

MIT Class 6.S080 (AUS)

Mechanical Invention through Computation

Expanding Structures – 2D

Hardware / Construction Terms

- Slip fit
- Press fit
- Knurl
- Tolerances
- Bearing
- Bushing
- Radial and pivotal forces
- Clearances
- Chamfers
- Sliding friction
- Rolling friction

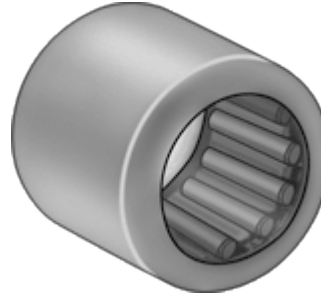
Bearing types



Ball bearing
(sealed)



Ball bearing
(unsealed)



Needle bearing



Spherical
bearing



Sleeve bearing
(bushing)

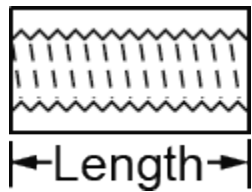
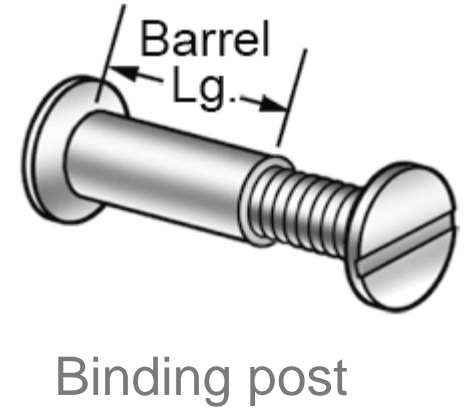
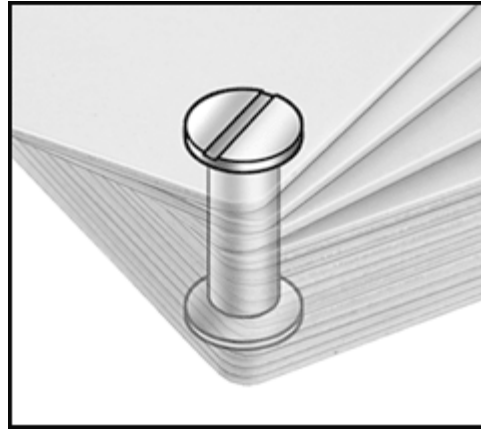
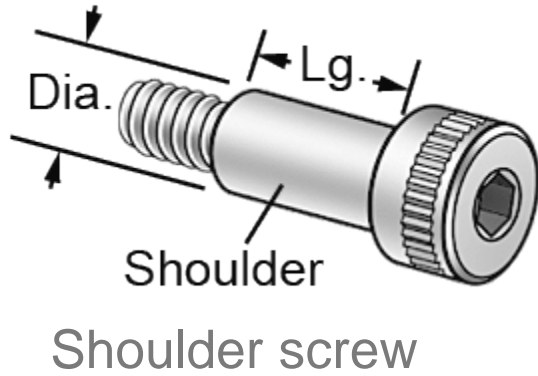


Flanged Sleeve
bearing

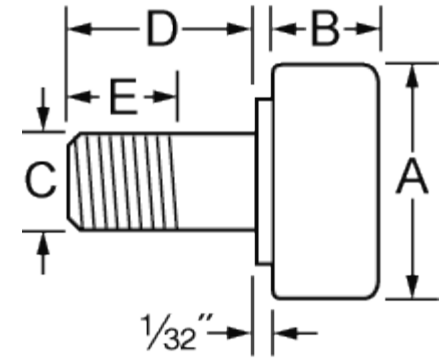


Angled roller bearing

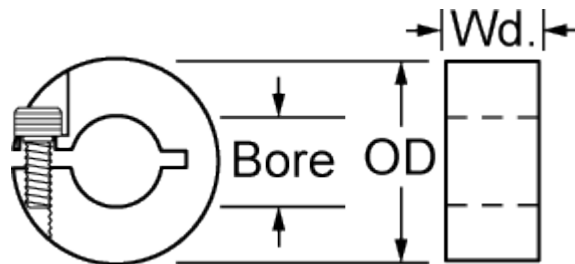
Shaft hardware



Threaded standoff



Cam follower

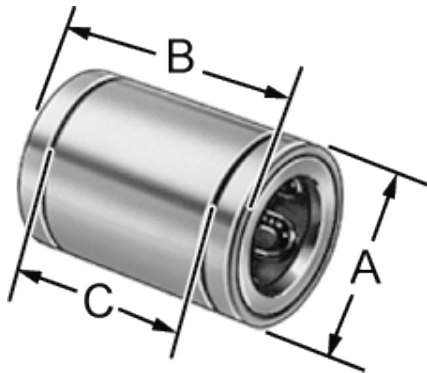


Collar clamp

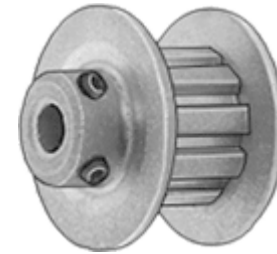
Other motion hardware

<http://www.mcmaster.com/>

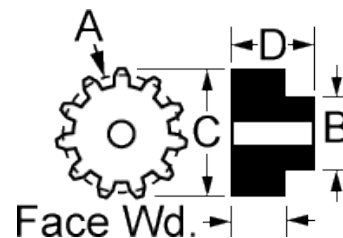
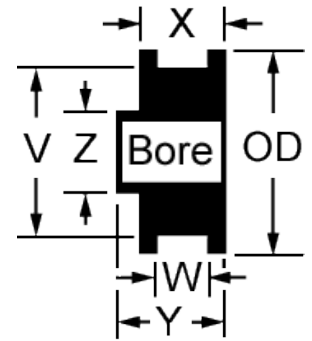
Linear bearing



