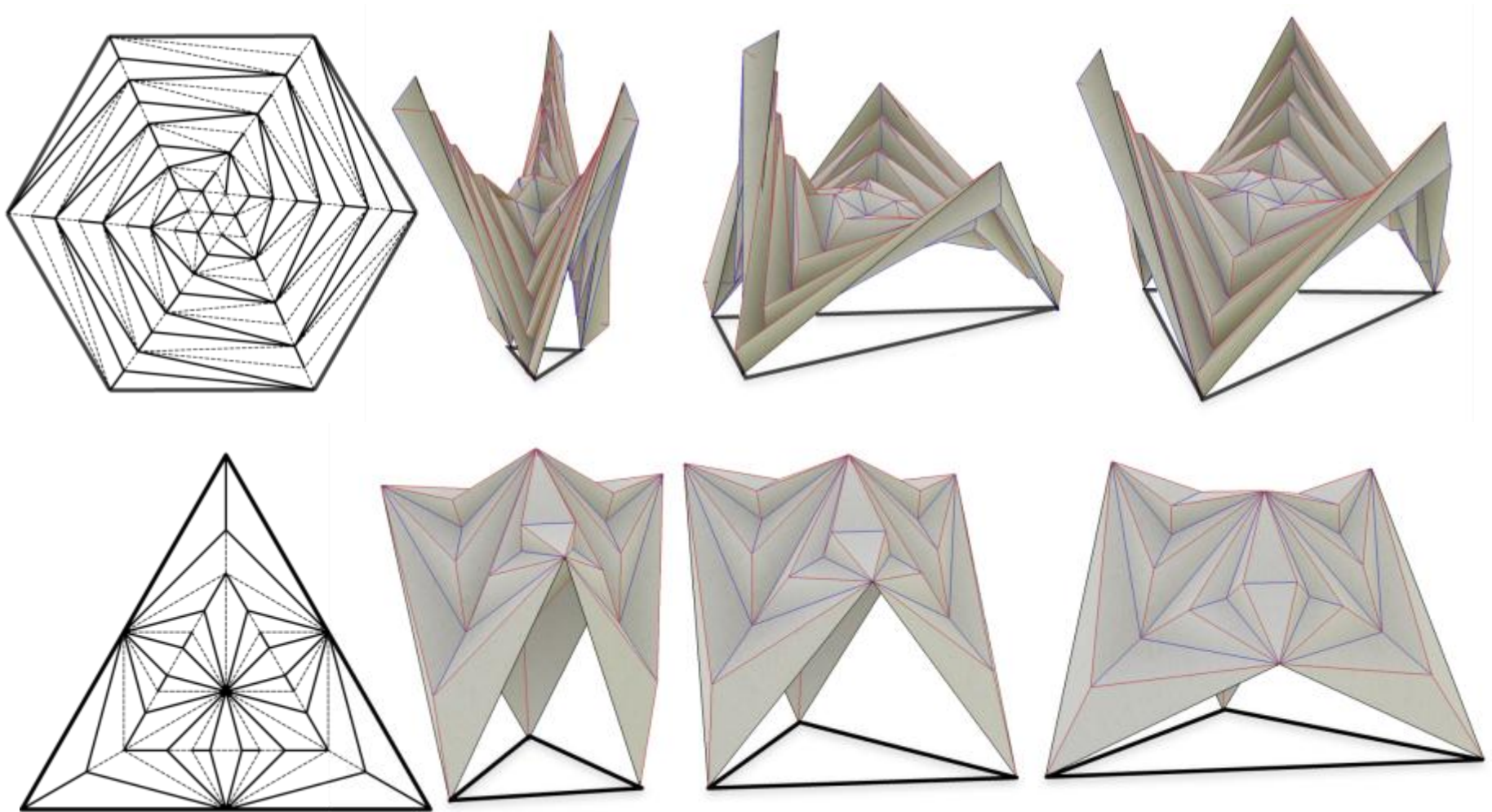


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University of Tokyo



Tomohiro Tachi  
University of Tokyo

## Hexagonal Tripod Shells





# Alternate methods for thick origami

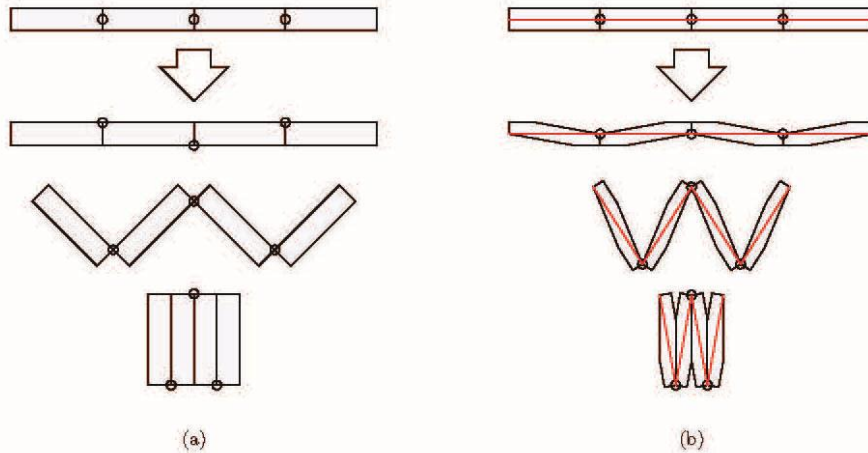
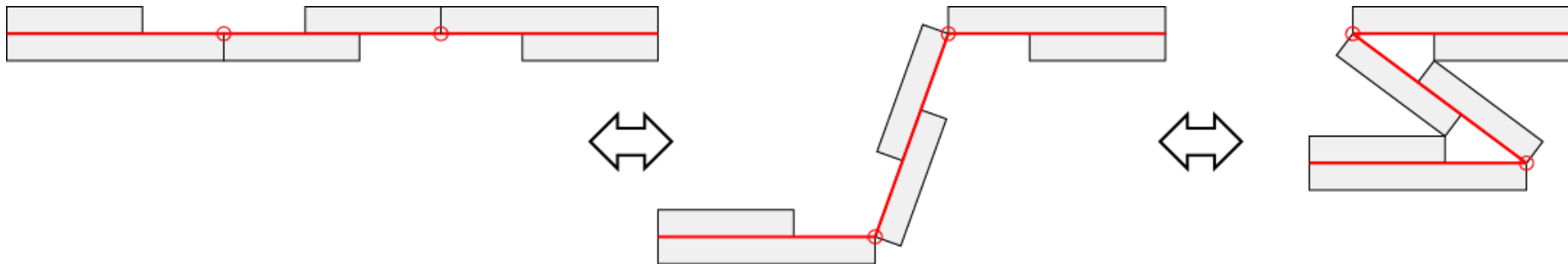


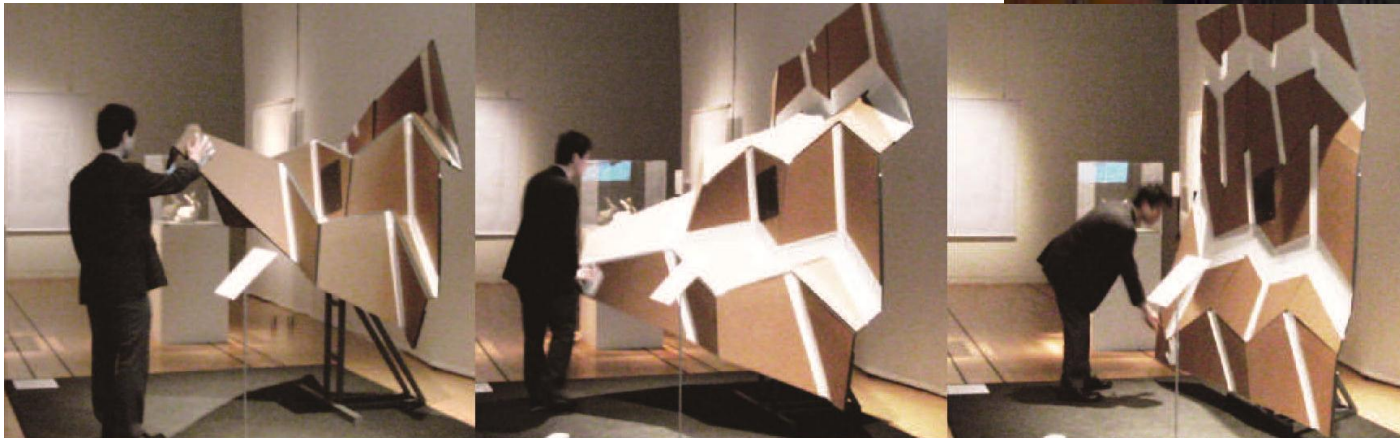
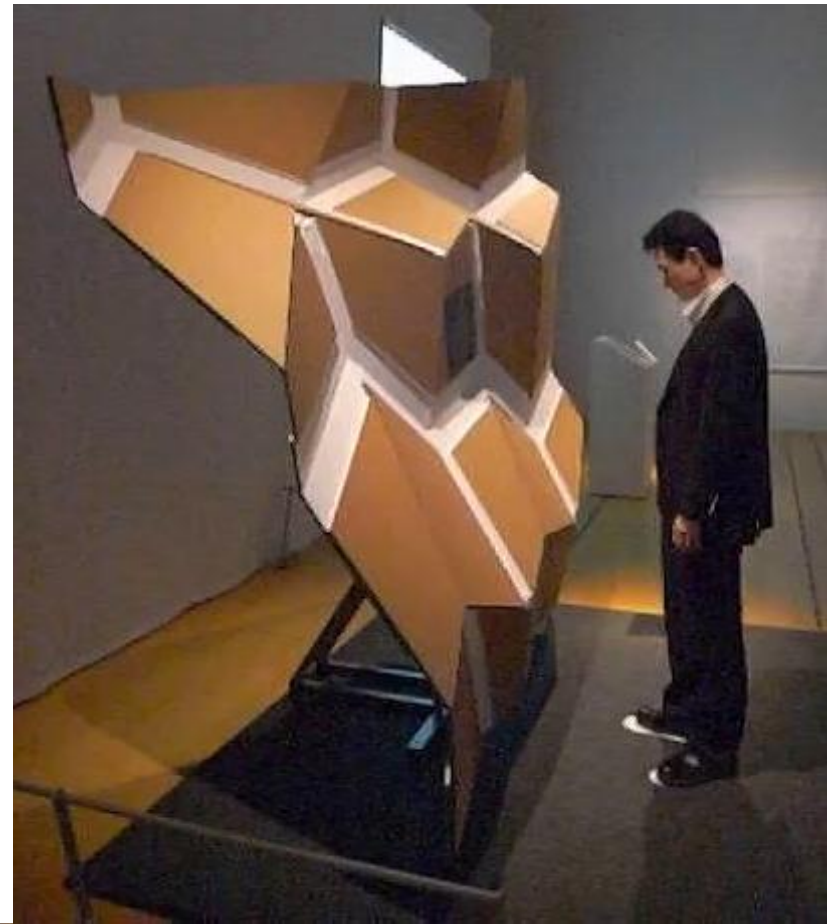
Figure 3: Two approaches for enabling thick panel origami. (a) Axis-shift. (b) The proposed method based on trimming by bisecting planes. Red path represents the ideal origami without thickness.



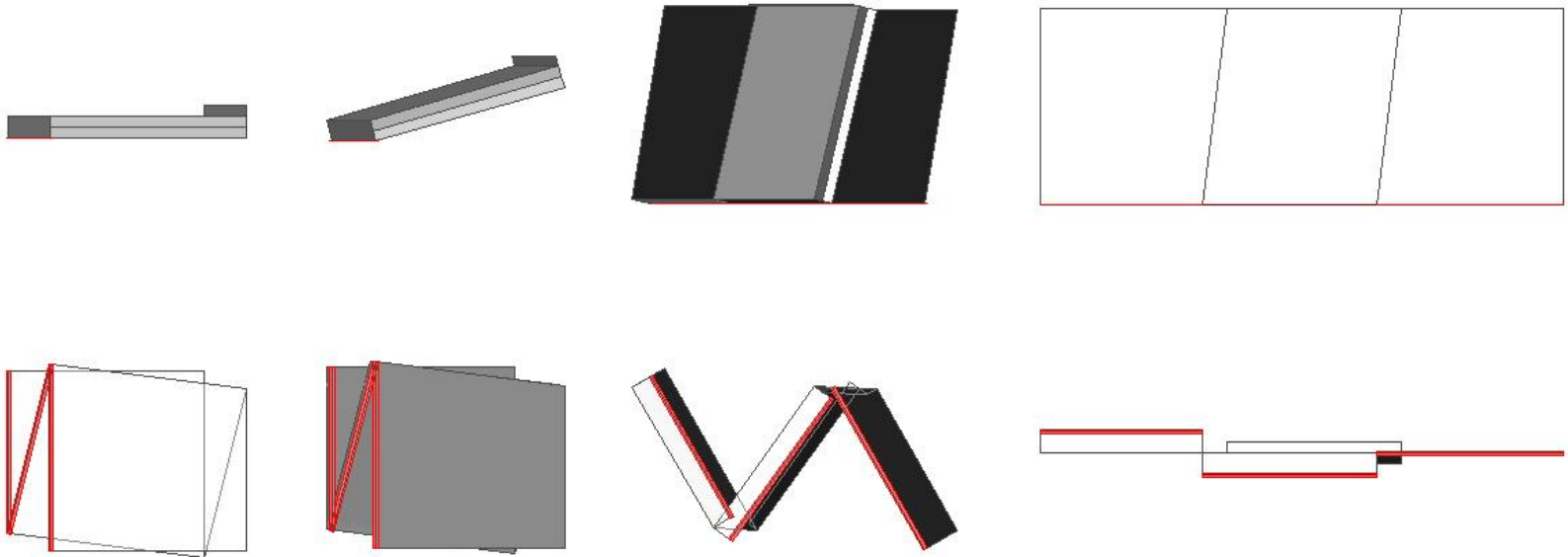
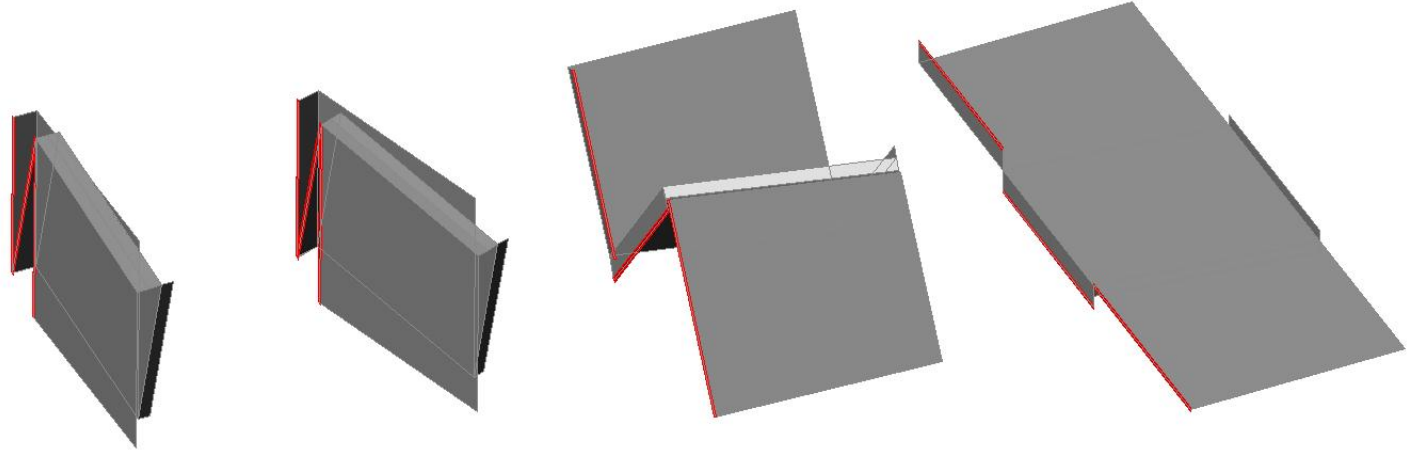
# Tomohiro Tachi

## University of Tokyo

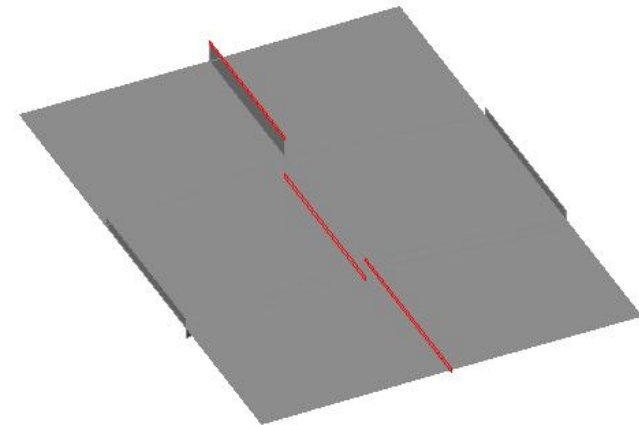
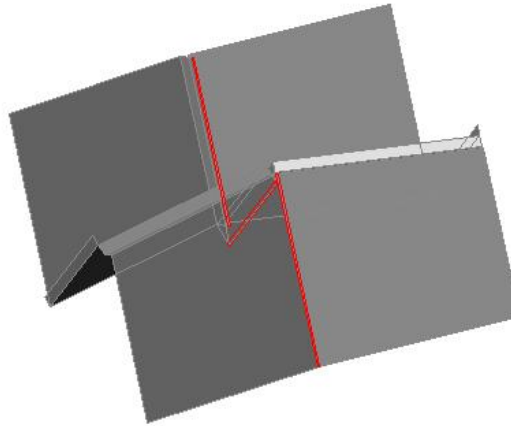
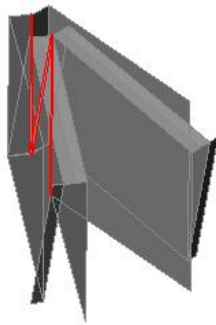
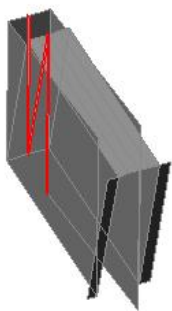
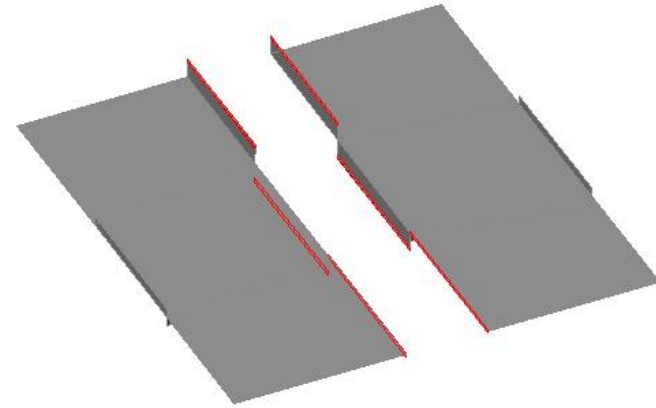
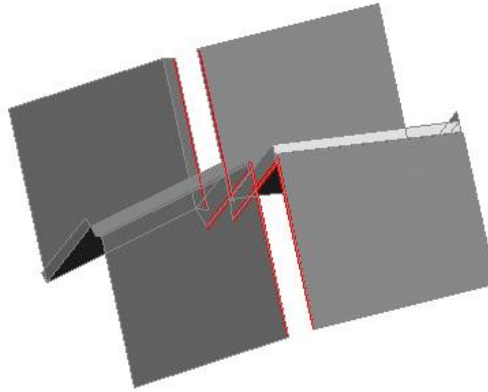
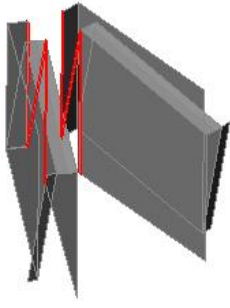
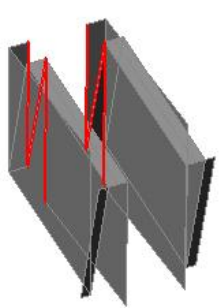
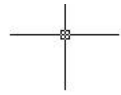
- Material
  - 10mm Structural Cardboard (double wall)
  - Cloth
- Size
  - 2.5m x 2.5m
- exhibited at NTT ICC