Timing belt



Timing belt pulley



Rack & pinion

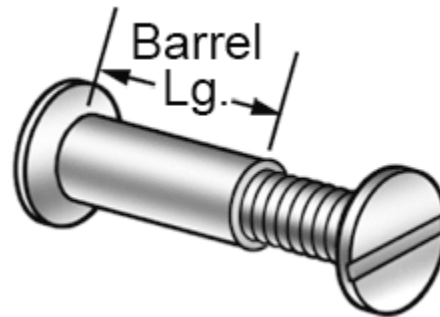
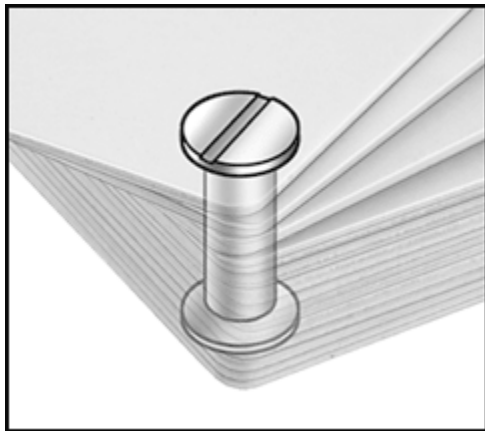
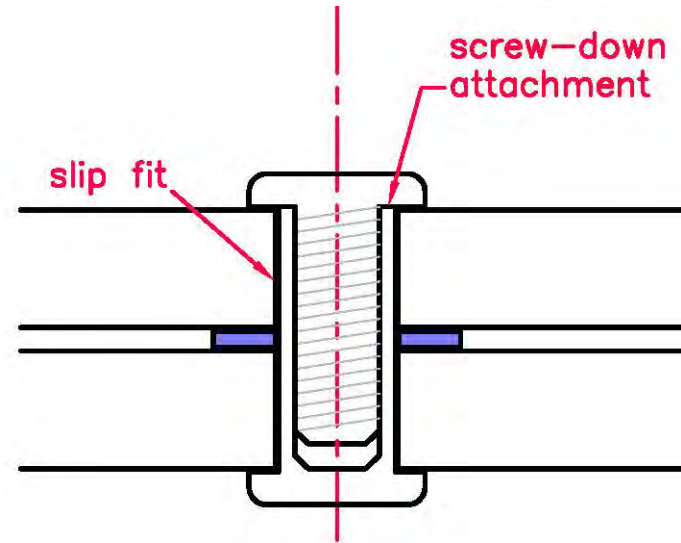
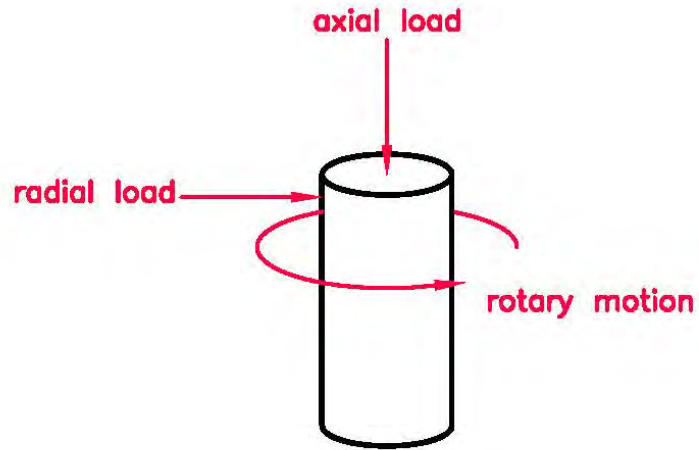
Ball
• Alloy steel, heat treated,
chrome plated for wear
resistance properties.



Bearing with rod end

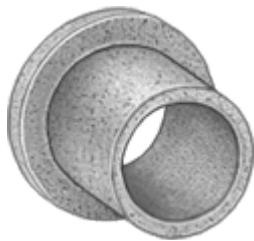
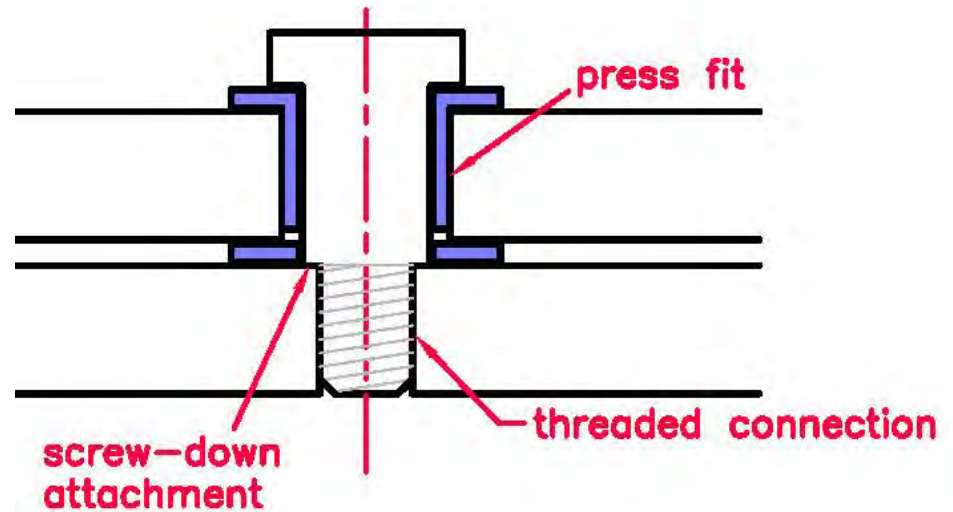
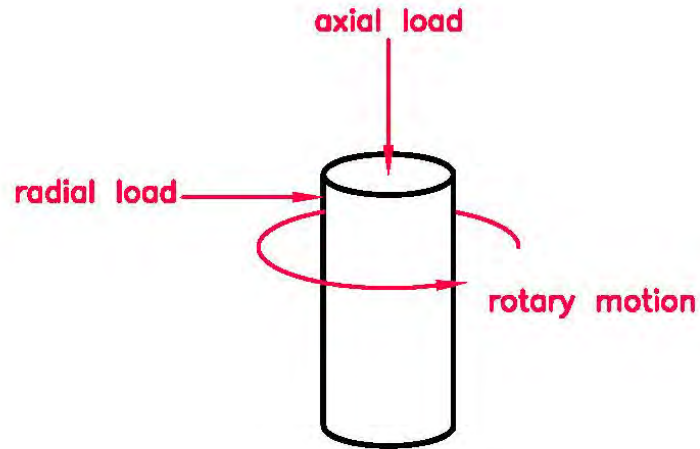
Pivot construction