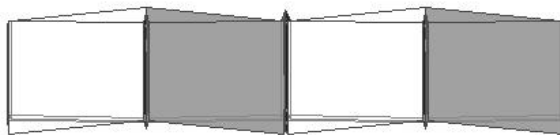
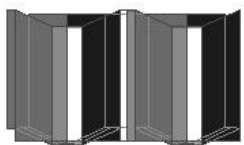
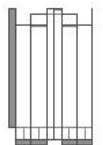
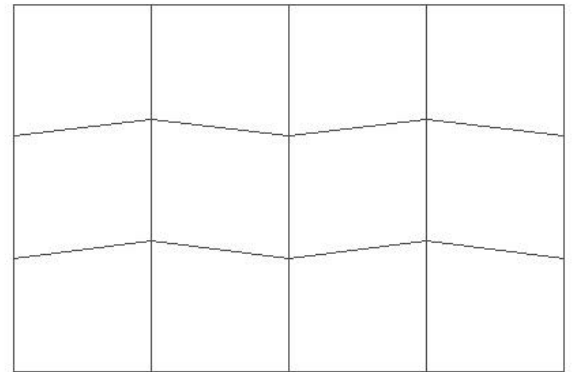
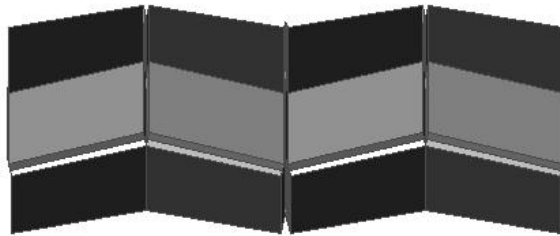
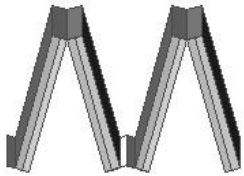
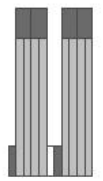
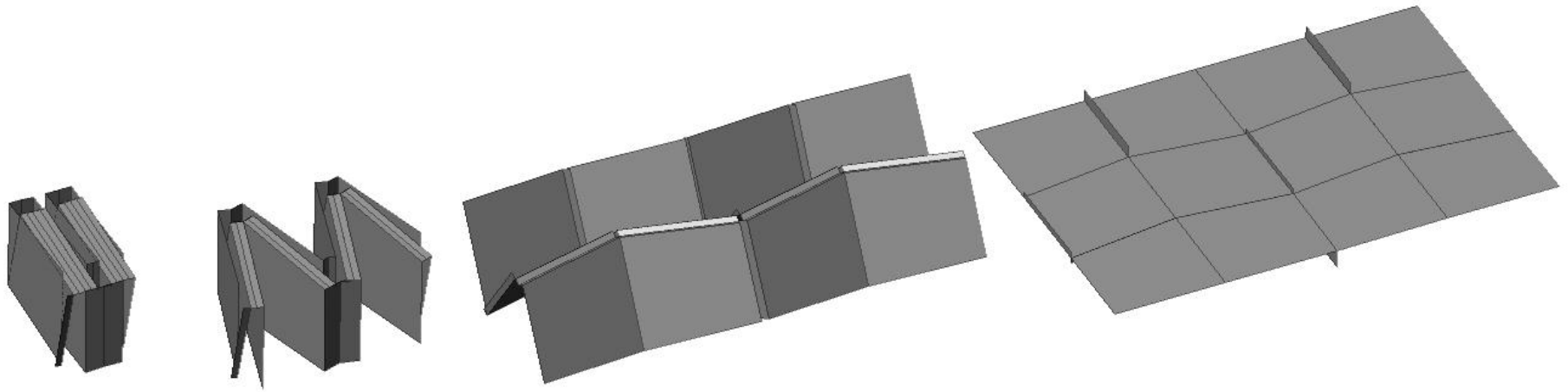
# 'Thick' Origami (Hoherman)



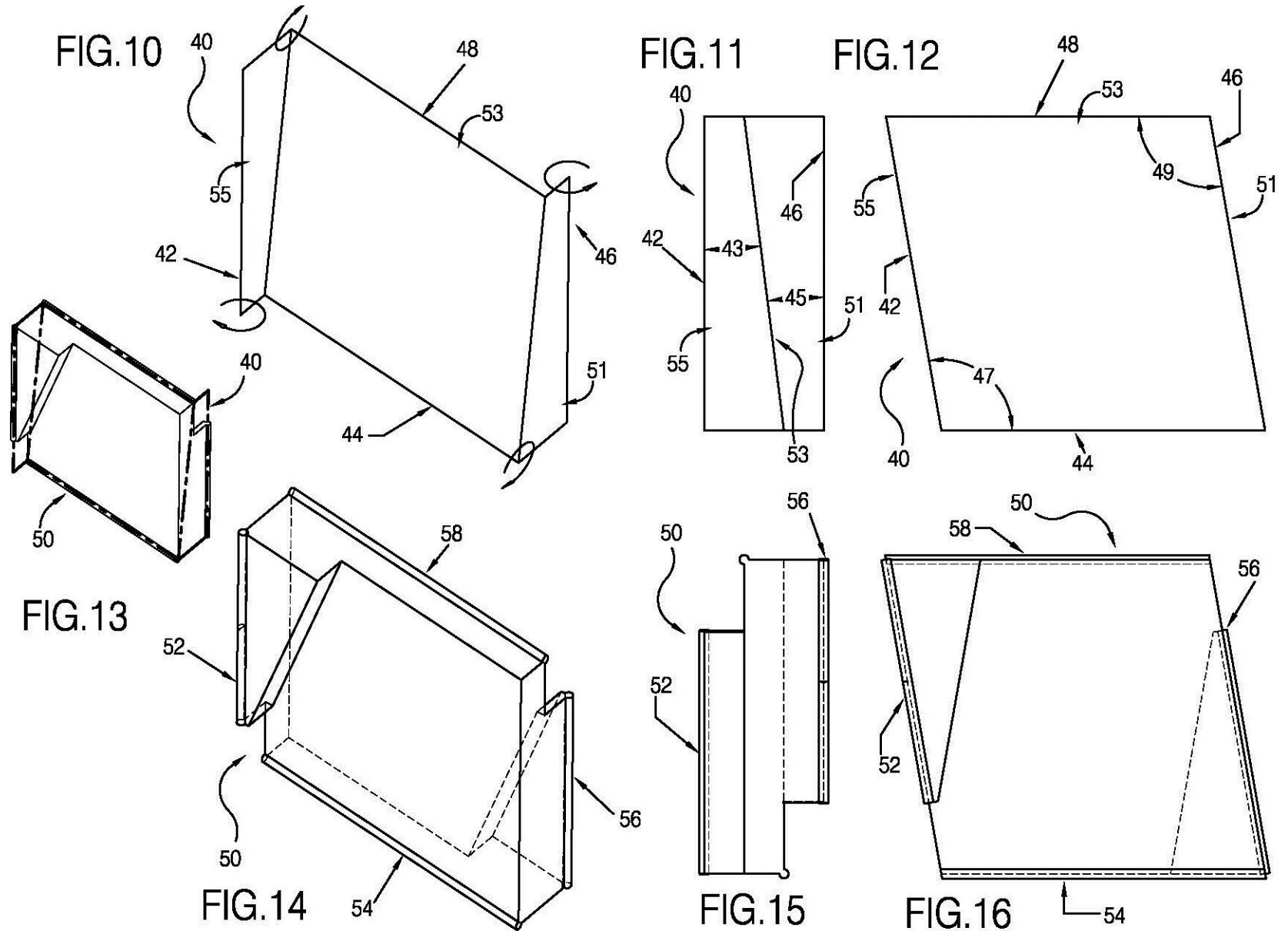
# 'Thick' Origami (Hoberman)



# 'Thick' Origami (Hoberman)



# 'Thick' Origami (Hoberman)





# 'Thick' Origami

FIG.17

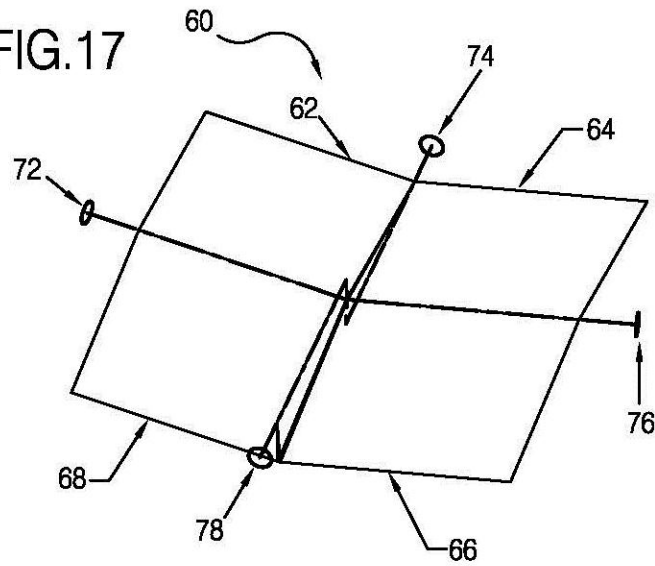


FIG.18

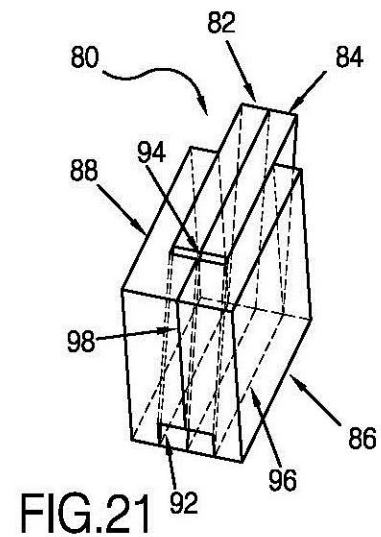
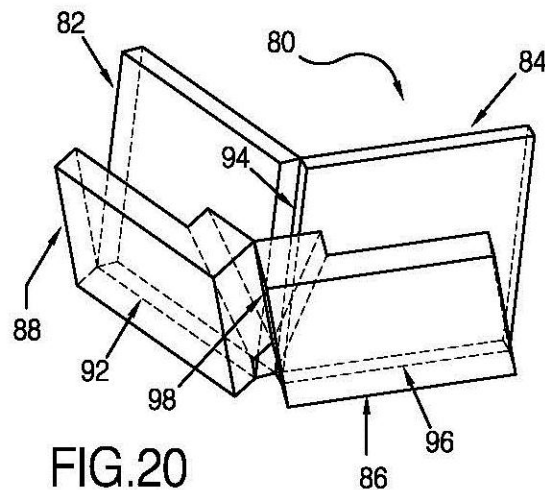
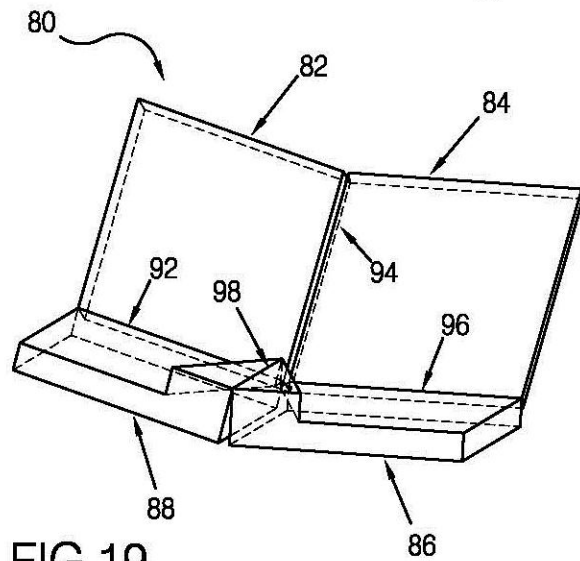
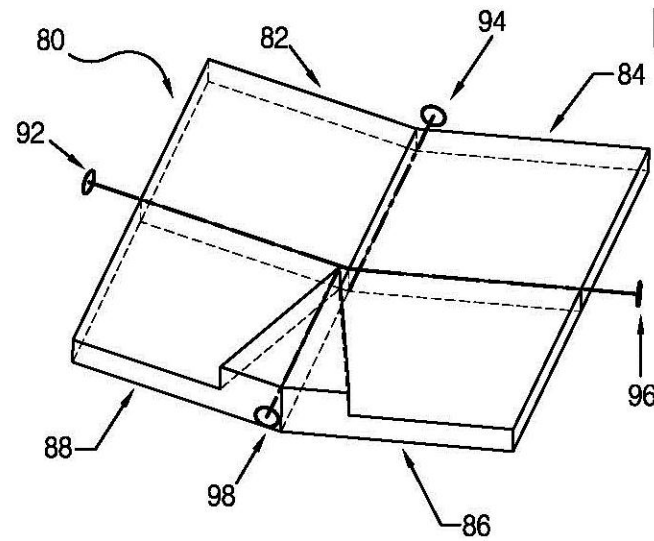
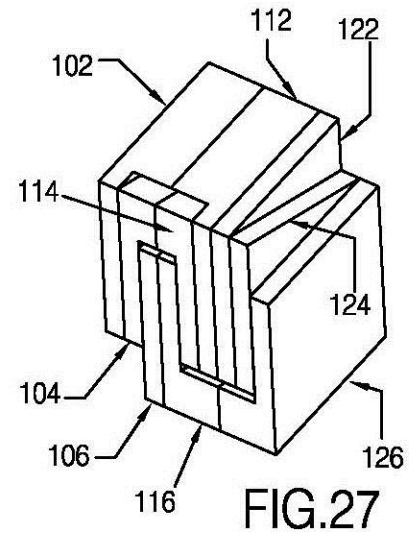
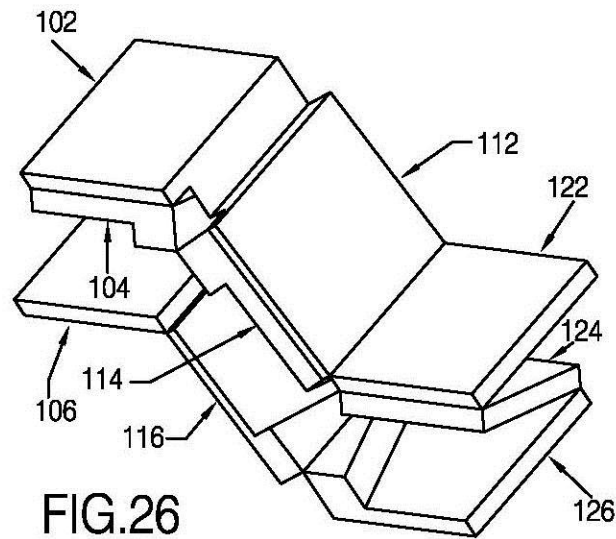
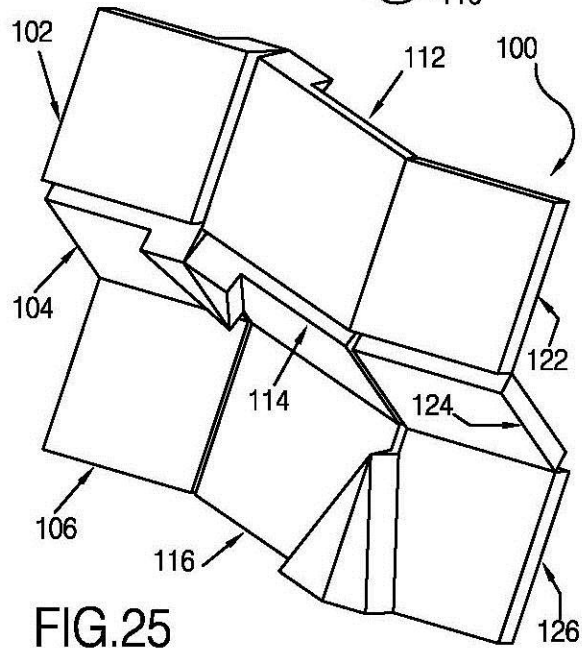
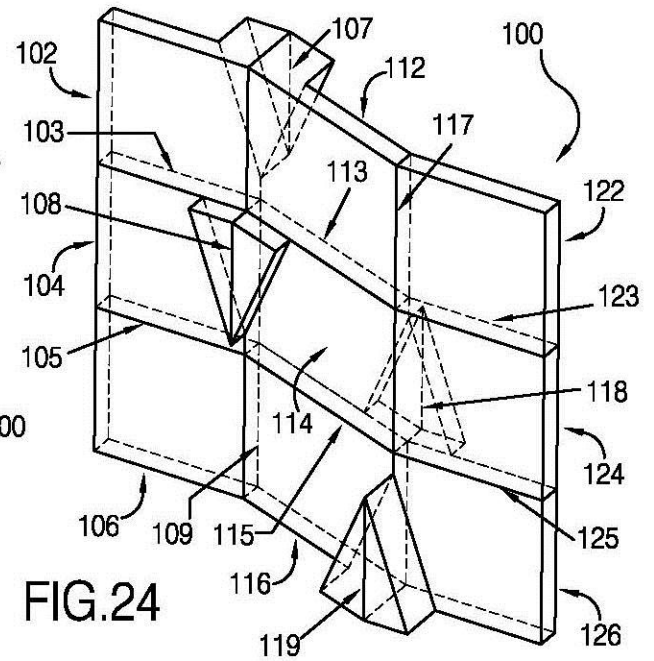
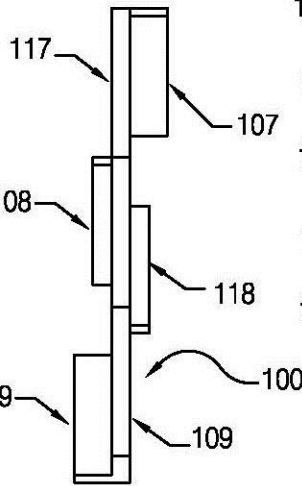
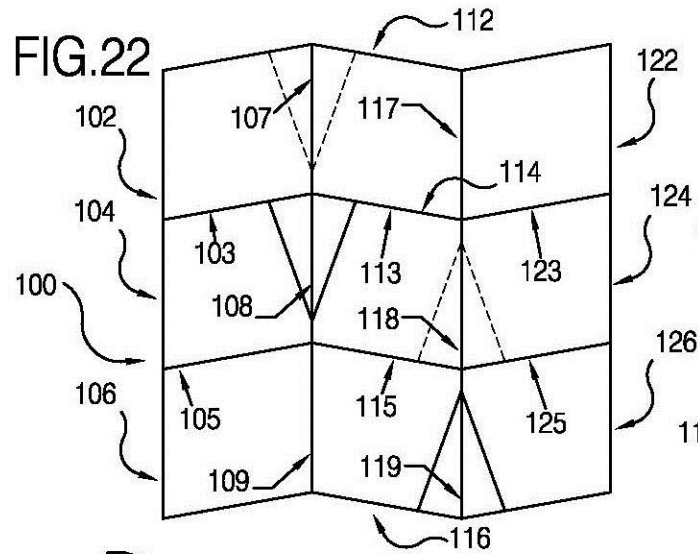


FIG.19

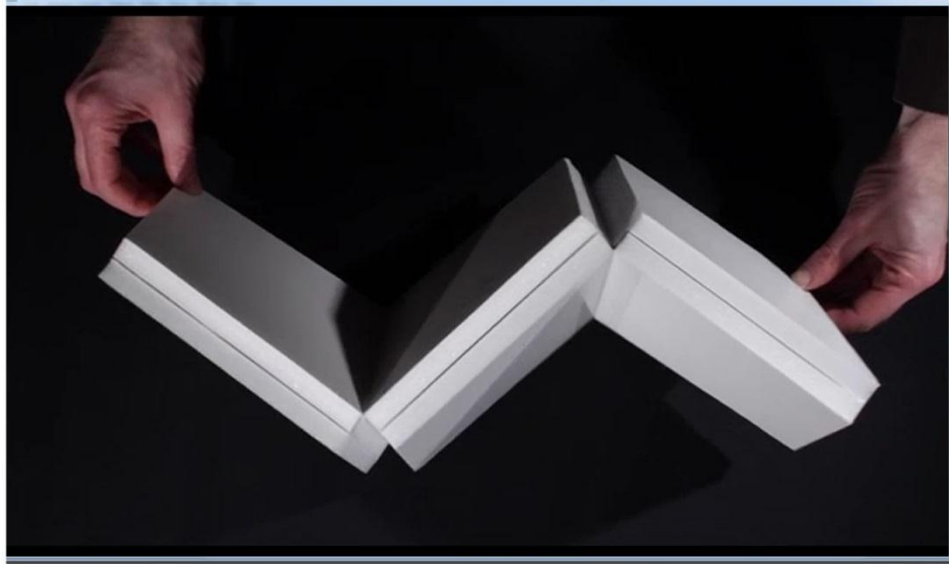
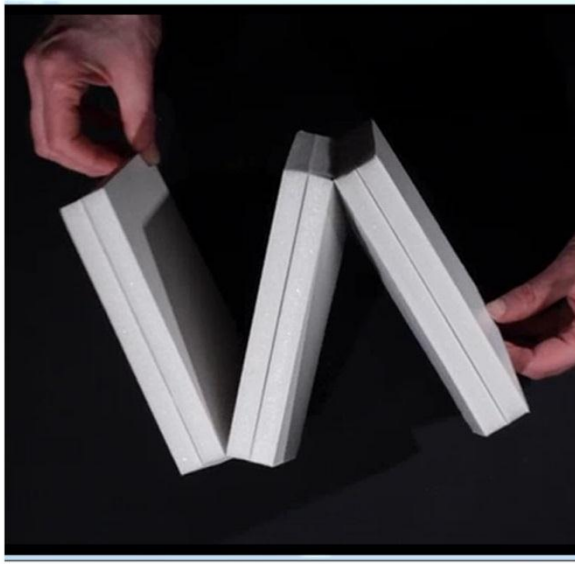
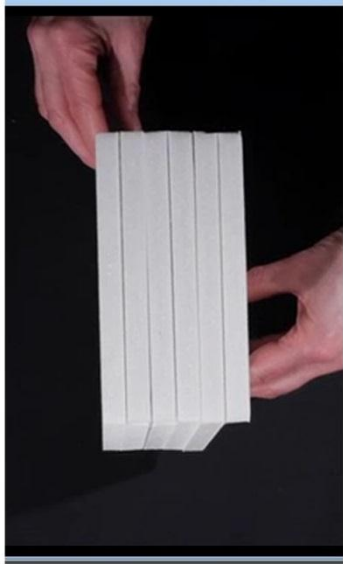
FIG.20

FIG.21

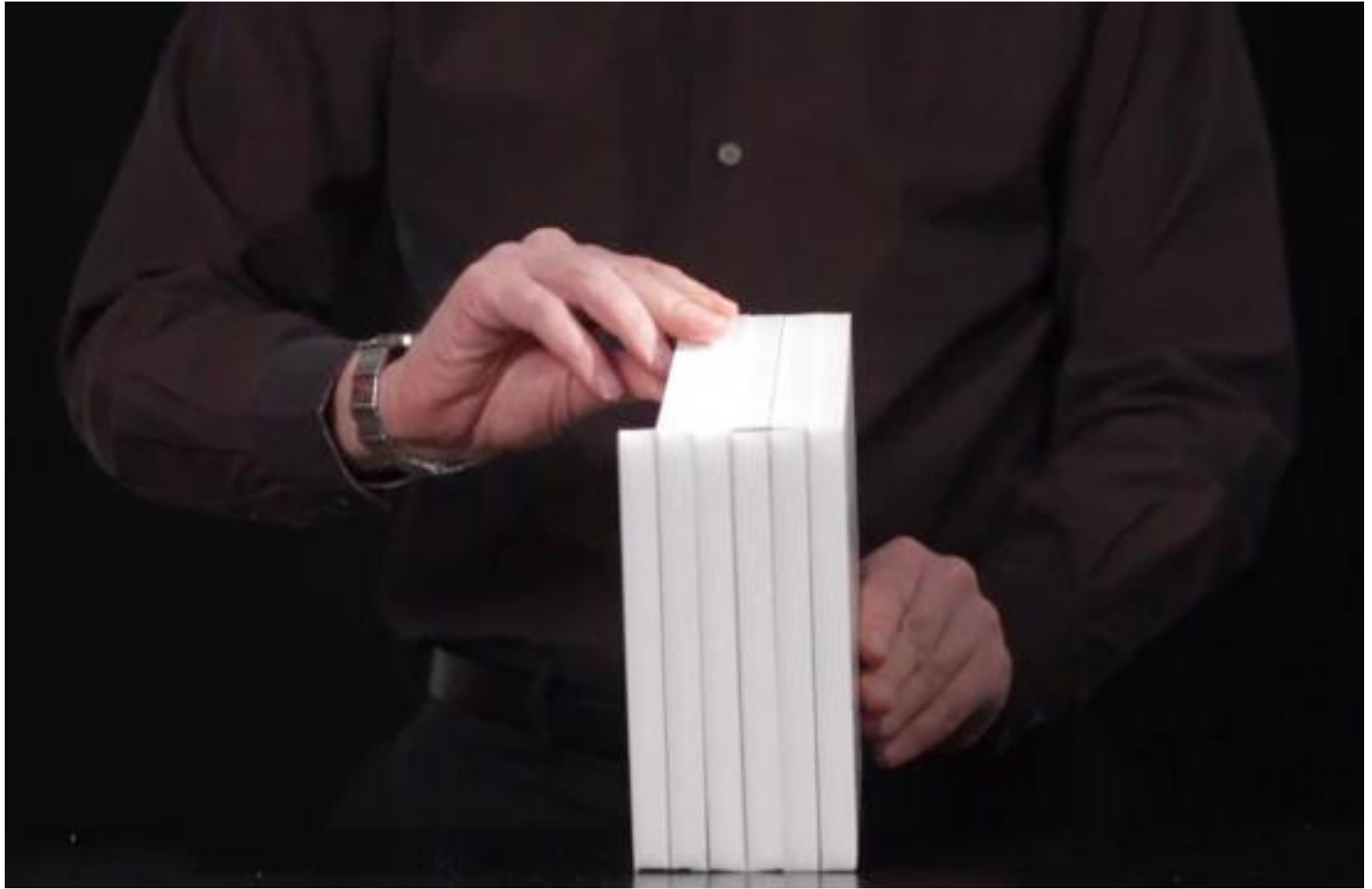
# 'Thick' Origami



# Kinetic Origami

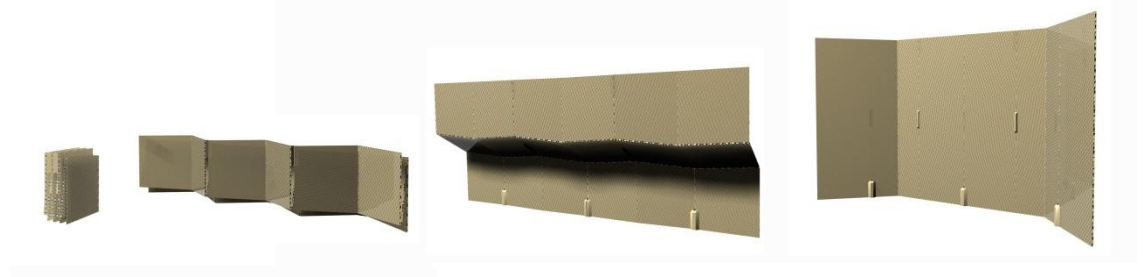


# Thick Origami





# Kinetic Origami



# Kinetic Origami



FIG. 47

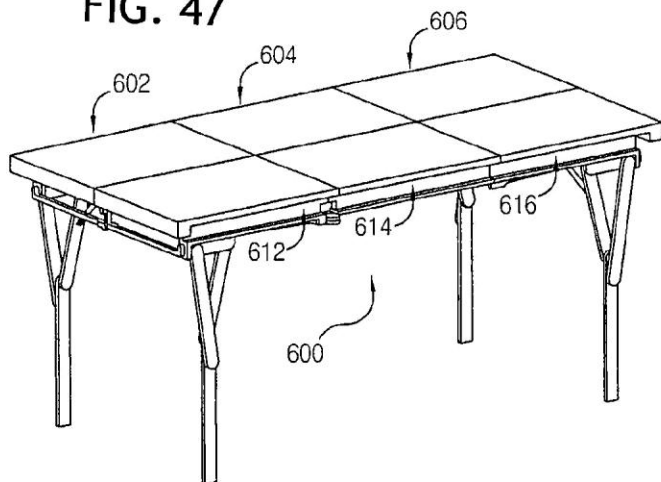


FIG. 48

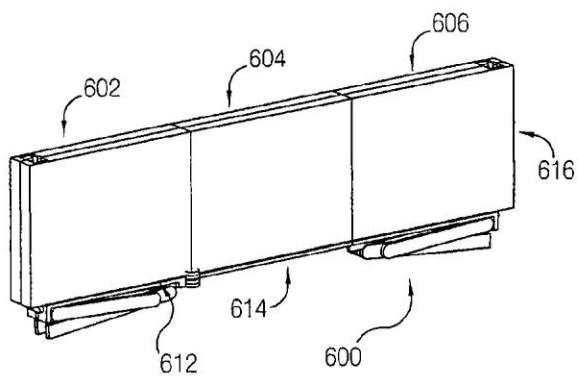
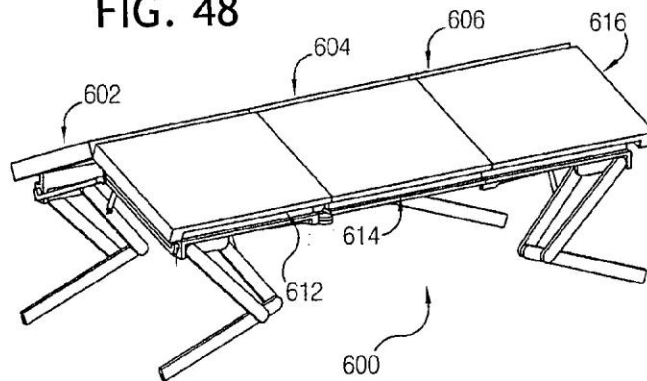


FIG. 49

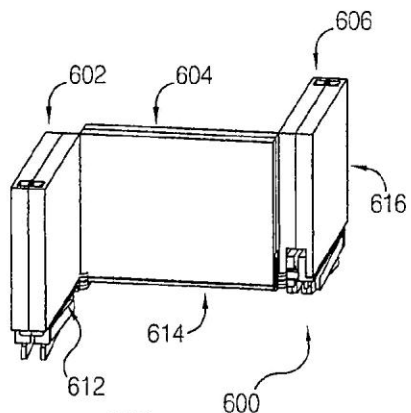


FIG. 50

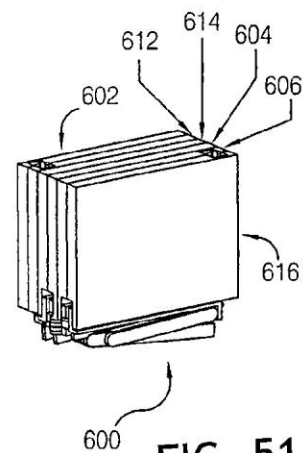


FIG. 51

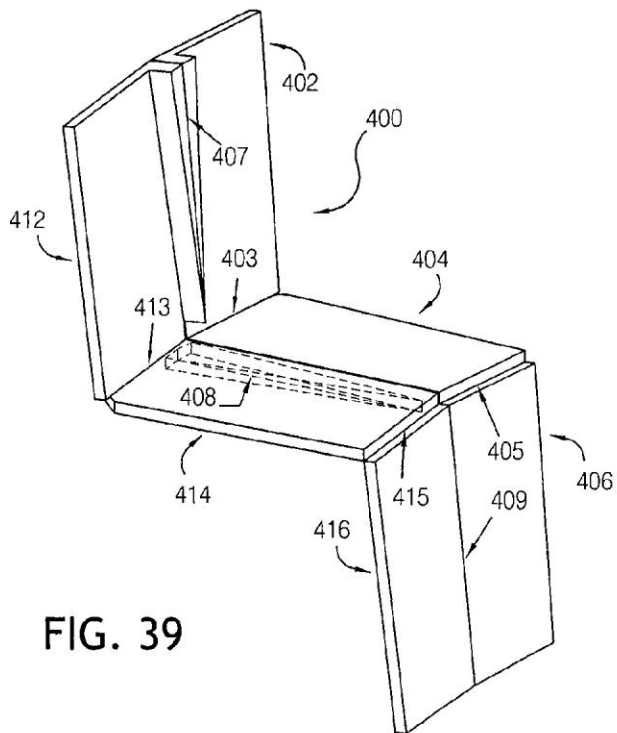


FIG. 39

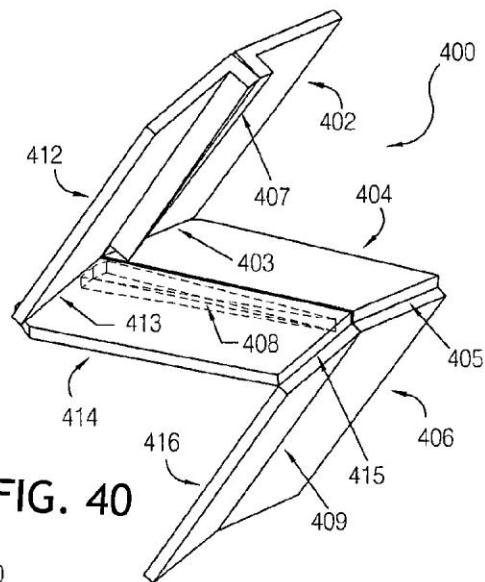


FIG. 40

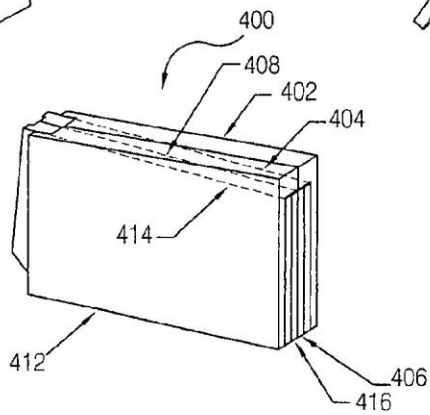


FIG. 41



FIG. 43

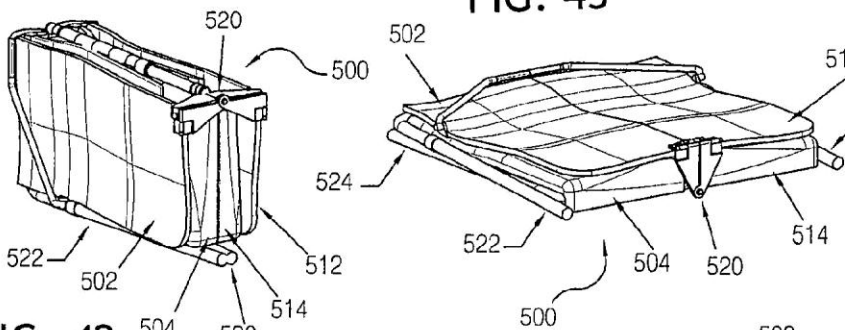


FIG. 42

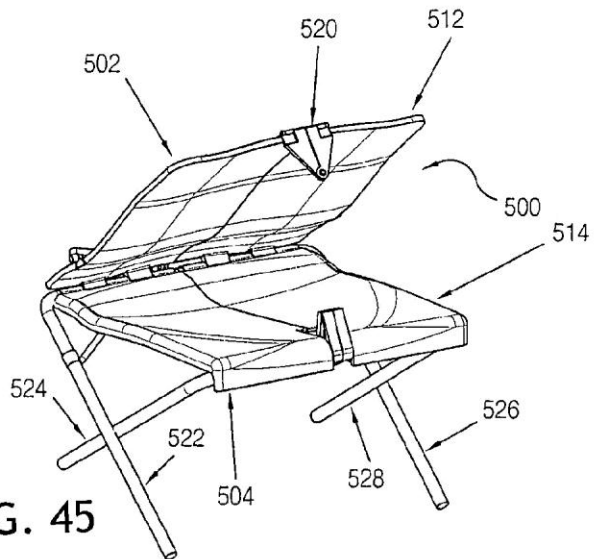


FIG. 45

FIG. 44

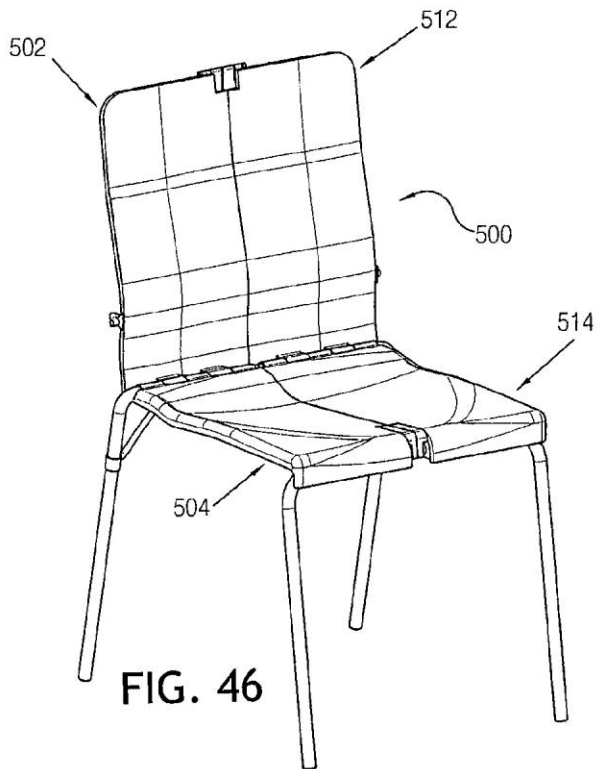
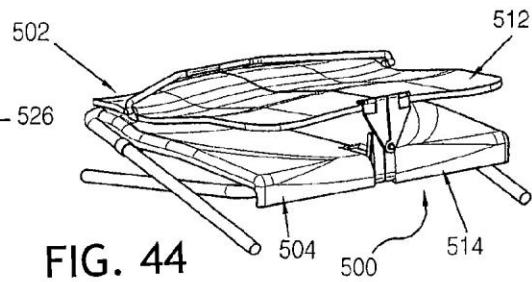