Binding post connection

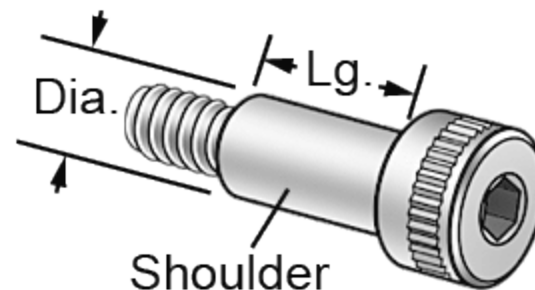


Pivot construction

Shoulder screw connection

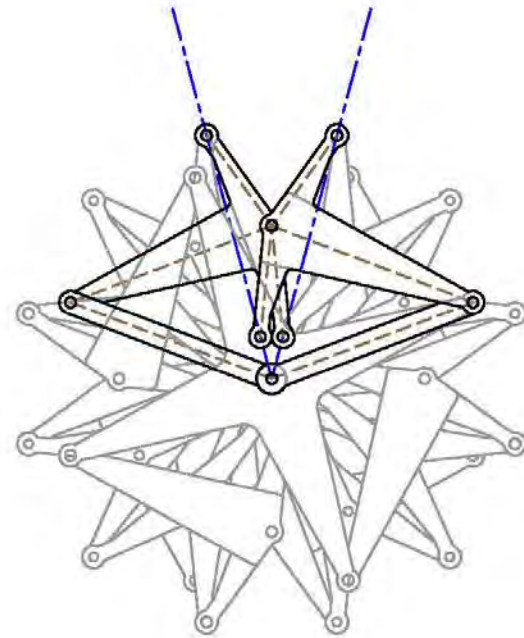
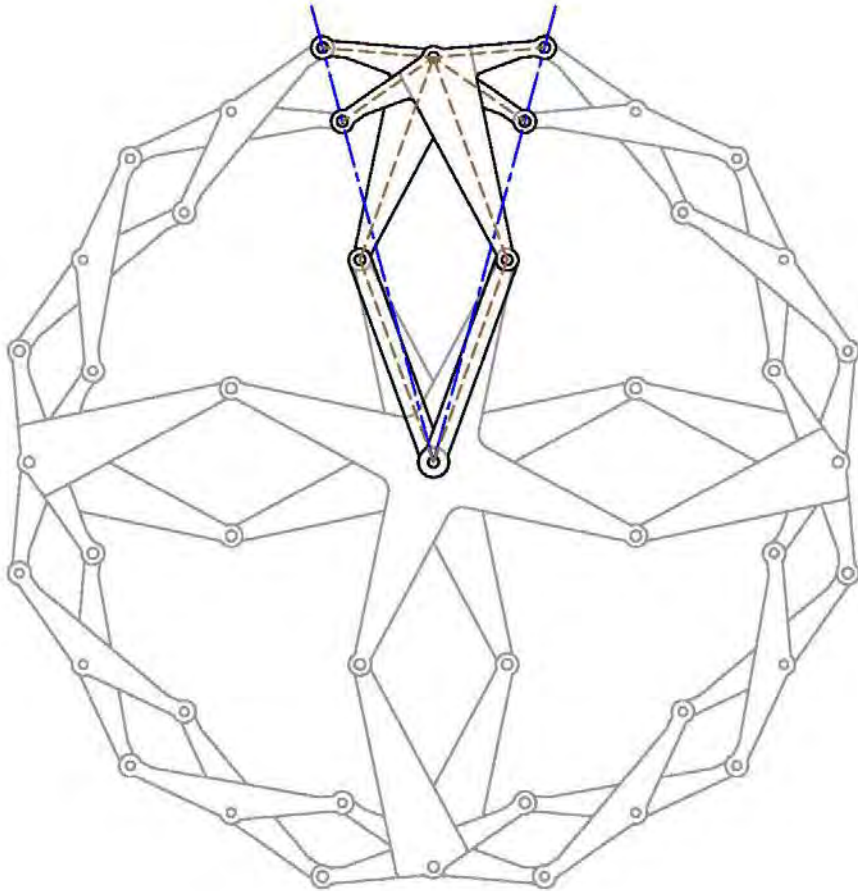


Flanged Sleeve bearing

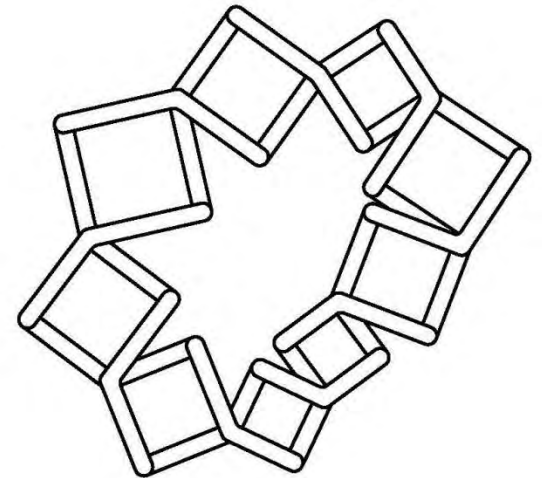
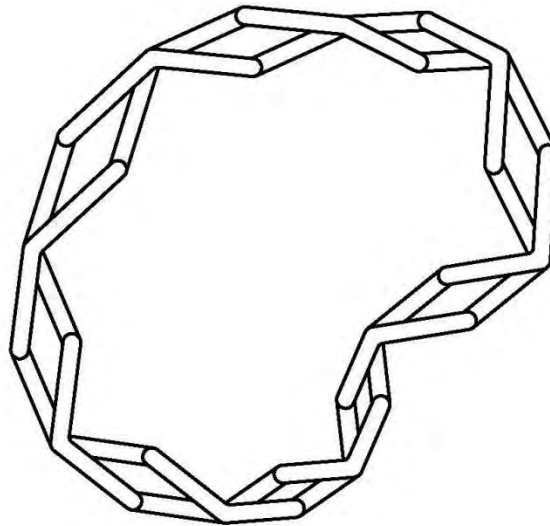
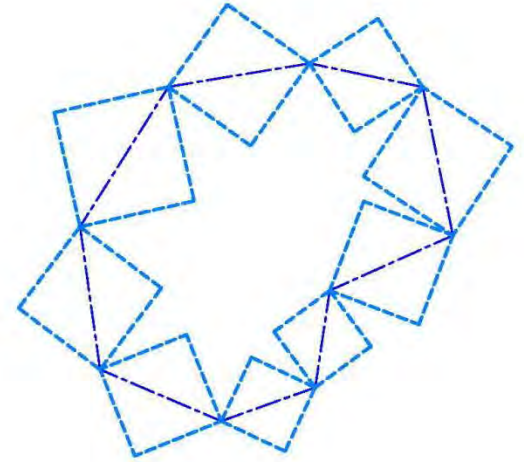
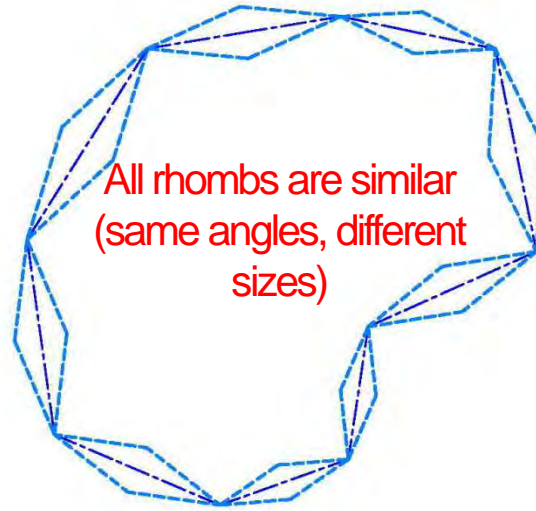
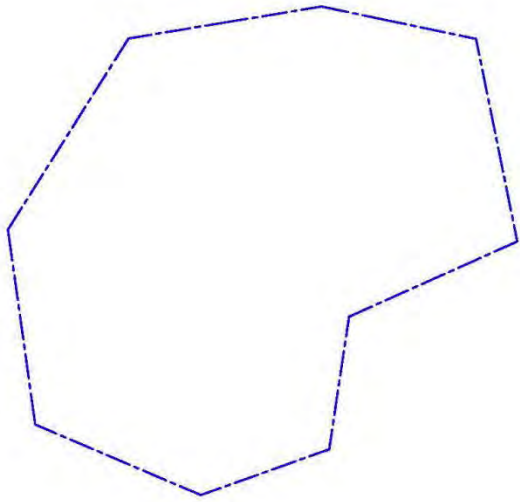


Shoulder screw

circular linkage with fixed center (four spokes)