FIG. 46

# Kinetic Origami

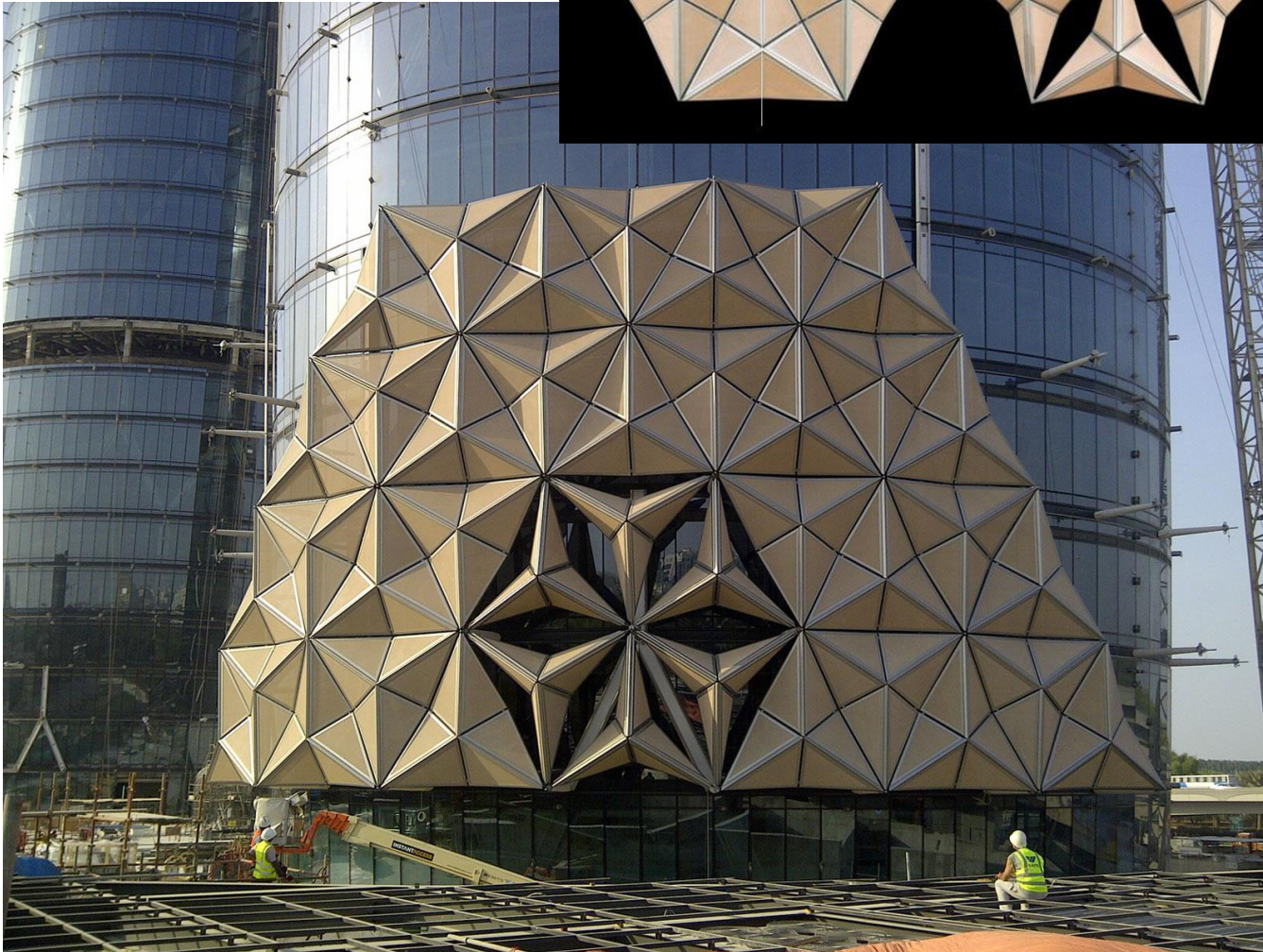
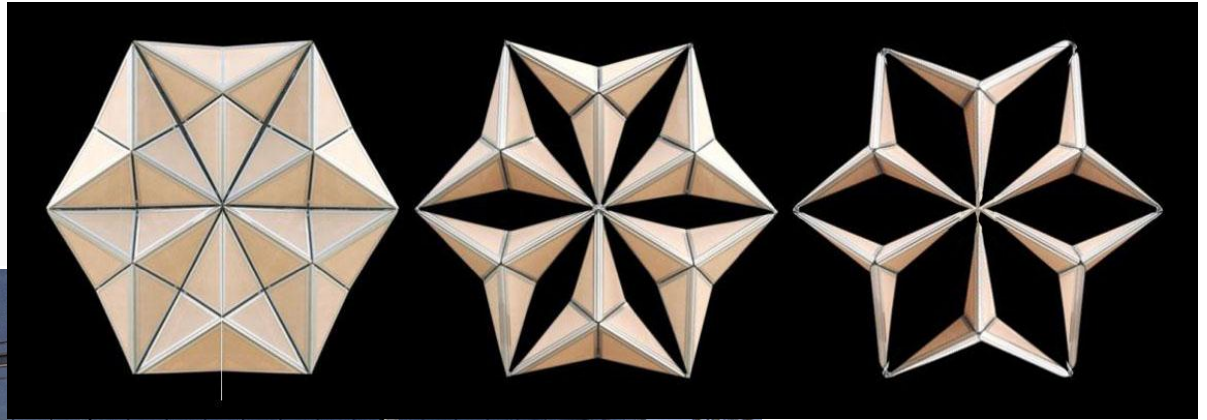


# Kinetic Origami



# Abu Dhabi Investment Council Headquarters

Architect: Aedas





*Custom Kinetic Facades:*

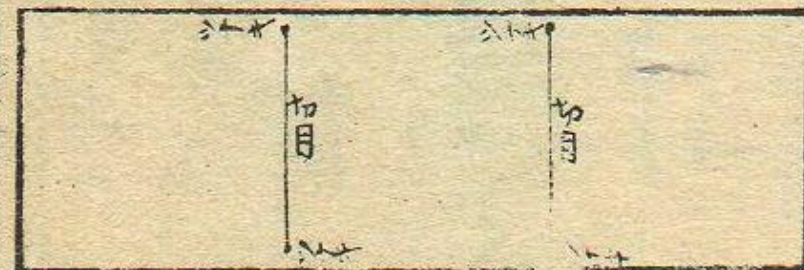
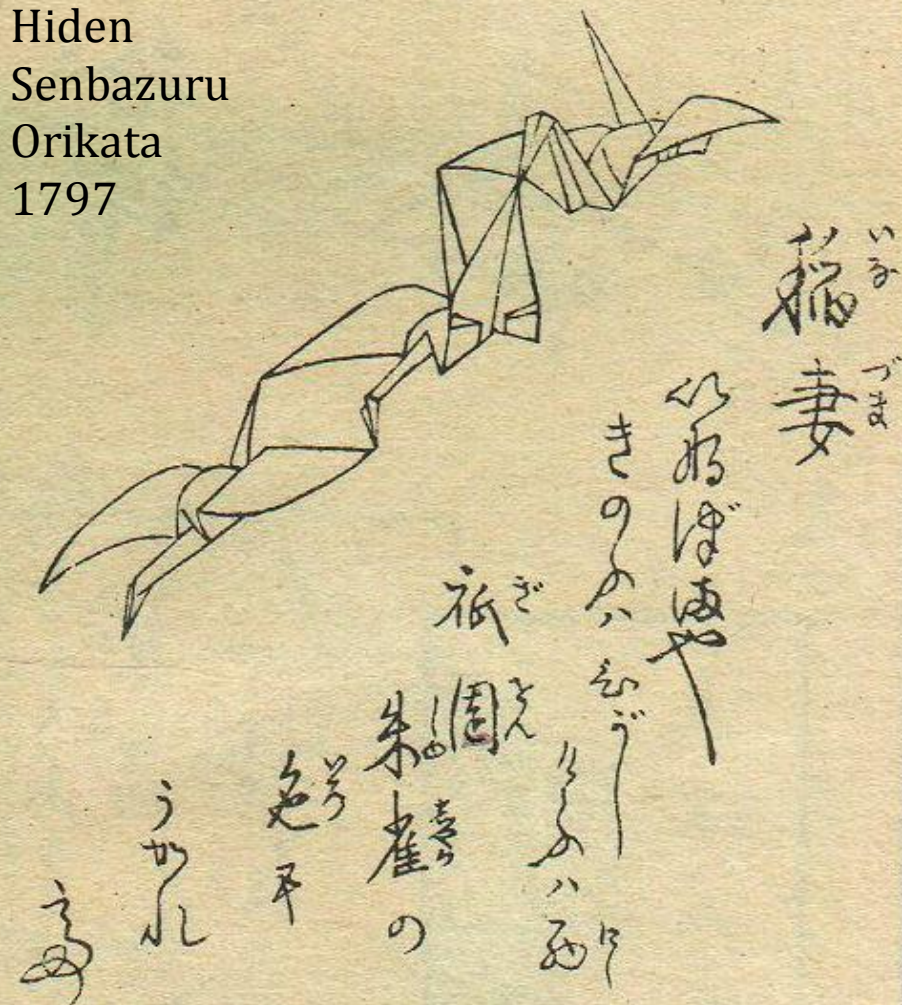
**Abu Dhabi Investment Council Headquarters**

**Architect: Aedas**





Hiden  
 Senbazuru  
 Orikata  
 1797





# Modern Origami



photo by Brian Chan



**Cerberus & Ryujin**

Satoshi Kamiya

2005



2006 Design Challenge  
Photos by Brian Chan



Andrea Hawksley



Brian Chan



Jason Ku



Giang Dinh



Robert Lang



# Origami USA Convention 2009



Joel Cooper

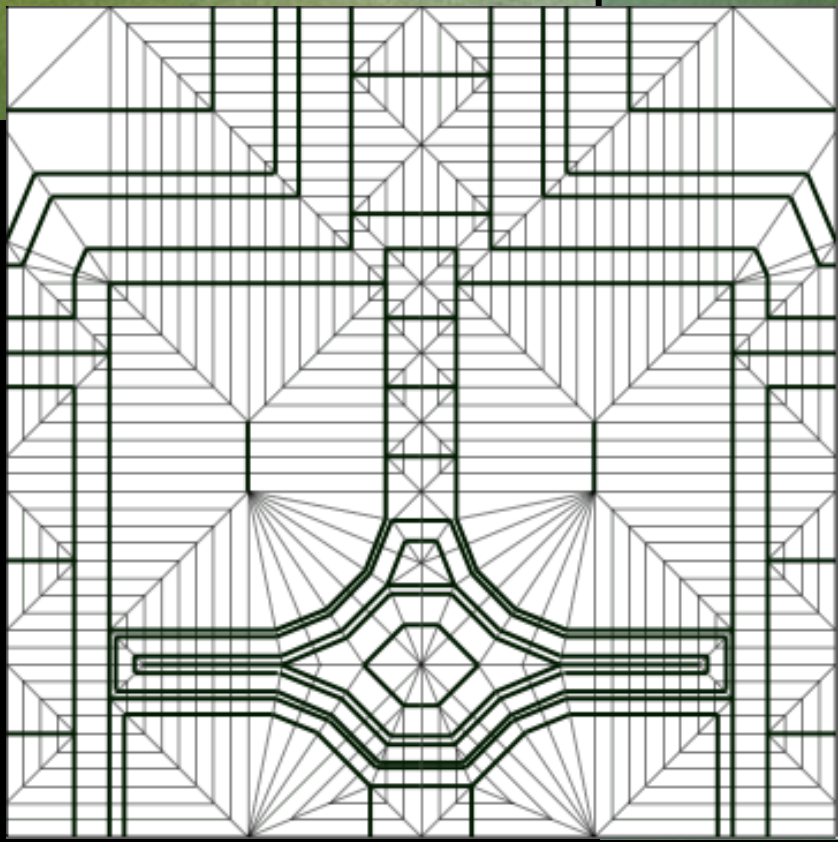


Brian Chan



Goran Konjevod





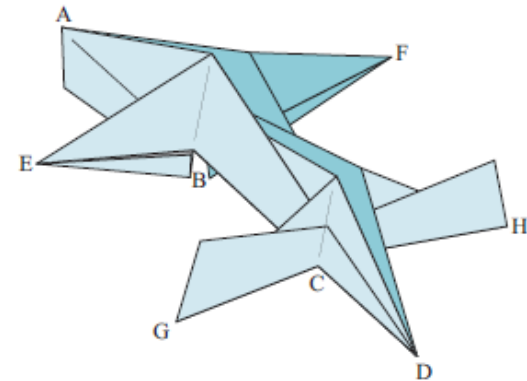
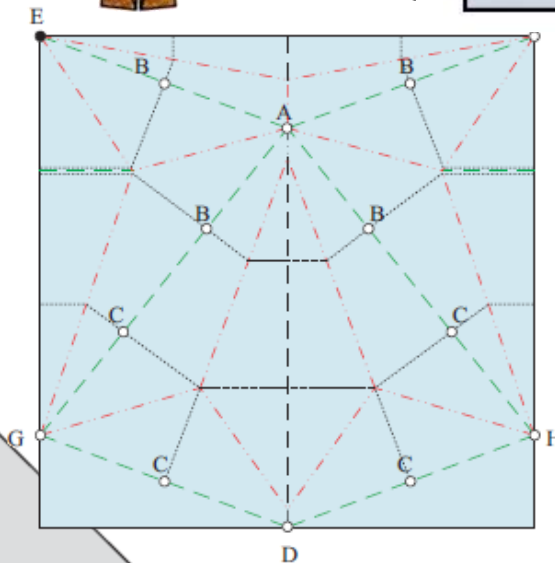
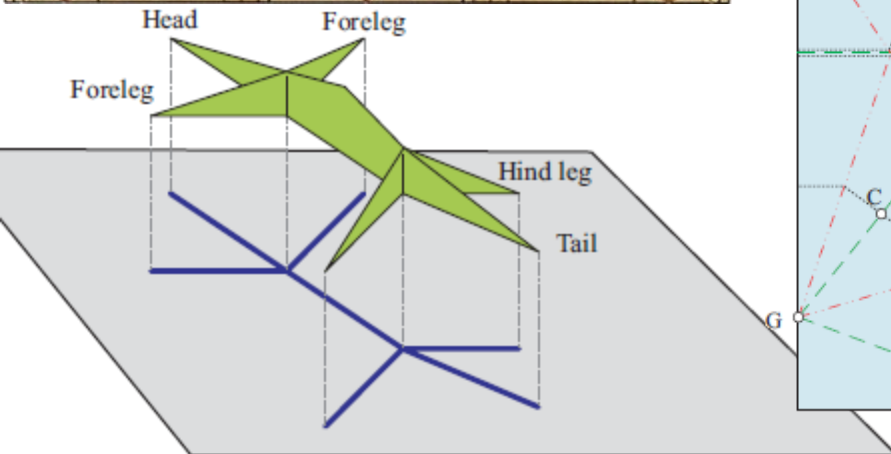
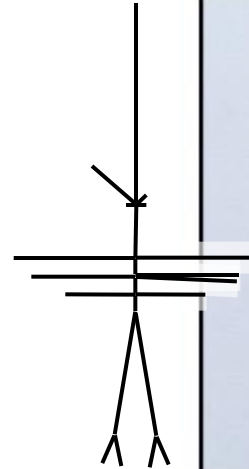
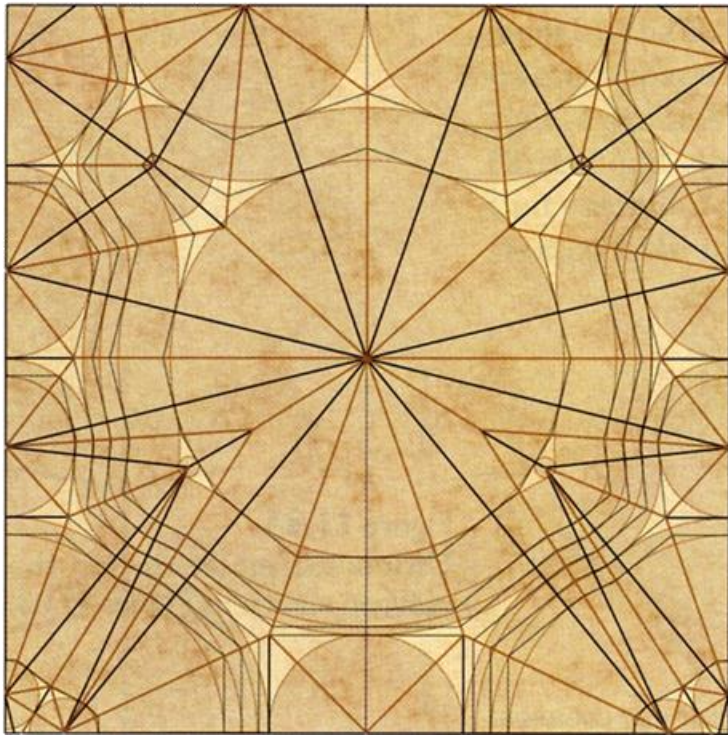
Butterfly 2.2

Jason Ku

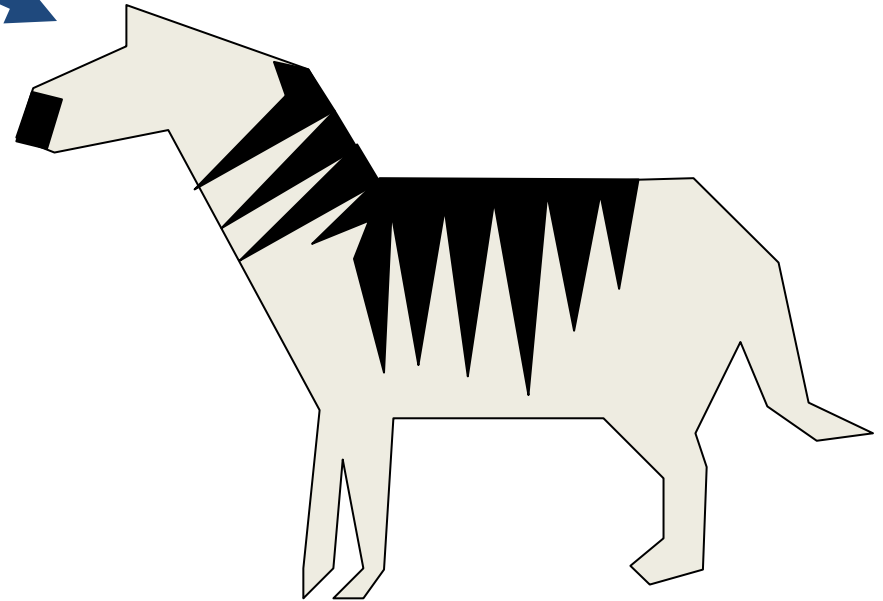
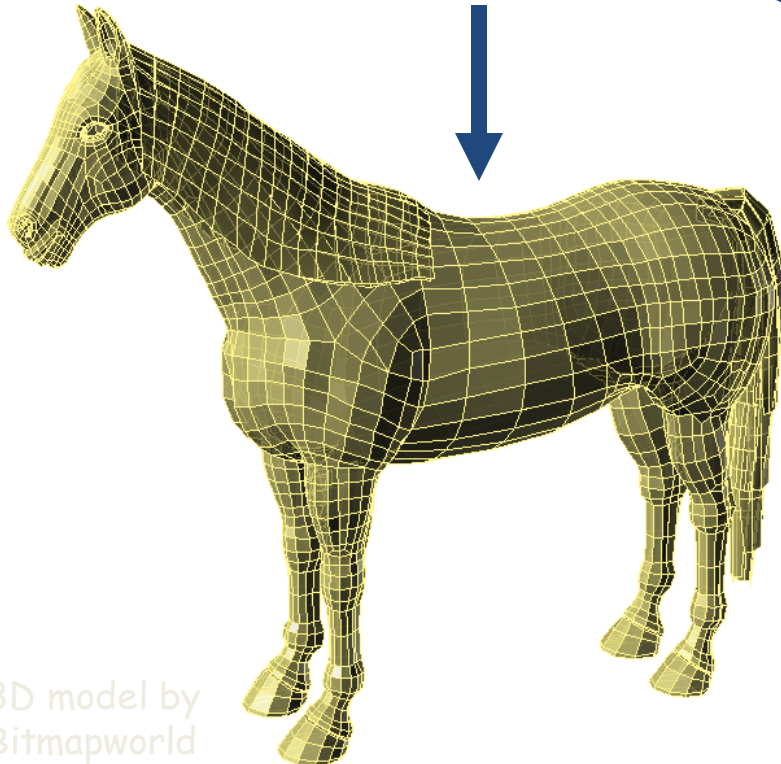
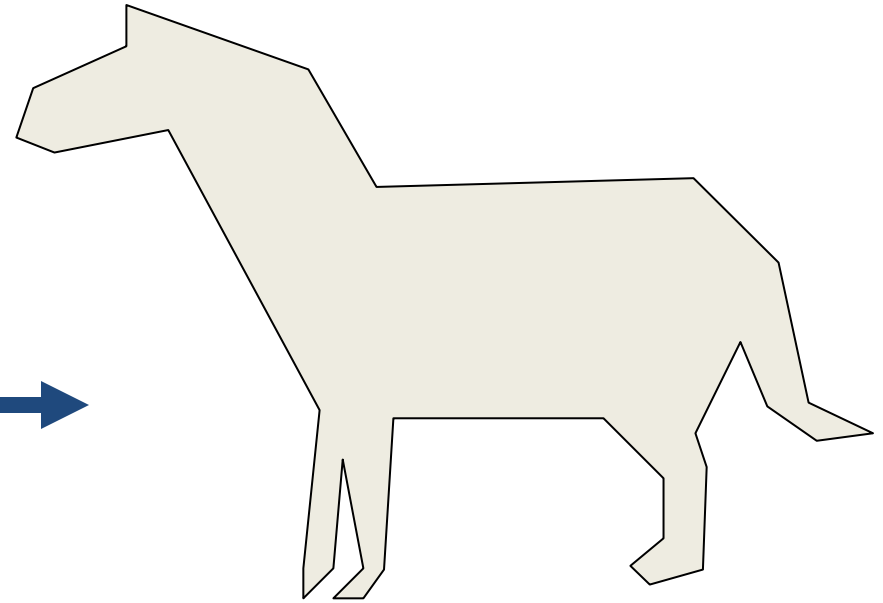
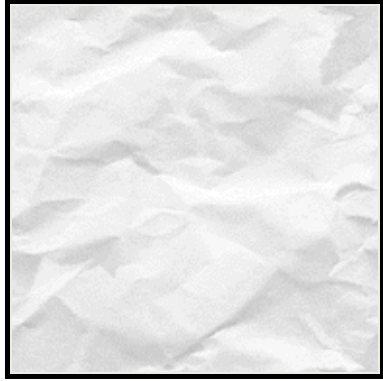
# Tree Method of Origami Design

[Fujimoto, Kamiya, Kawahata, Lang, Maekawa, Meguro, Yoshino]

[Lang, Demaine, Demaine 2006–2012]



# What Shapes Can Be Folded?

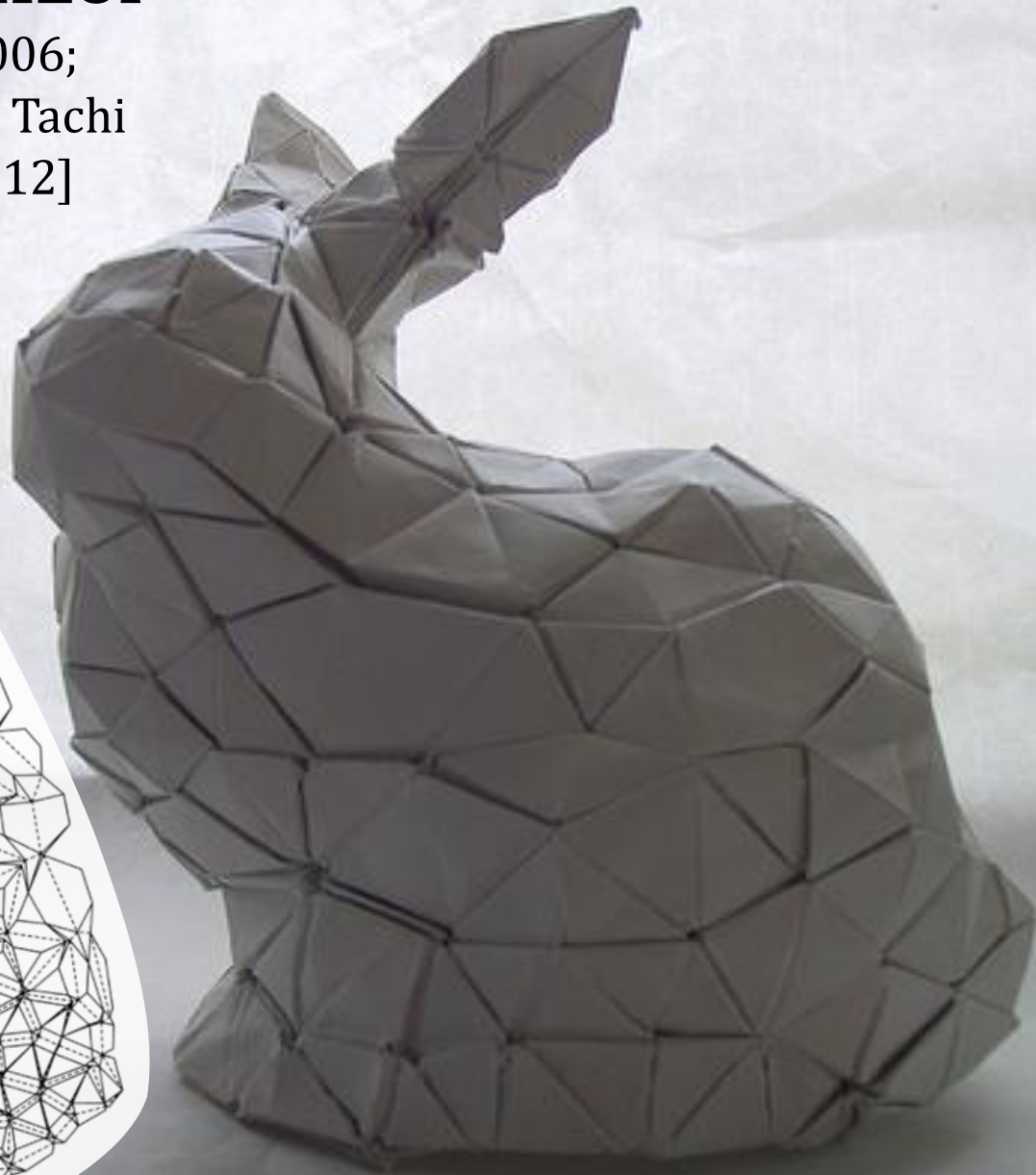
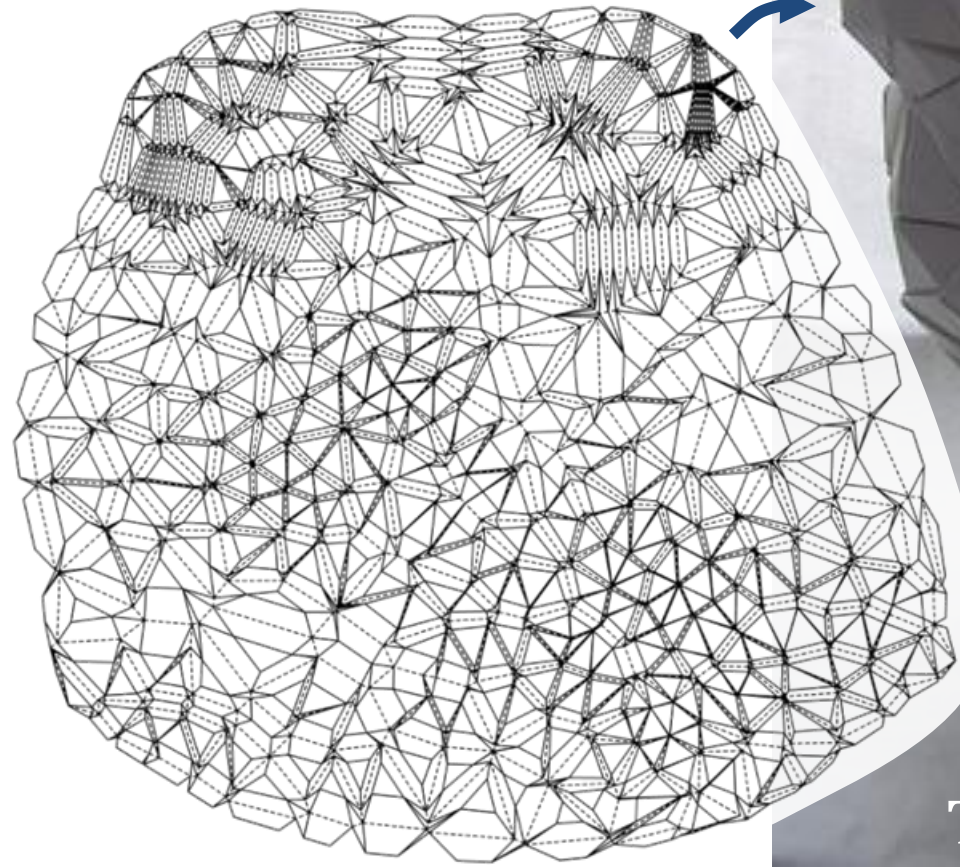


[Demaine, Demaine, Mitchell 1999]



# Origamizer

[Tachi 2006;  
Demaine & Tachi  
2009–2012]

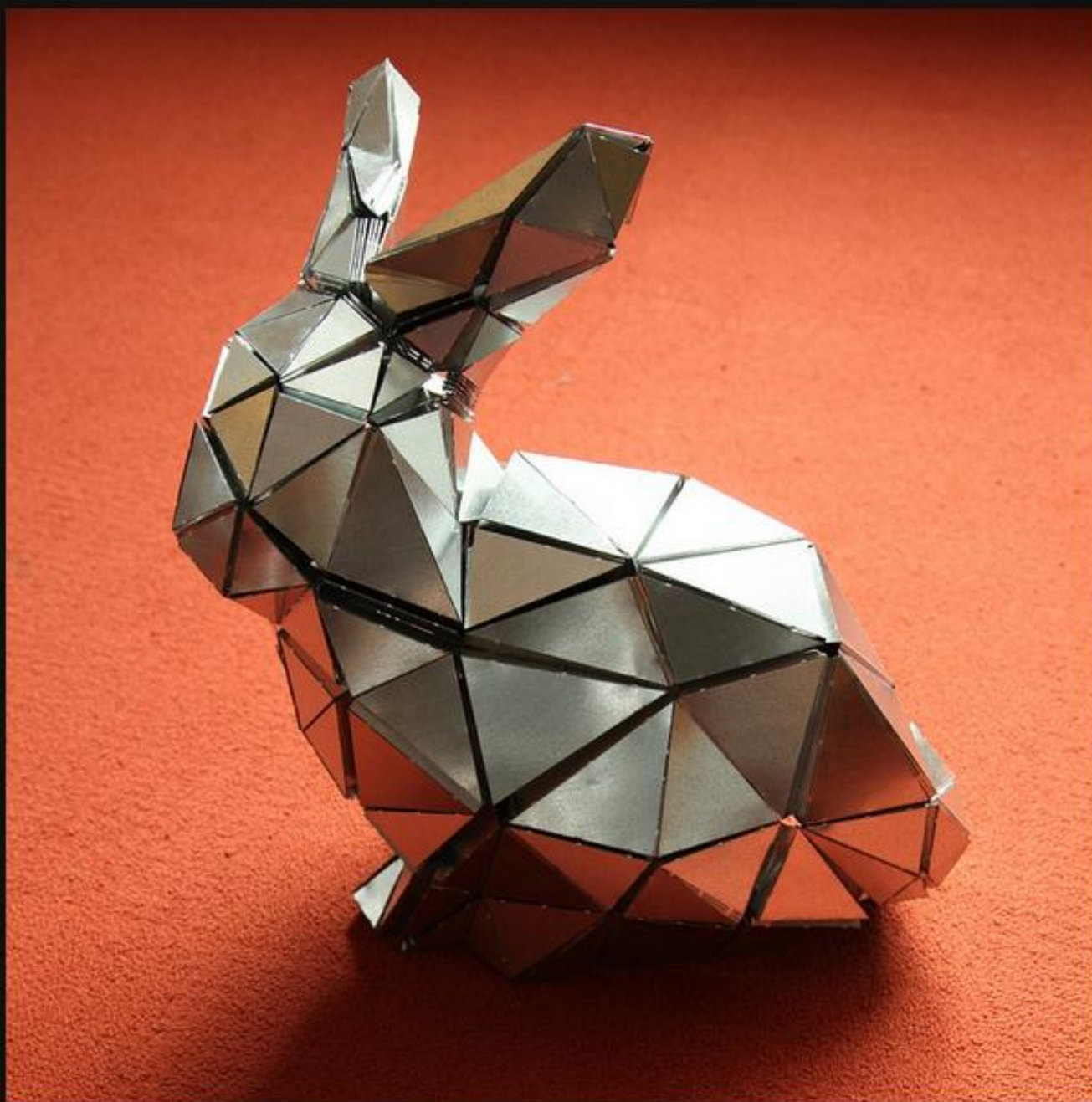


Tomohiro Tachi



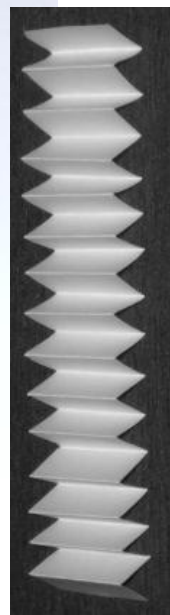
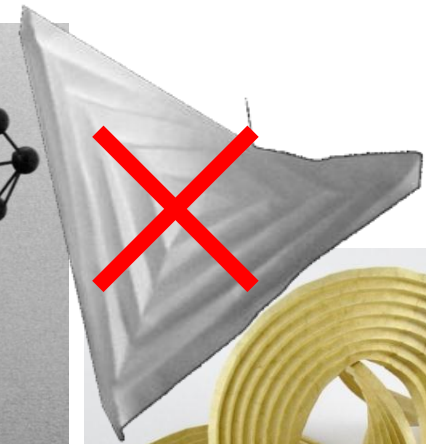
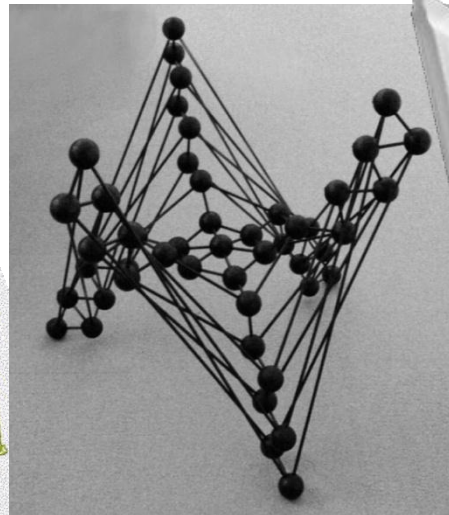
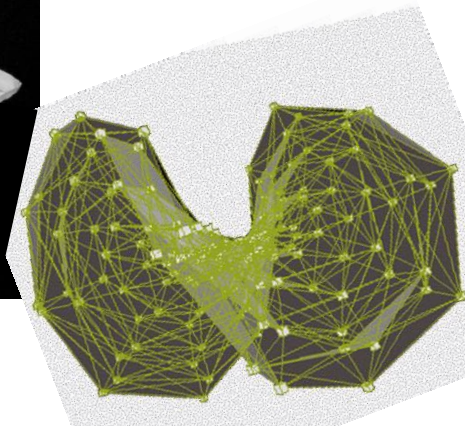
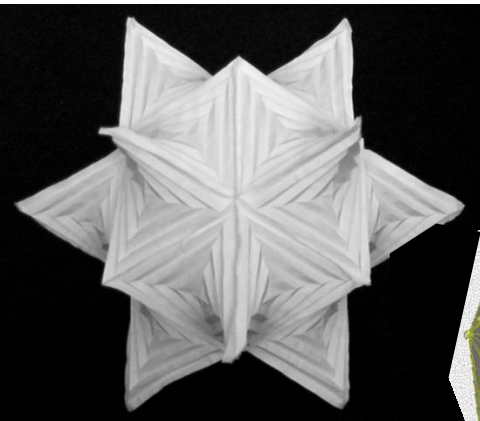
[Cheung, Demaine, Demaine, Tachi 2011]



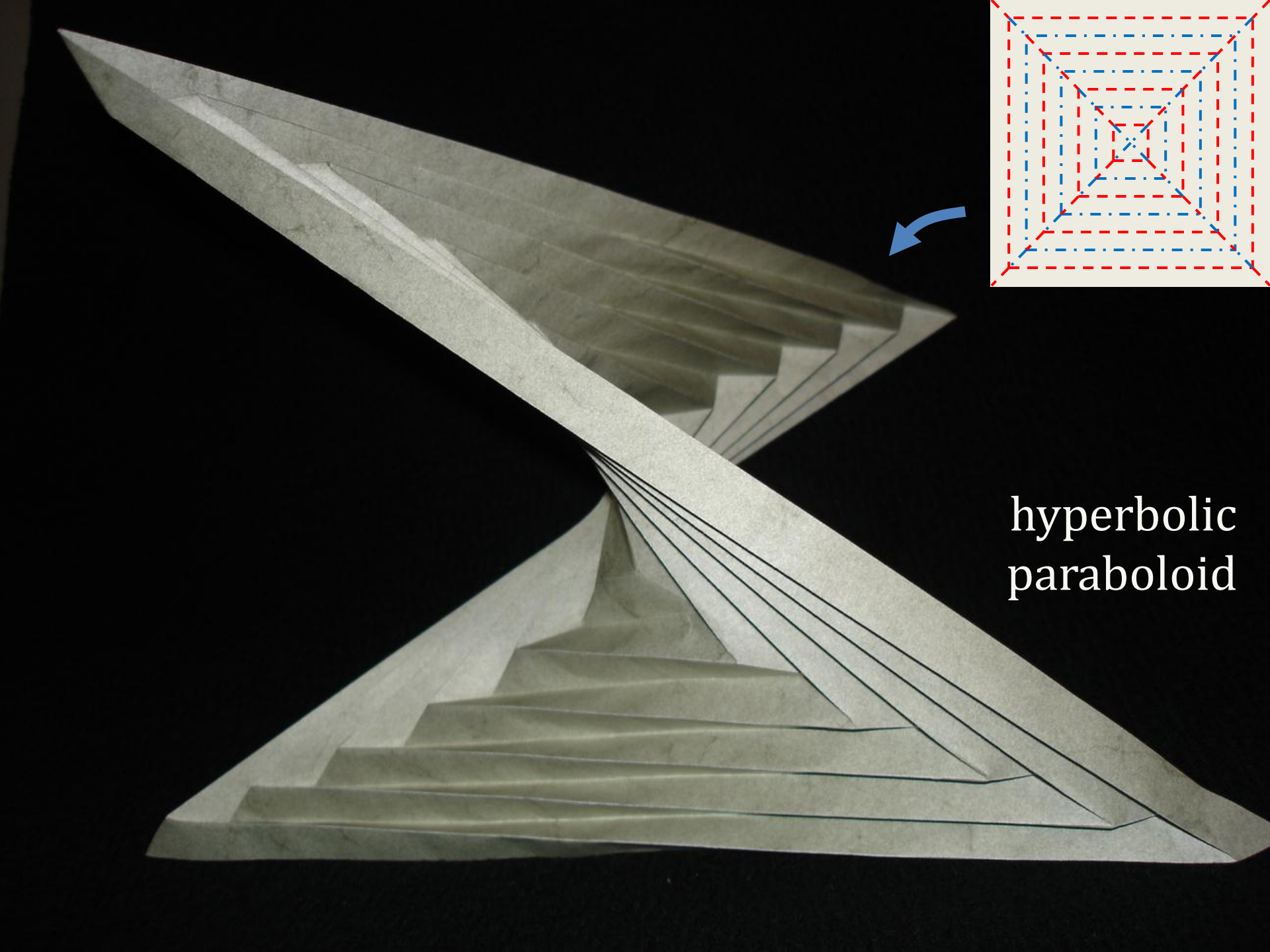


[Cheung, Demaine, Demaine, Tachi 2011]

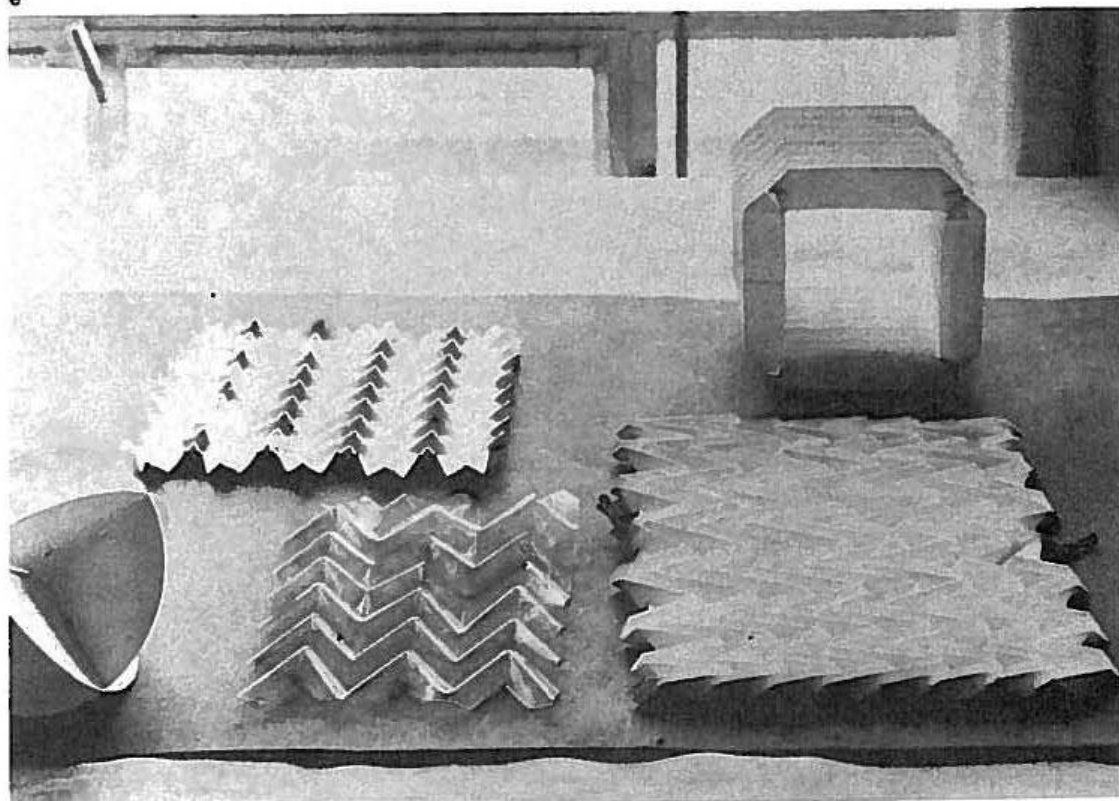
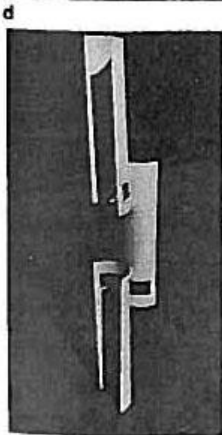
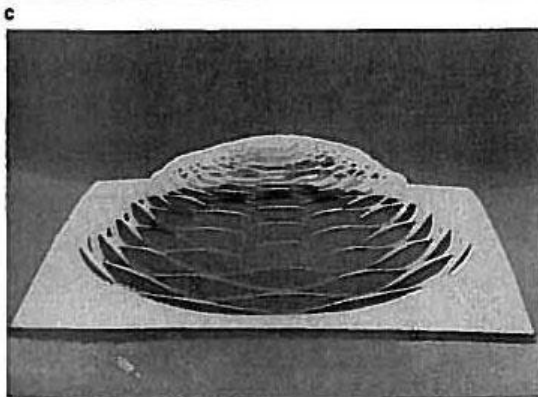
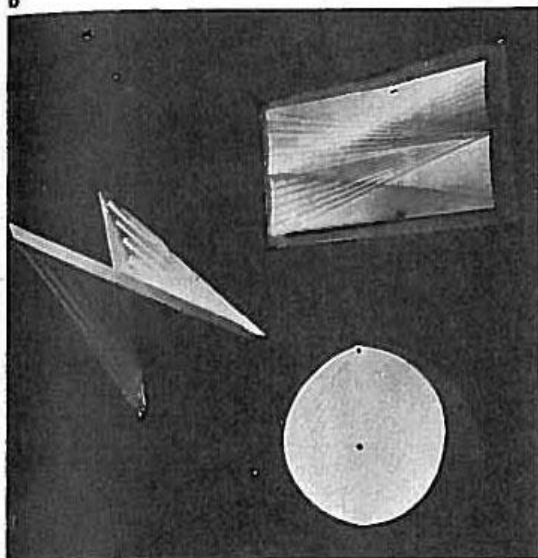
# Pleated Folding [1999-2013]







hyperbolic  
paraboloid



**b**  
Students in Albers's preliminary course: paper study, 1927–28. Foliate construction: a circular piece of paper was folded like a fan, from two opposite points of departure. This resulted in a shrinkage which altered the periphery (form) of the sheet.—Square sheet: here too the paper was folded fanlike from two opposite sides. The folds cross each other and result in a "snake" effect—one edge curves up, the other down.  
Wing form: automatic result of folding concentric squares.