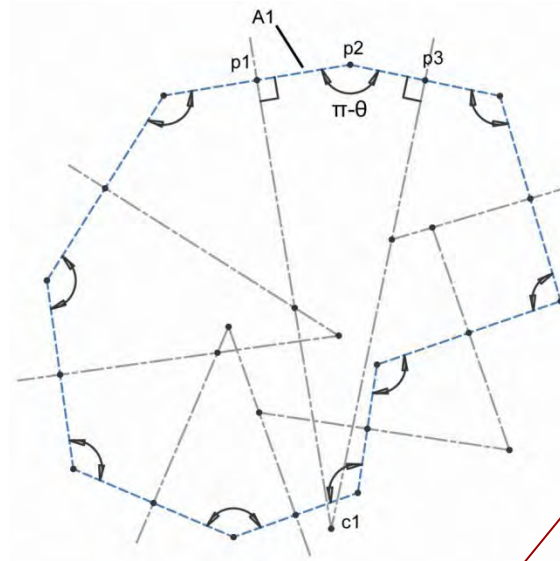
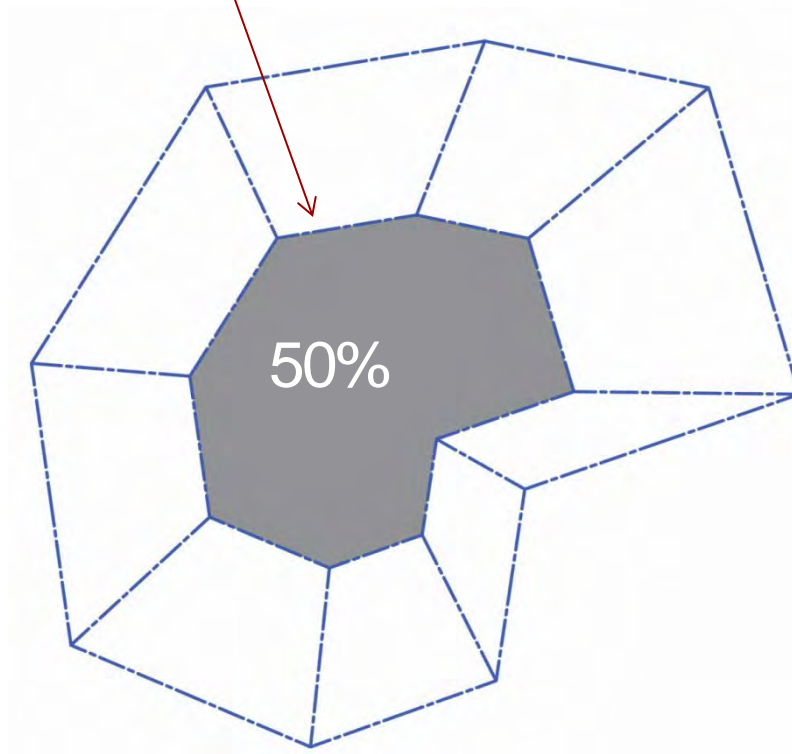


Irregular polygon – geometric construction

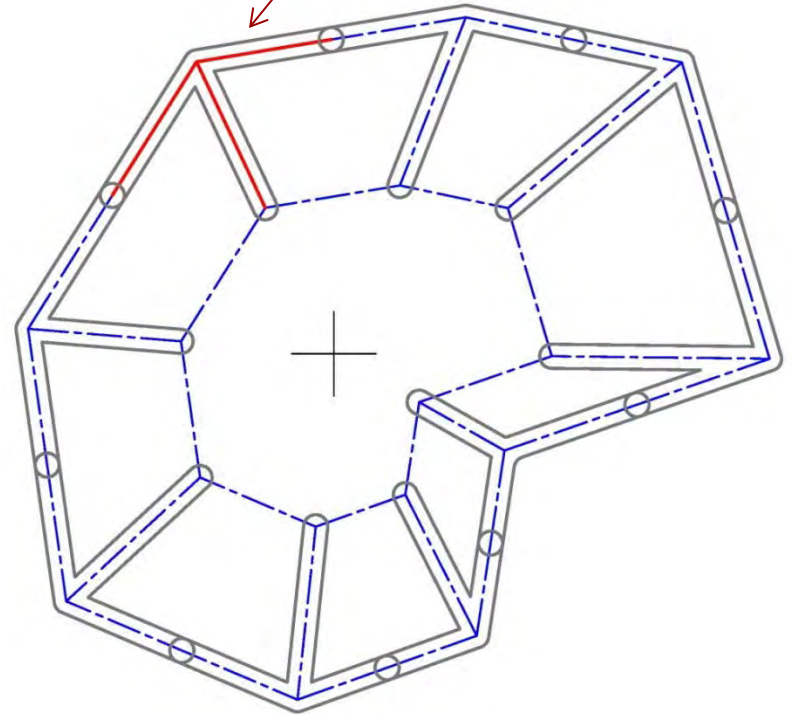


Center link for asymmetric polygon linkages

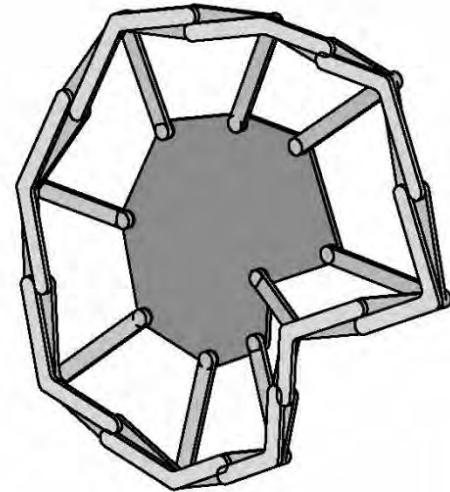
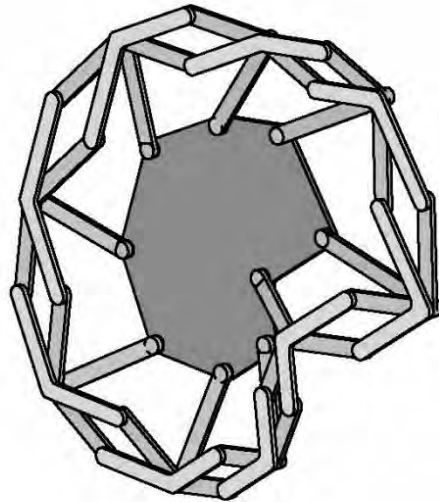
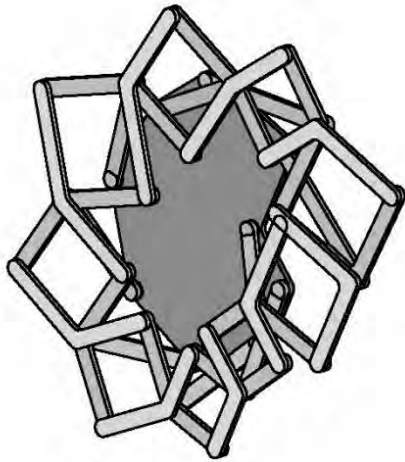
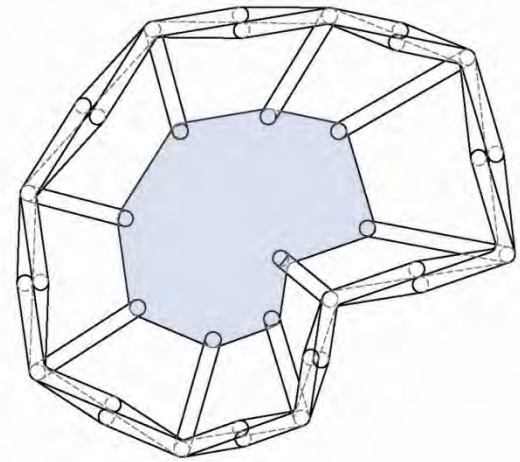
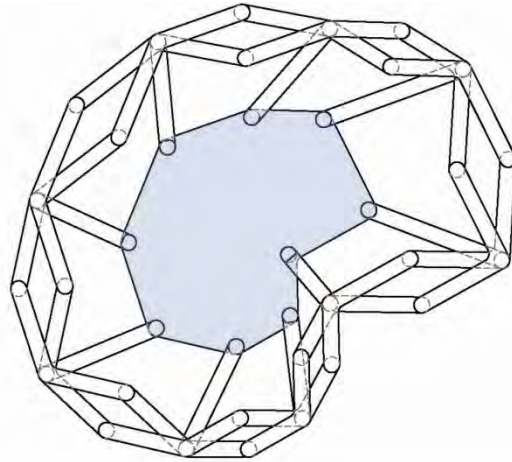
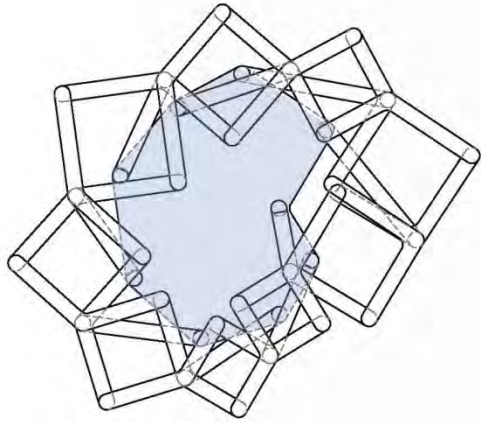
Define center link at 50% scale to original polygon