**c**  
Students in Albers's preliminary course: paper study, 1927–28. The dome-shaped structure evolves from a flat sheet of paper by means of cuts which make extension into a dome shape possible.

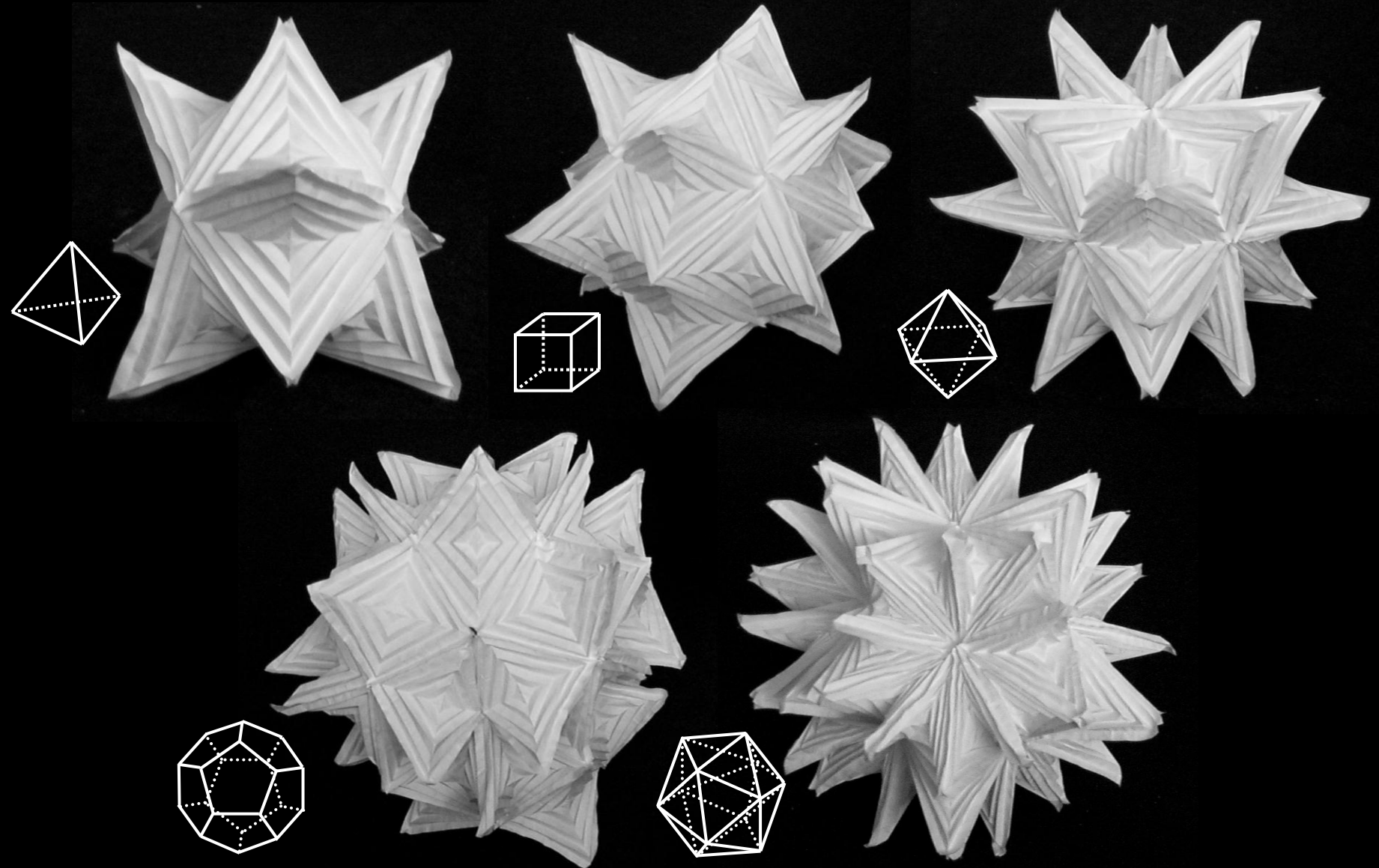
**d**  
Students in Albers's preliminary course: paper studies, 1927–28. Both exercises took advantages of a given material quality: the paper was rolled and tended to

remain rolled. The columnar form (left) resulted from cuts. The conic forms (right) derive automatically from cutting two concentric circles out of rolled paper.

**e**  
Students in Albers's preliminary course: studies with paper and acetate, 1927–28. Various zigzag folds—fundamental exercises. Two-dimensional shrinkage is one result of such folds in the case of flat structures. Two of these structures are made of paper; the transparent one in center foreground is made of acetate. Iridescent colors in the corners of the acetate structure indicate areas of especially high tension. The camera bellows (upper right) is the result of zigzag folds in a single direction. The corners were so rounded off that only a single overlap resulted; bevels were not permitted because otherwise the specific qualities of a camera bellows, light and air impermeability, would not be achieved. The task of constructing a camera bellows was assigned by Albers to every student; the student had to solve it entirely independently. No technical explanations were given.

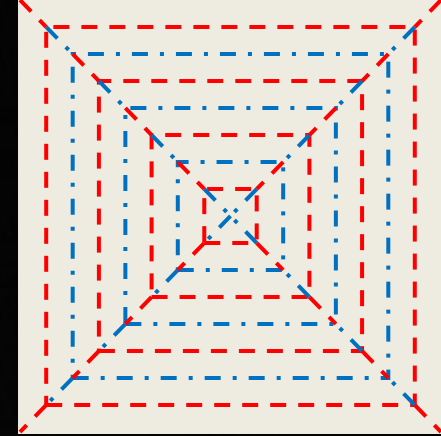
# Hyparhedra: Platonic Solids

[Demaine, Demaine, Lubiw 1999]





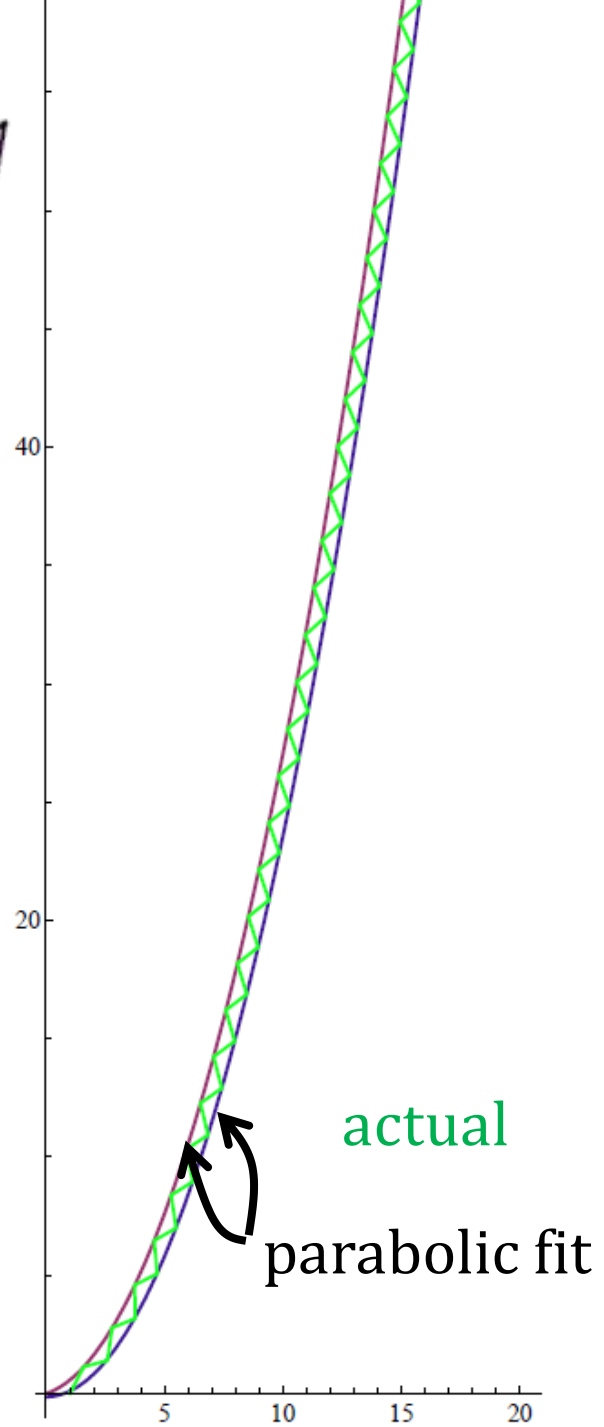
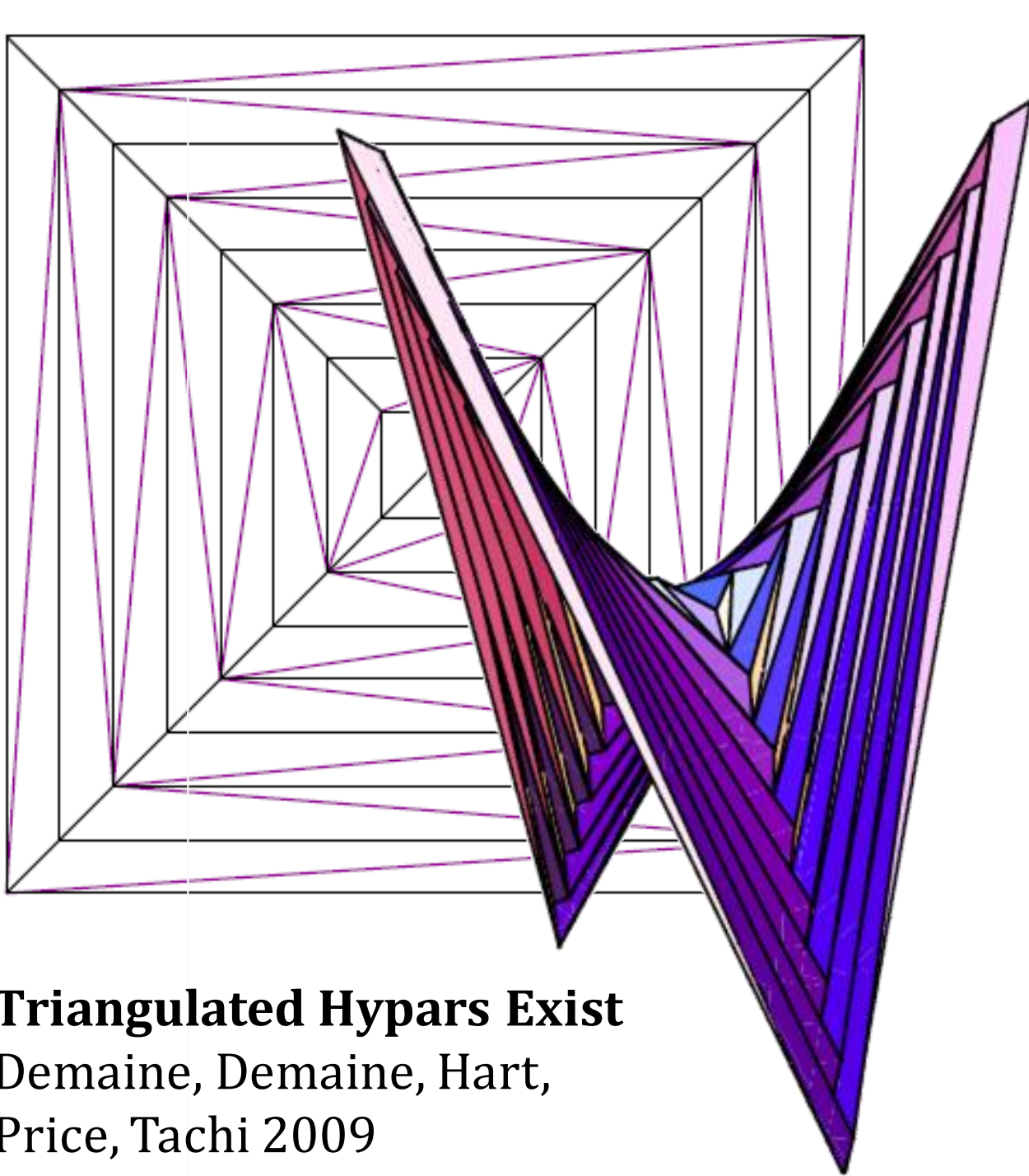
mathematically  
impossible!



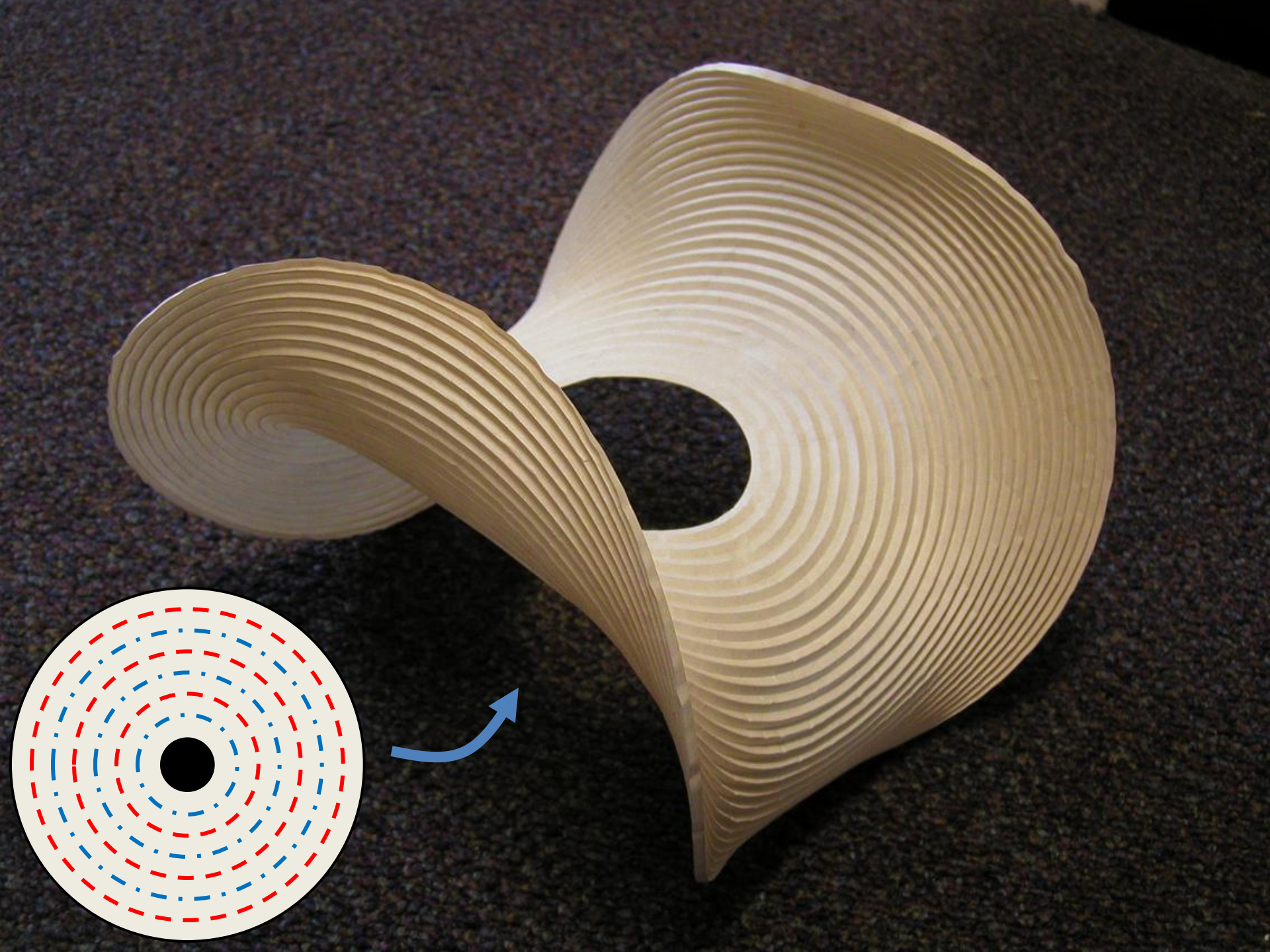
Demaine,  
Demaine,  
Hart, Price,  
Tachi 2009