Define 3-pivot links
As shown



Center link for asymmetric polygon linkages



Geometric construction - wheel

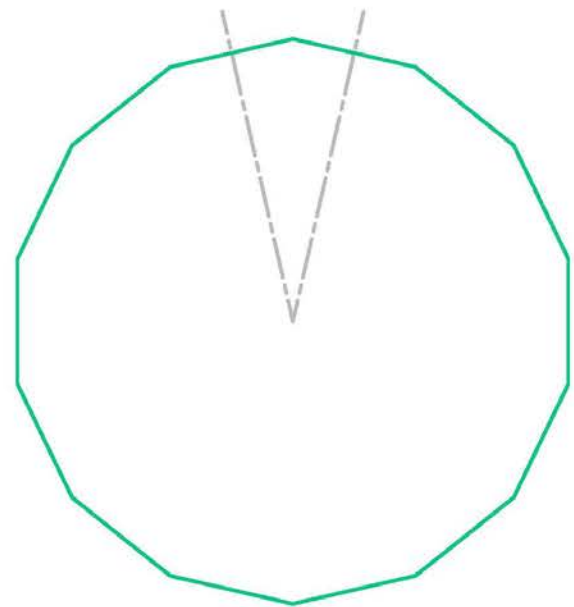
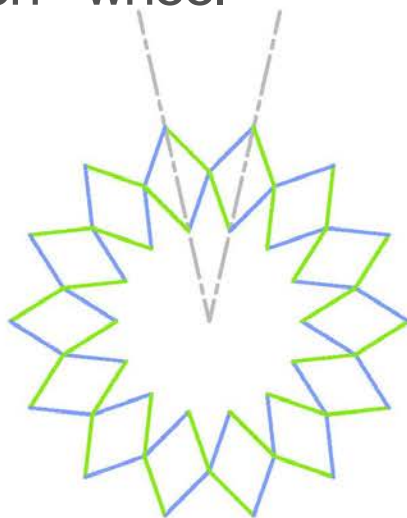


scissor
element

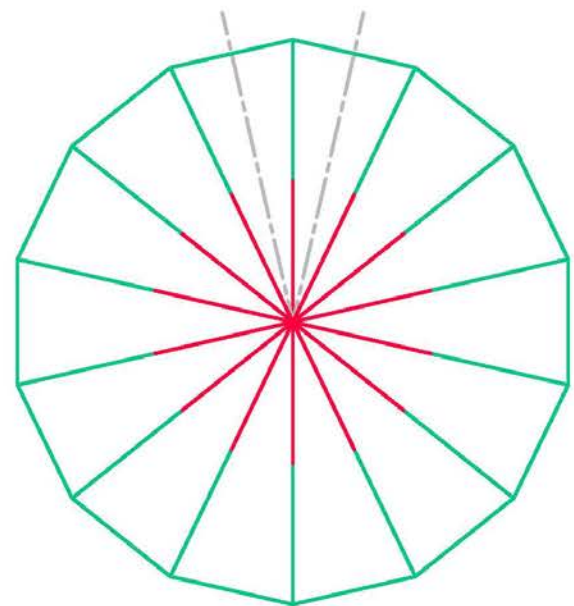
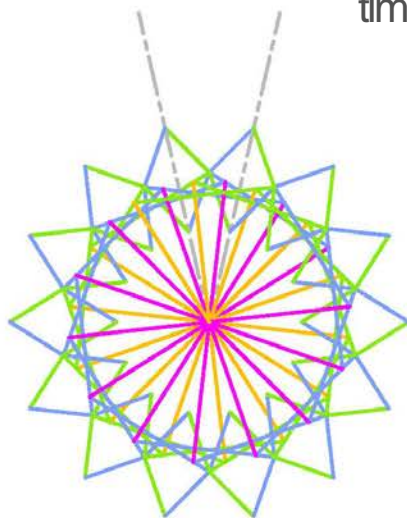


Scissor / spoke
element

Geometric construction - wheel

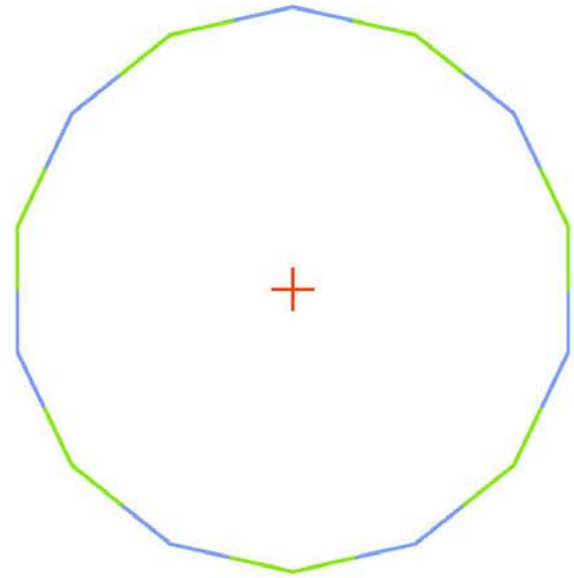
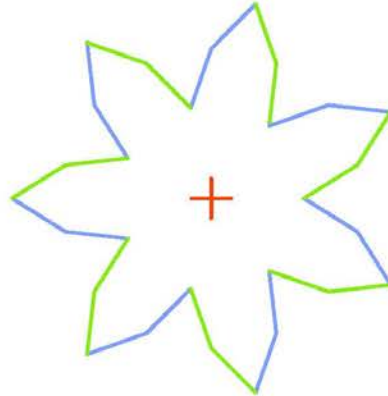
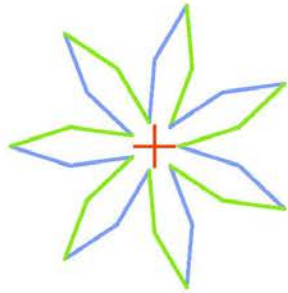


Arrayed 14
times



Geometric construction - wheel

- Remove every other scissor / spoke element

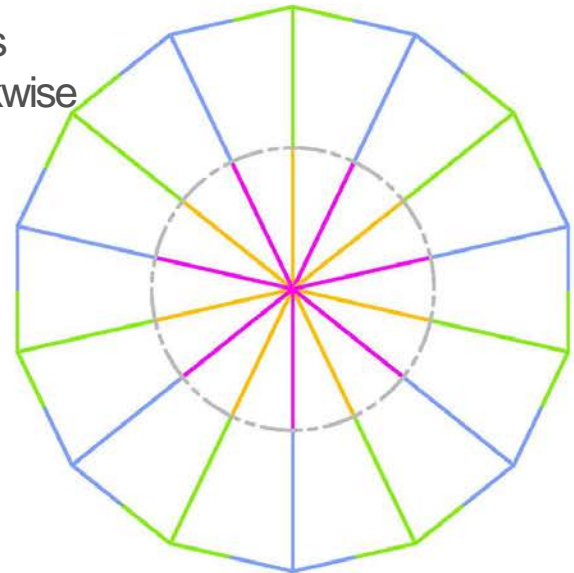
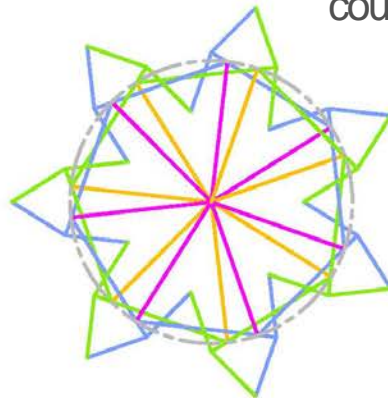
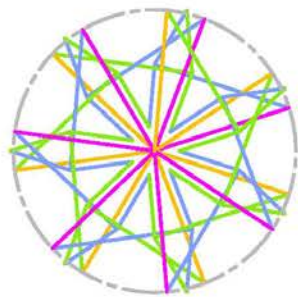


As wheel expands

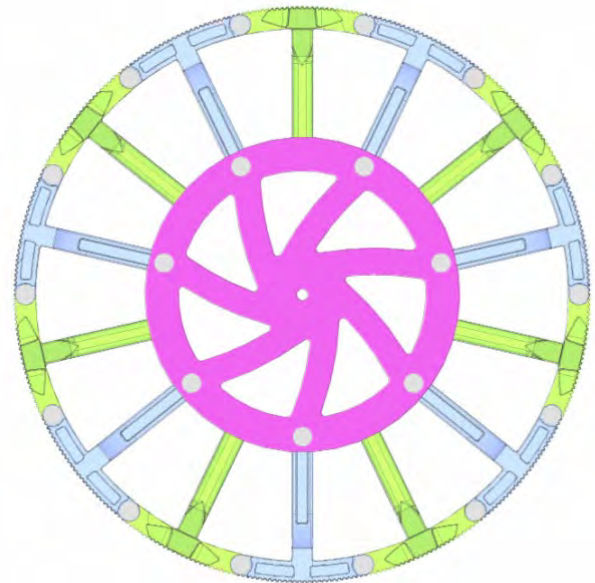
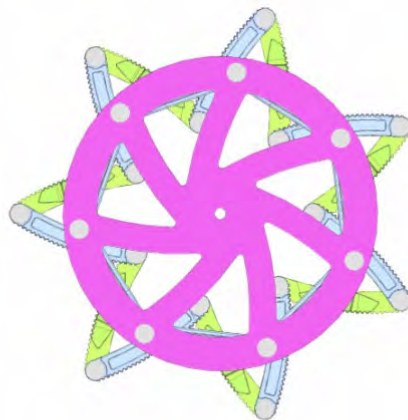
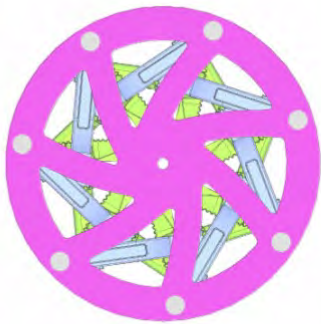
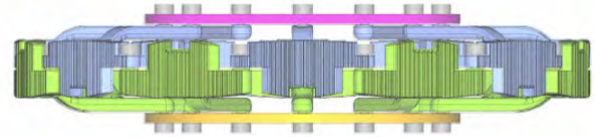
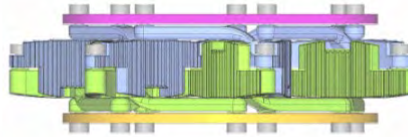
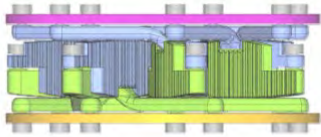