hyperbolic  
paraboloid

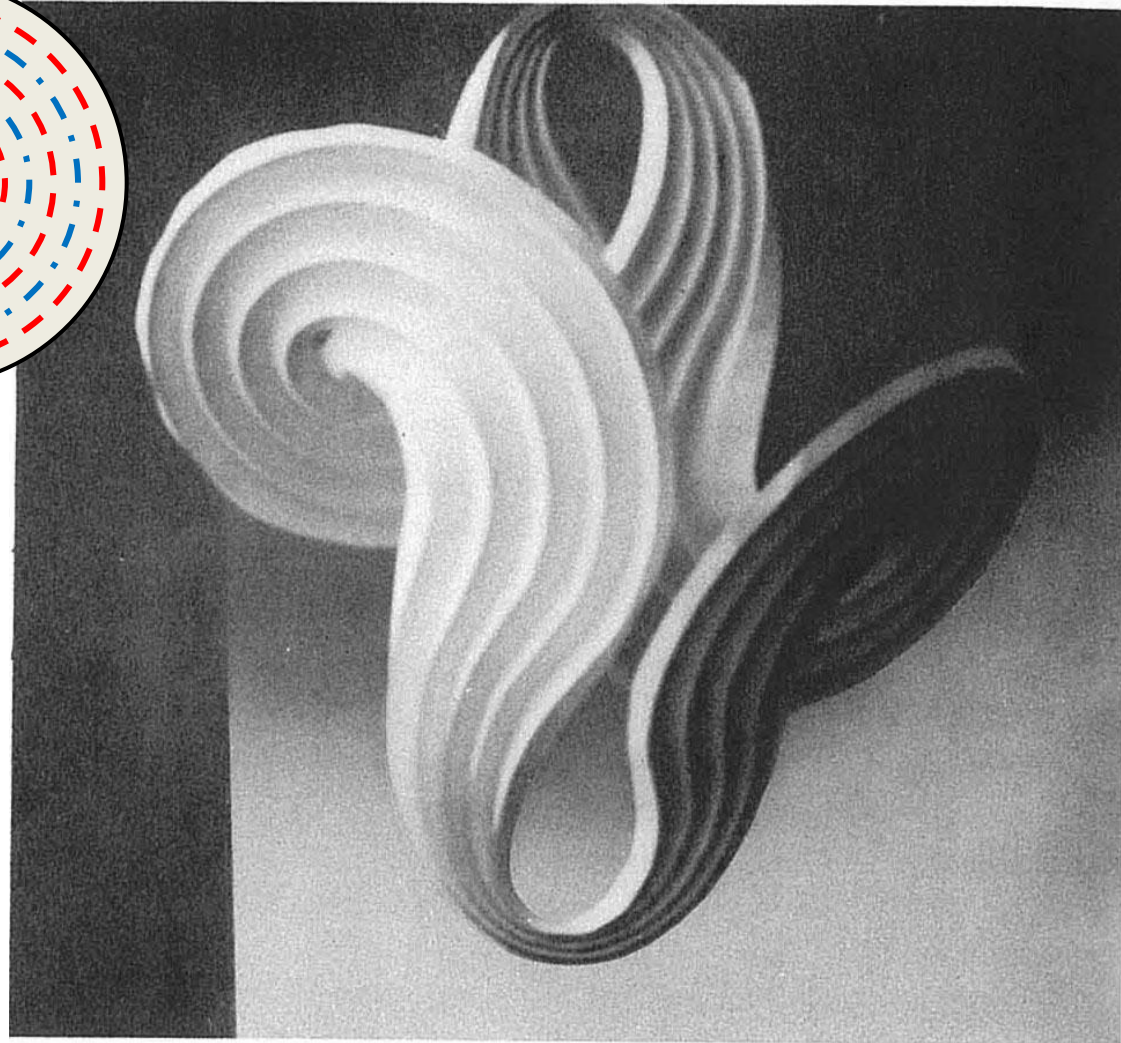
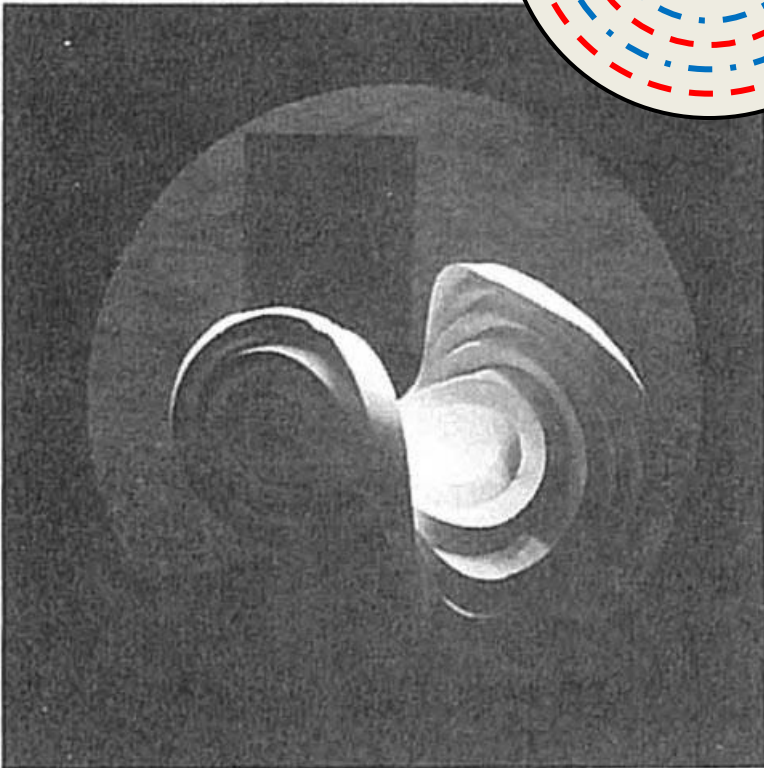
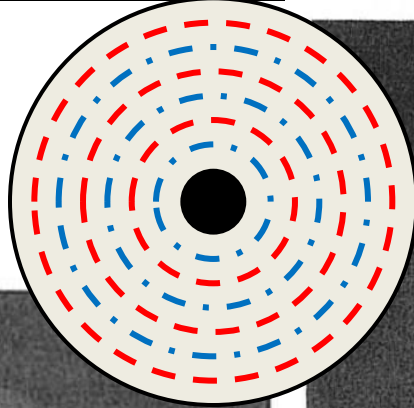




**Triangulated Hypars Exist**  
Demaine, Demaine, Hart,  
Price, Tachi 2009







a

Student in Albers's preliminary course: paper study. 1927–28. The shape results automatically; it is the result of back-and-forth folds in concentric circles. One special feature of this form is its mobility. The development of the curve form is of special pedagogic value, because it provides the student with unexpected revelations concerning the material and the construction principles.

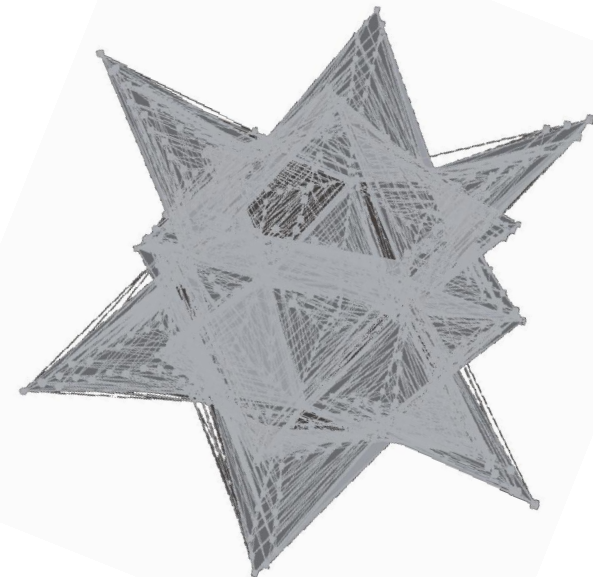
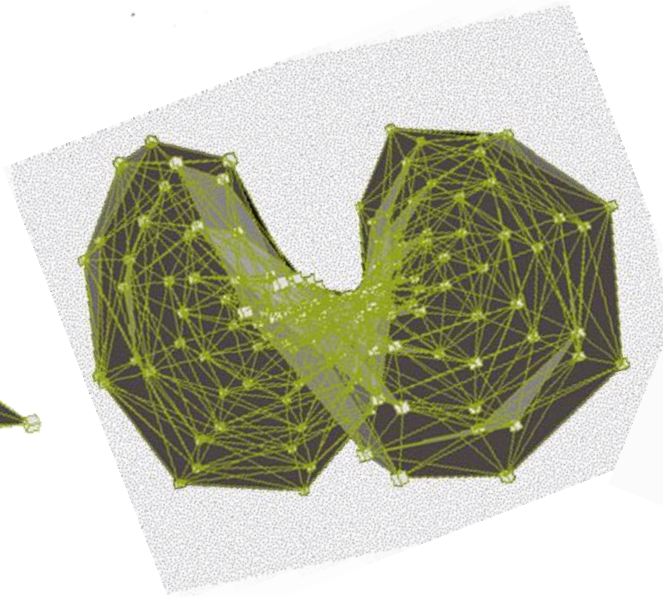
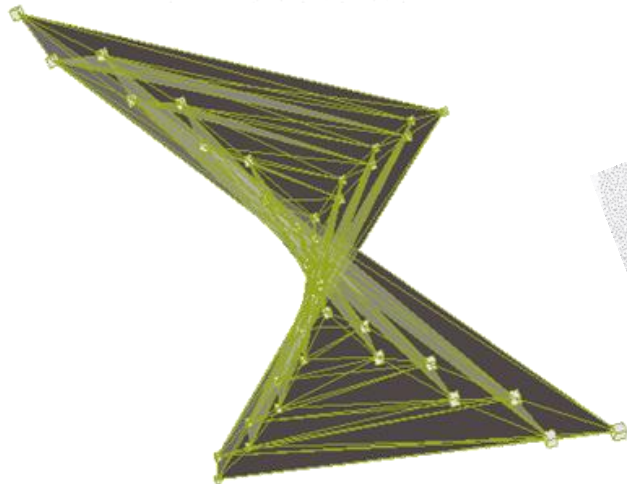
A paper sculpture abstraction by Irene Shawinsky. Photo from the Museum of Modern Art. This piece, over a yard wide, was made by cutting a “doughnut” from a very large sheet of white paper, scoring it in concentric lines, accordion-pleating it, and hanging it from wires so that it would take these convolutions of its own weight.





# Virtual Origami

[Demaine, Demaine, Fazel, Ochsendorf 2006]



< 6 sides  
< 15 folds  
< 30 scale

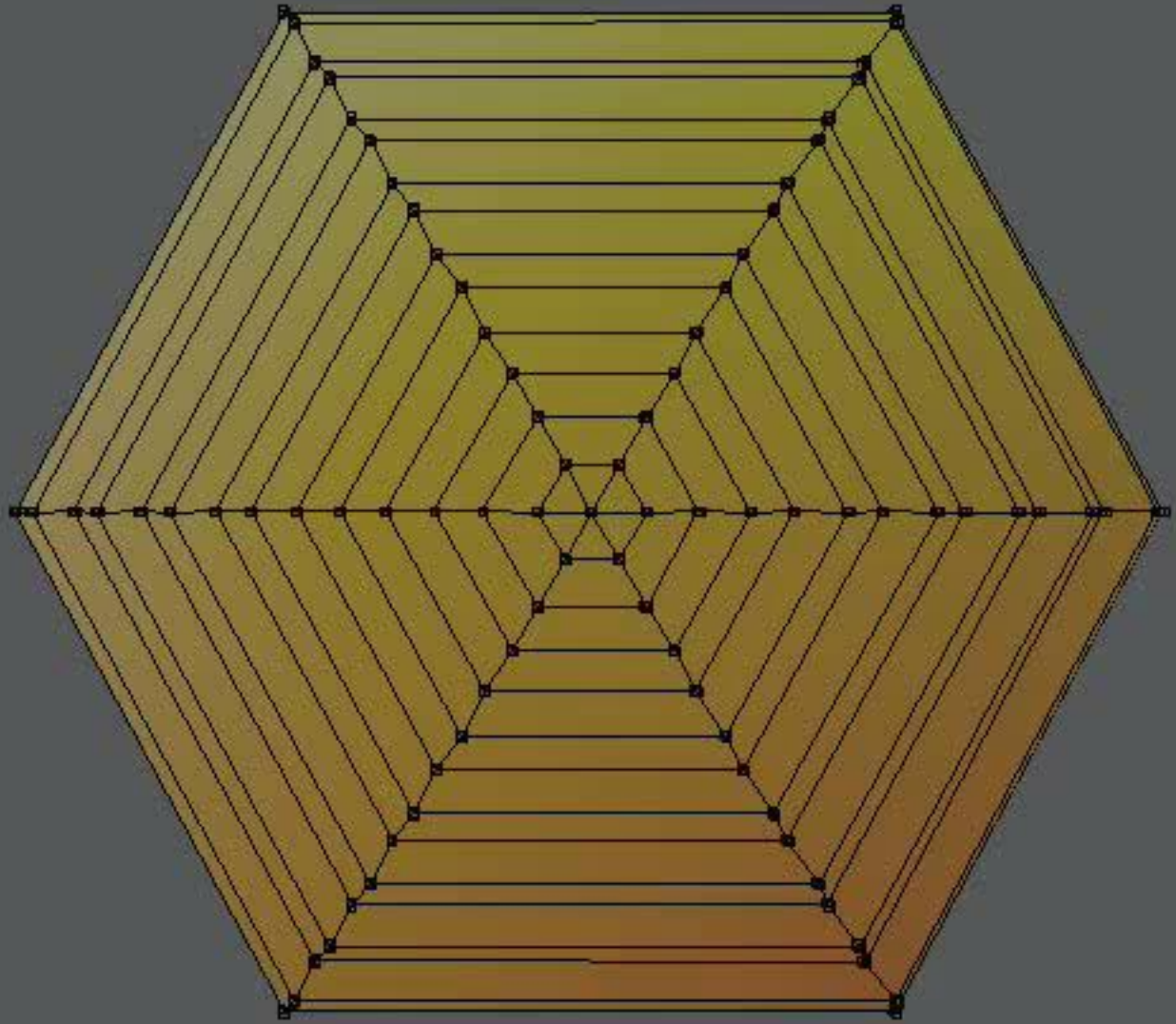
piece

solid

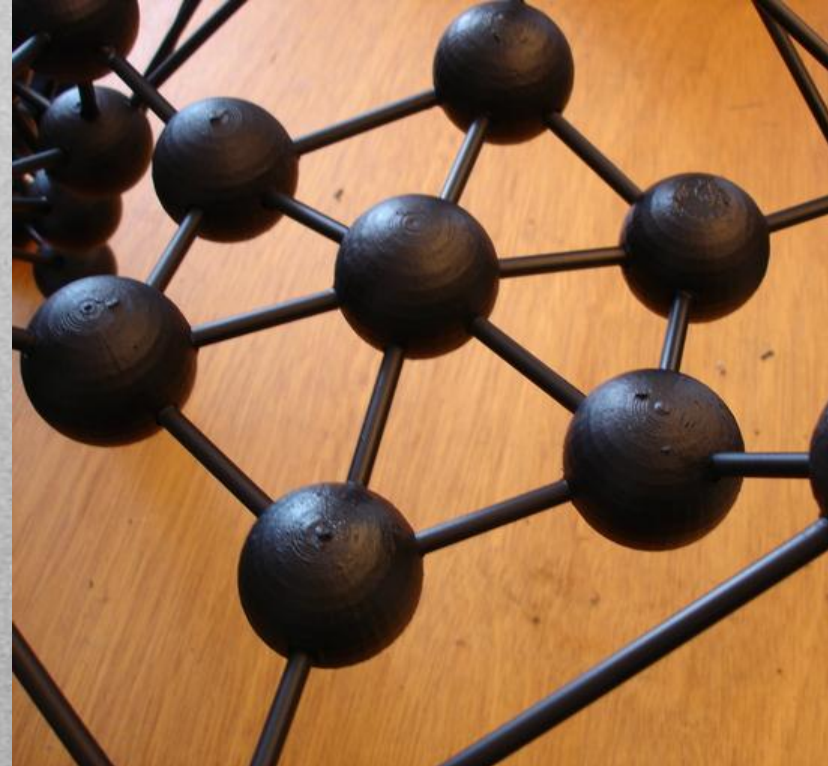
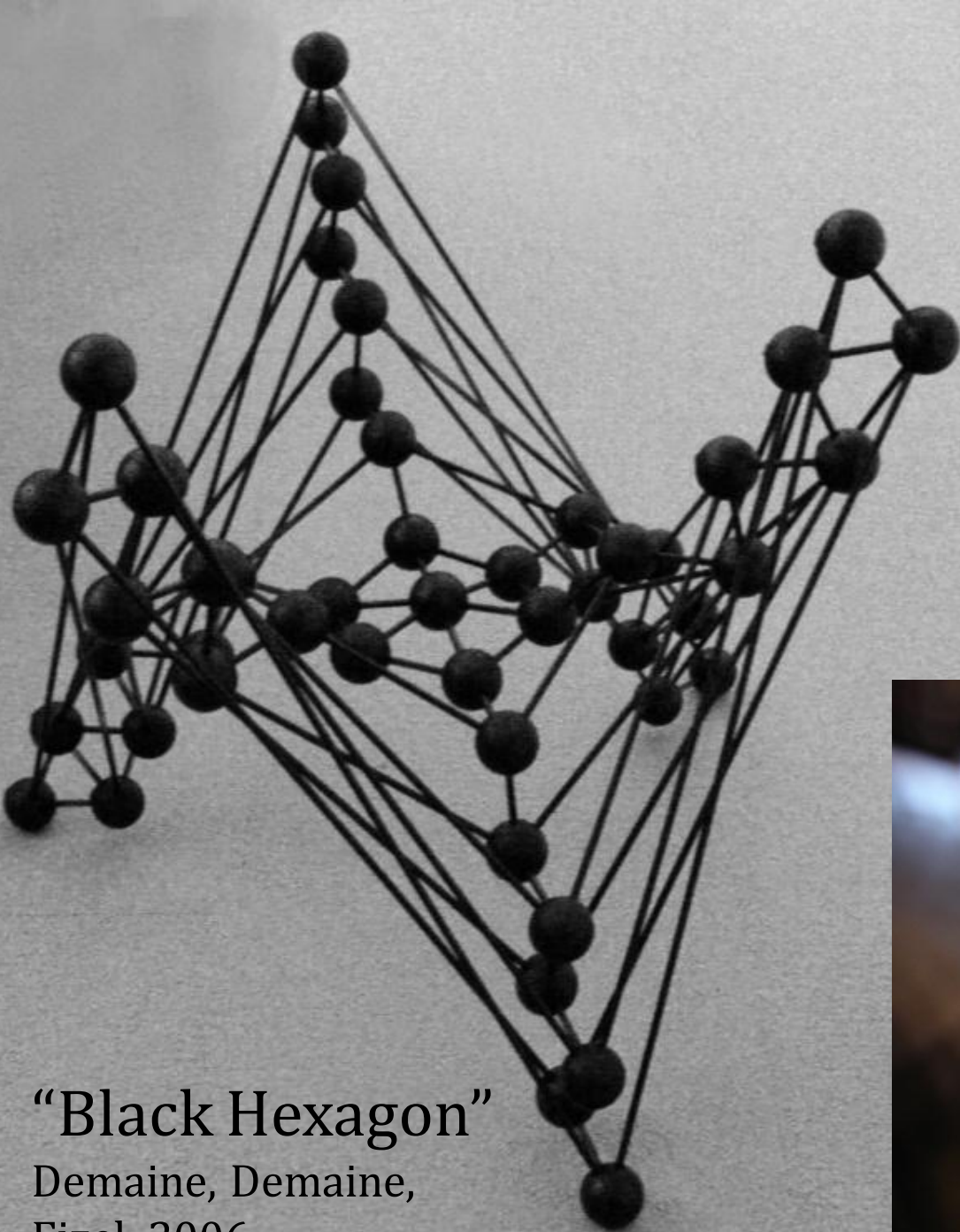
free-form

tools

view







# “Black Hexagon”

Demaine, Demaine,  
Fizel 2006



“Computational Origami”  
Erik & Martin Demaine  
MoMA, 2013–2014

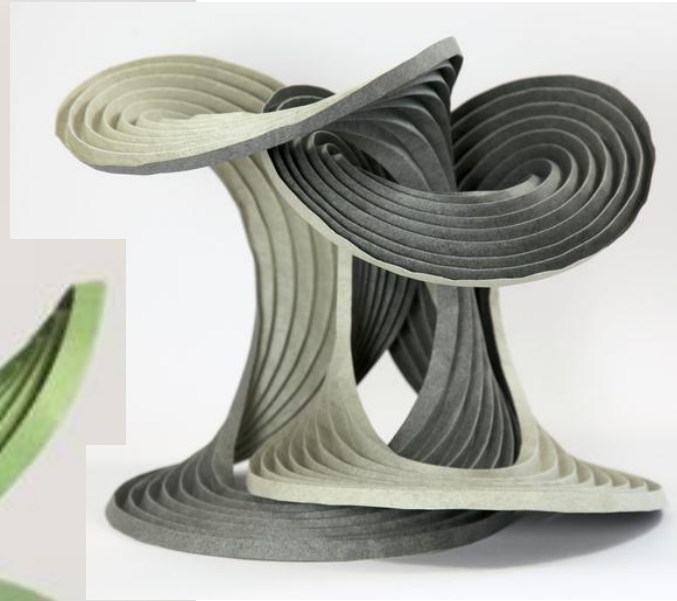
Elephant hide paper  
~9"x15"x7"