Orange rotates
clockwise

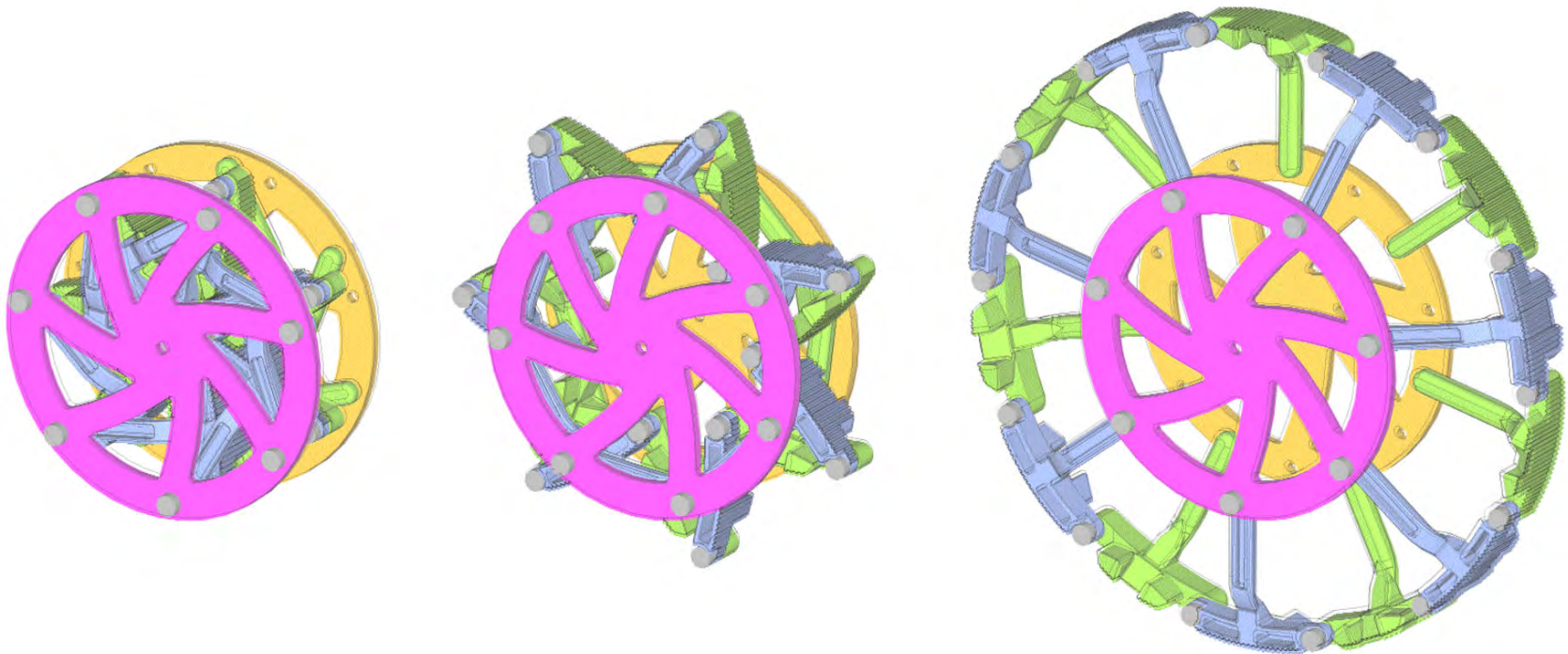
purple rotates
counter-clockwise



Geometric construction - wheel



Geometric construction - wheel

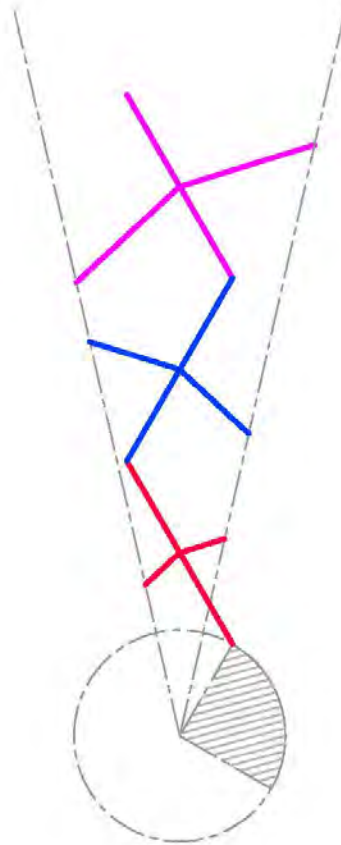
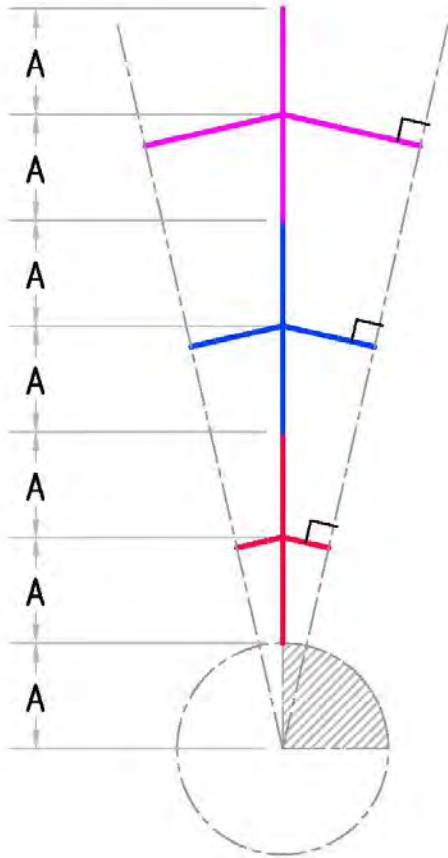


Wheel

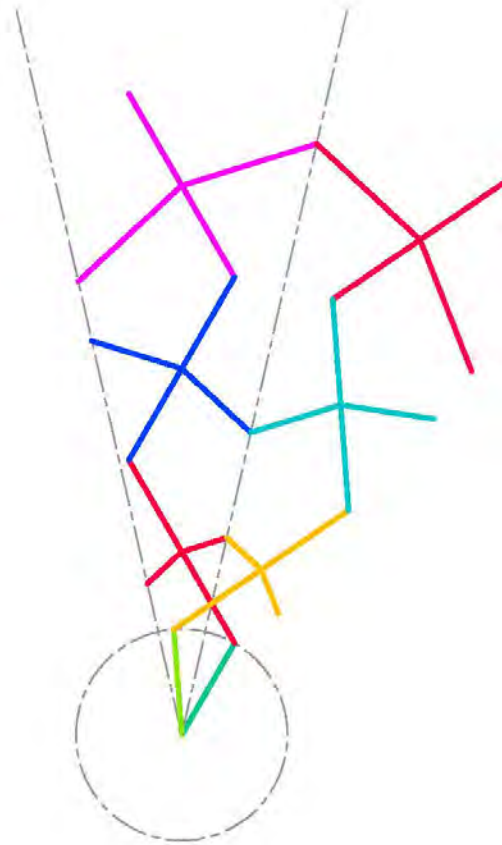
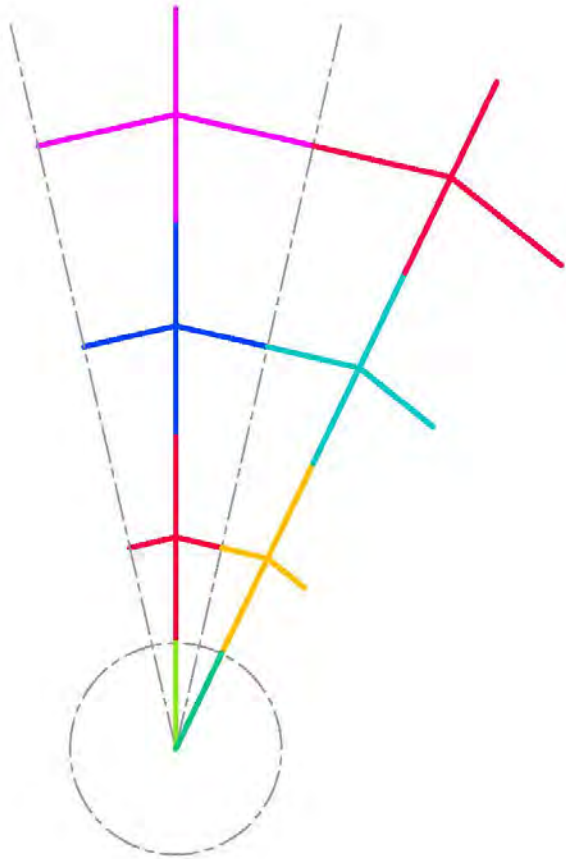


Extended expanding wheels

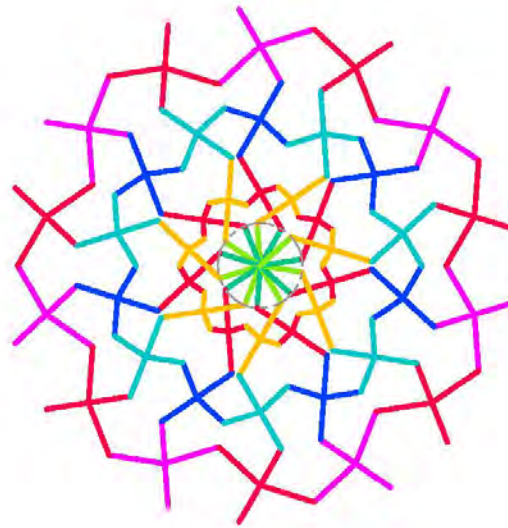
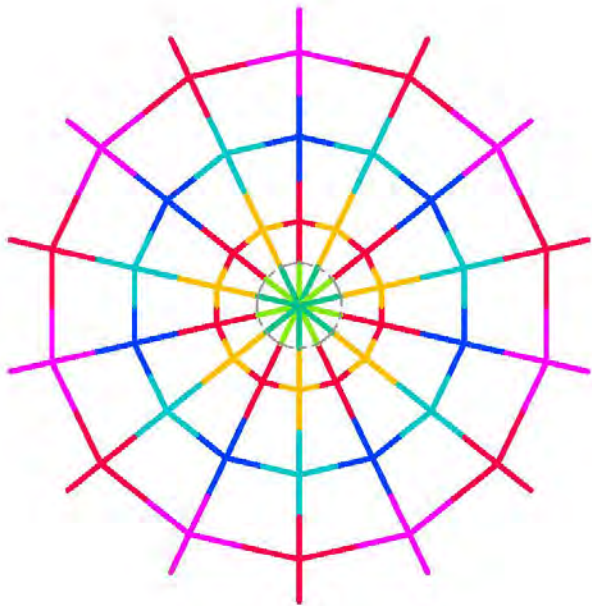
Extended wheel geometry