# Curved Crease Sculpture

Erik & Martin Demaine

Renwick Gallery,  
Smithsonian  
American Art  
Museum, 2012





Feb.–Apr., 2012

Brockton, Mass.



fullerCRAFT  
museum™



Demaine &  
Demaine  
2011



Guided By Invoices  
Chelsea, New York  
Jan.–Mar., 2012



**Earthtone Series**  
Demaine & Demaine  
2012

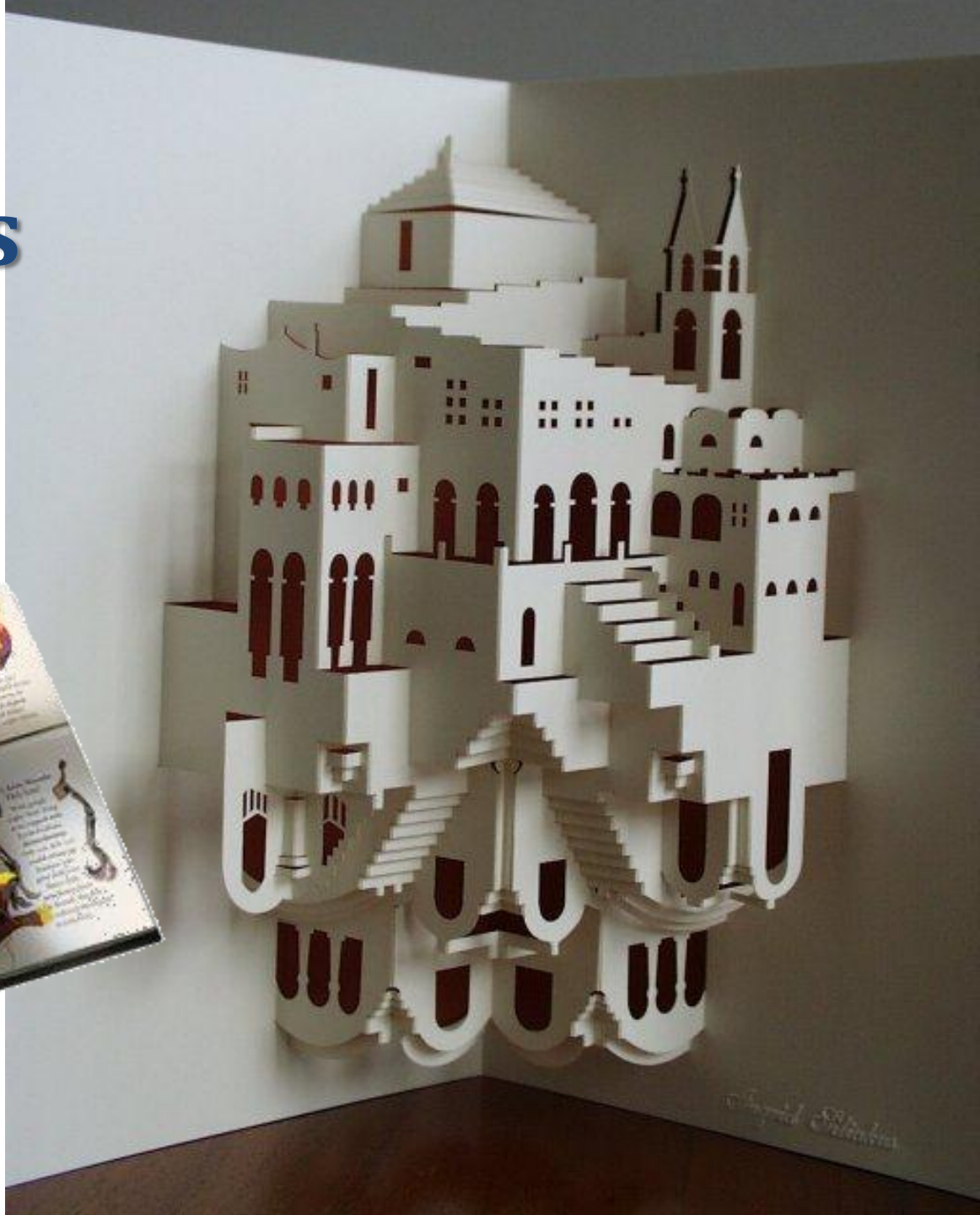


Simons Gallery  
Stony Brook, NY  
July–Aug., 2012



**Ocean Series**  
Demaine &  
Demaine, 2012

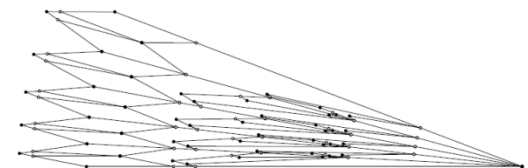
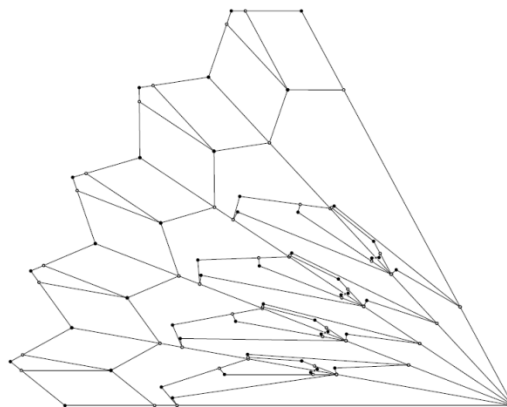
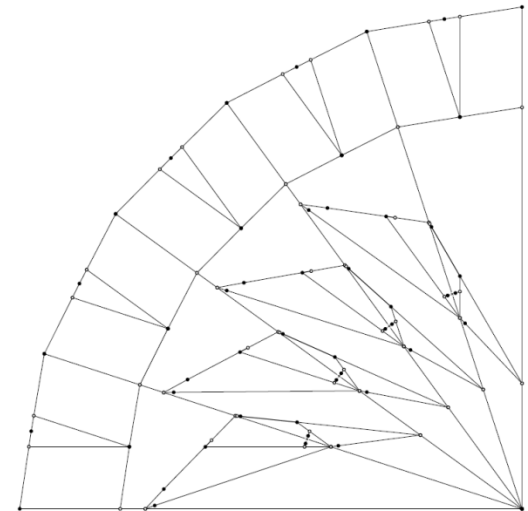
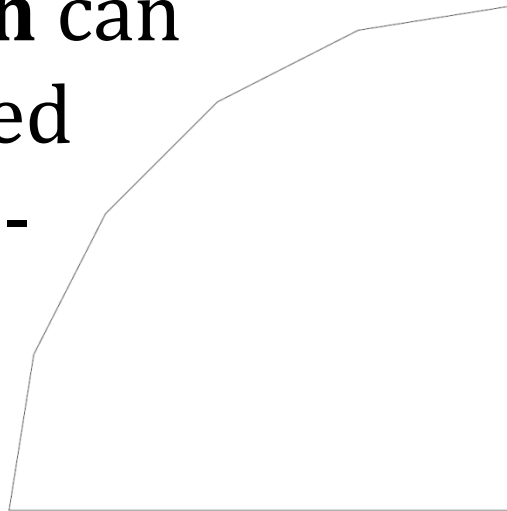
# Popup Books/Cards





# Popups [Abel, Demaine, Demaine, Eisenstat, Lubiw, Schulz, Souvaine, Viglietta, Winslow 2013]

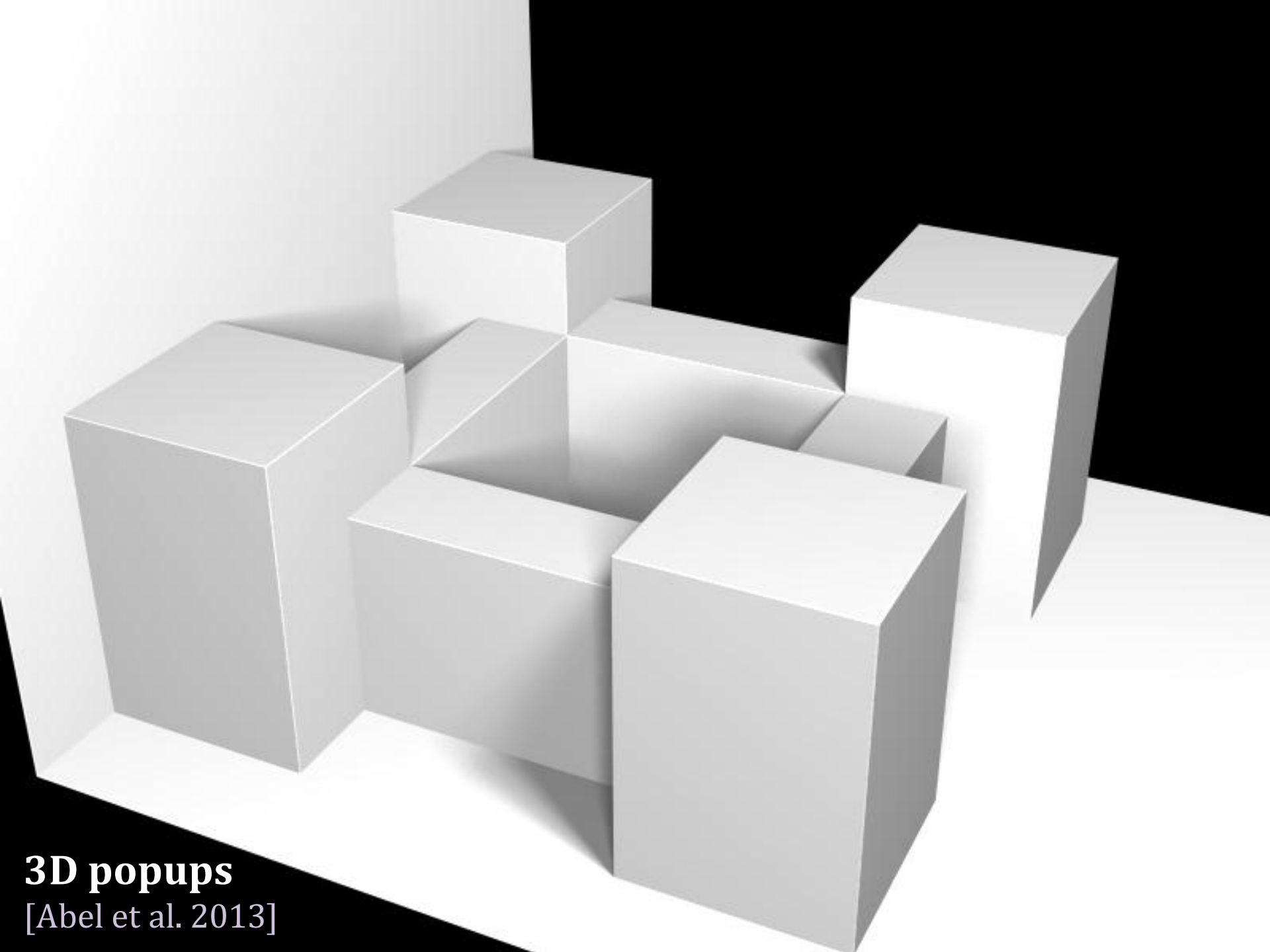
- Any **polygon** can be subdivided into a single-degree-of-freedom popup, with specified target angle



# Popups [Abel, Demaine, Demaine, Eisenstat, Lubiw, Schulz, Souvaine, Viglietta, Winslow 2013]

- Any **polygon** can be subdivided into a single-degree-of-freedom popup, with specified target angle





**3D popups**

[Abel et al. 2013]



Hydro-Fold [Christophe Guberan 2012]



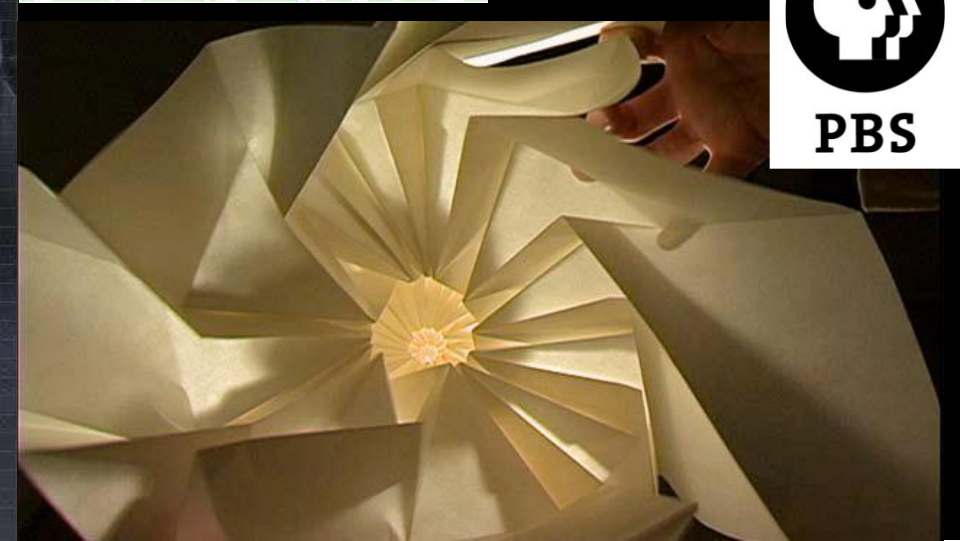
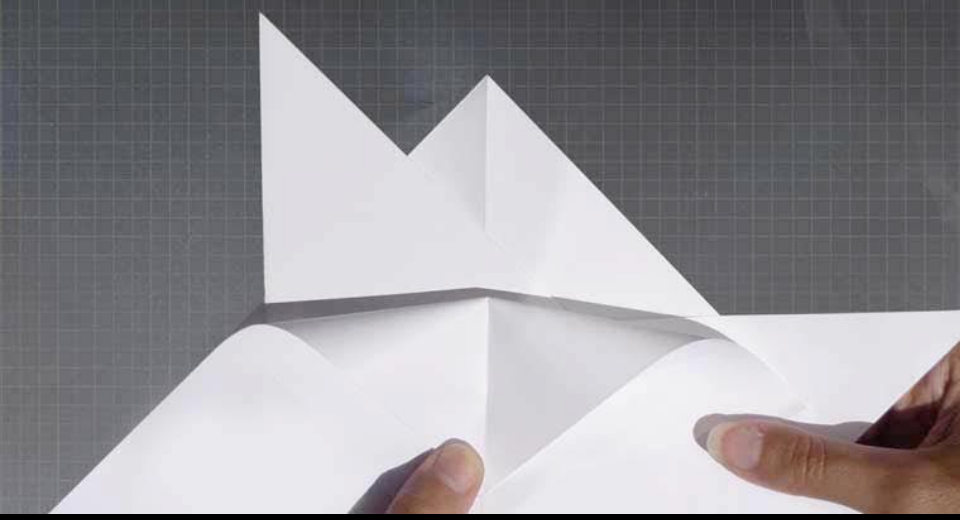
[i]NDEPENDENT LENS



THE SCIENCE  
**OF ART.**  
THE ART  
**OF SCIENCE.**

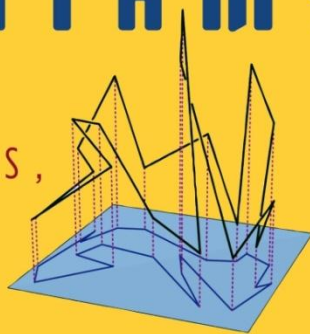
B E T W E E N  
T H E **FOLDS**

A NEW DOCUMENTARY FROM GREEN FUSE FILMS

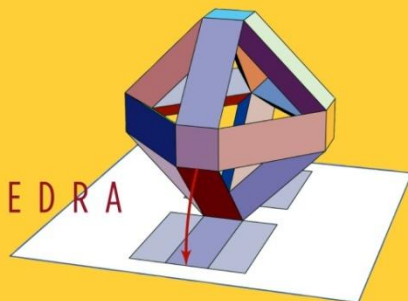


# Geometric Folding Algorithms

LINKAGES,



ORIGAMI,



& POLYHEDRA

ERIK D. DEMAINE & JOSEPH O'ROURKE

# 幾何的な Geometric FOLDING ALGORITHMS 折りアルゴリズム

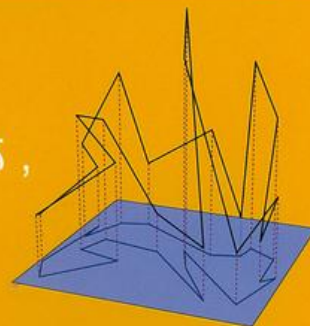
リンケージ, 折り紙, 多面体

エリック・D・ドメイン & ジョセフ・オルーク 著

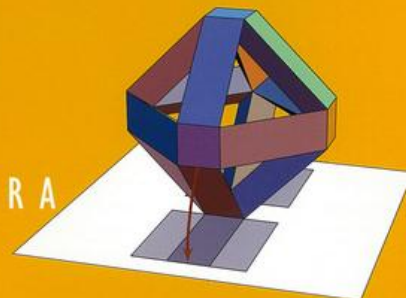
ERIK D. DEMAINE & JOSEPH O'ROURKE

上原隆平 訳

LINKAGES,



ORIGAMI,



POLYHEDRA

近代科学社



## 6.849: Geometric Folding Algorithms: Linkages, Origami, Polyhedra (Fall 2010)

Prof. [Erik Demaine](#)

[\[Home\]](#) [\[Problem Sets\]](#) [\[Project\]](#) [\[Lectures\]](#) [\[Problem Session Notes\]](#)

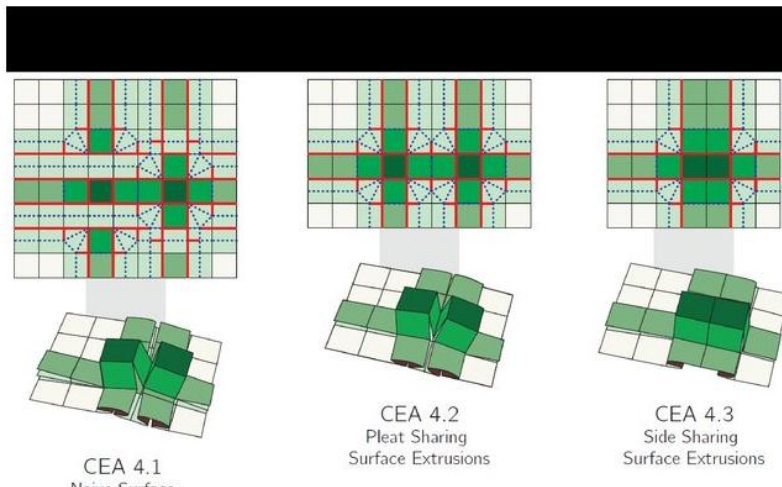
### Lecture 5 Video [\[previous\]](#)

[\[+\]](#) **Universal hinge patterns:** box pleating, polycubes; orthogonal maze folding. **NP-hardness:** introduction, reductions; simple foldability; crease pattern flat foldability; disk packing (for tree method).



Download Video: [360p](#)

Slides, page 5/20 • [\[previous page\]](#) • [\[next page\]](#) • [\[PDF\]](#)



## Free Video Lectures!

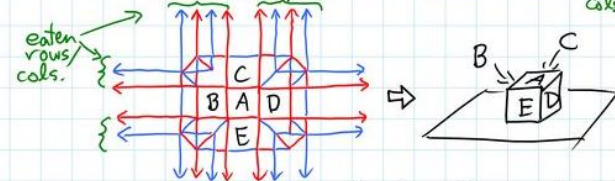
Handwritten notes, page 1/7 • [\[previous page\]](#) • [\[next page\]](#) • [\[PDF\]](#)

6.849 Lecture 5 Sept. 22, 2010

Universal hinge patterns: (for origami transformers)

*[Benbernou, Demaine, Demaine, O'Radya 2010]*

- suppose crease pattern required, to be subset of fixed "hinge pattern" (e.g. Origamizer uses completely different creases for every model)
- $n \times n$  box-pleat pattern can make any polycube of  $O(n)$  cubes, seamless:
  - cube gadget turns  $O(1)$  rows & columns into a cube sticking out of sheet ~ even if bumps elsewhere (not in eaten rows/cols.)



- to make a tree of cubes: (= any polycube)
  - make a leaf
  - conceptually remove it } "postorder traversal"
  - repeat
- actually need to reserve space ahead of time for all the cube gadgets

Handwritten notes, page 1/7 • [\[previous page\]](#) • [\[next page\]](#) • [\[PDF\]](#)