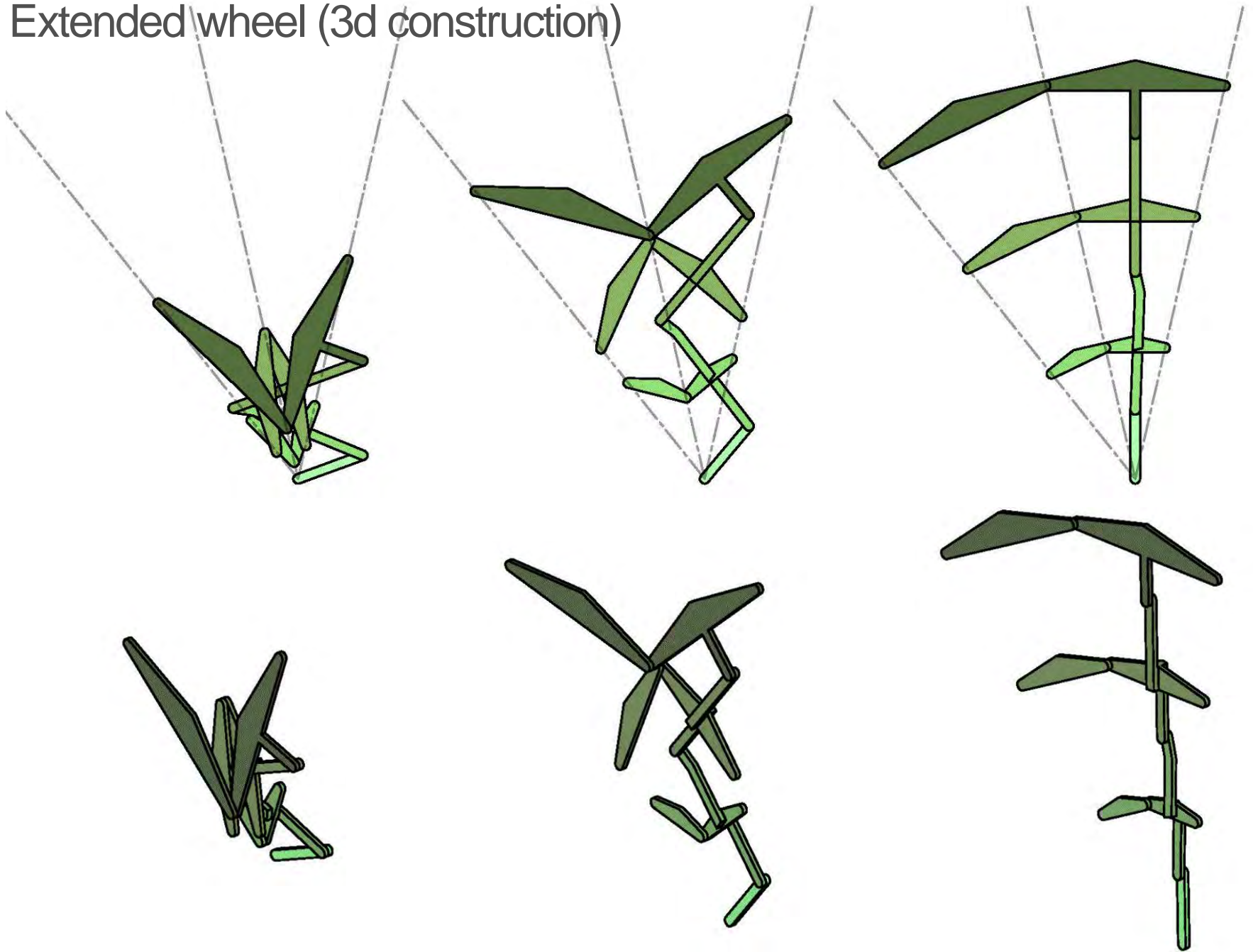
Extended wheel geometry



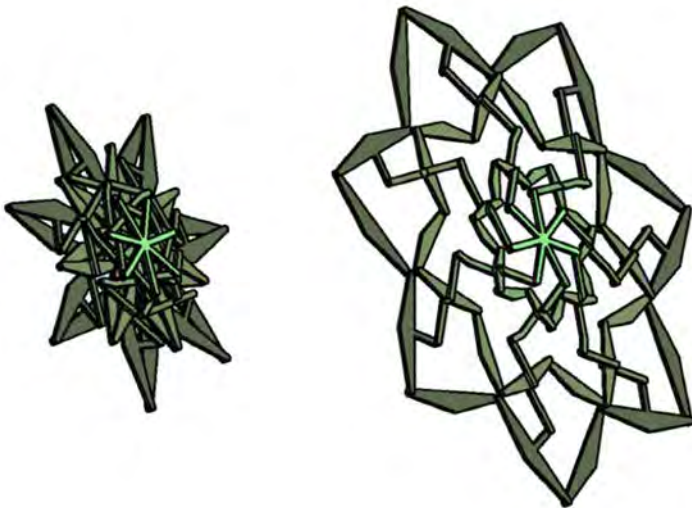
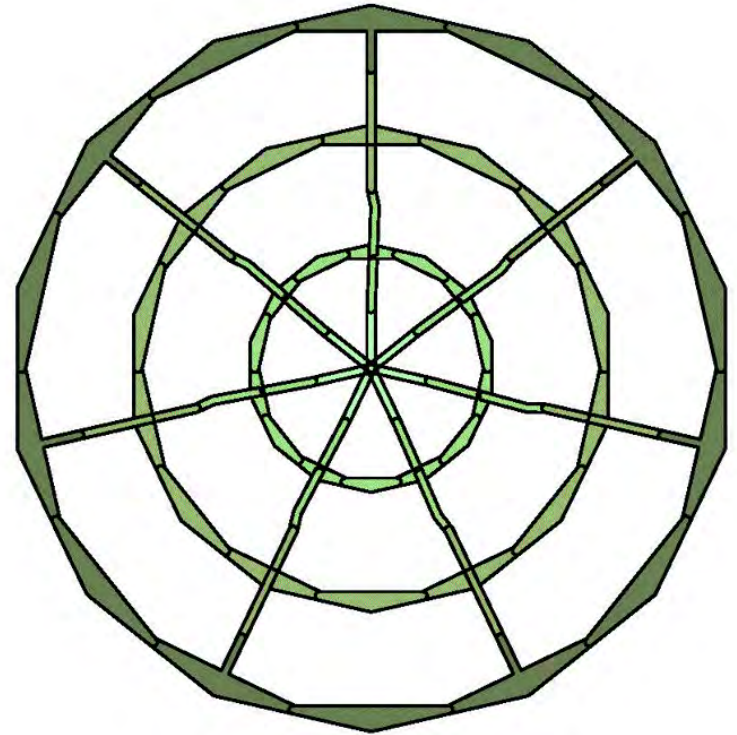
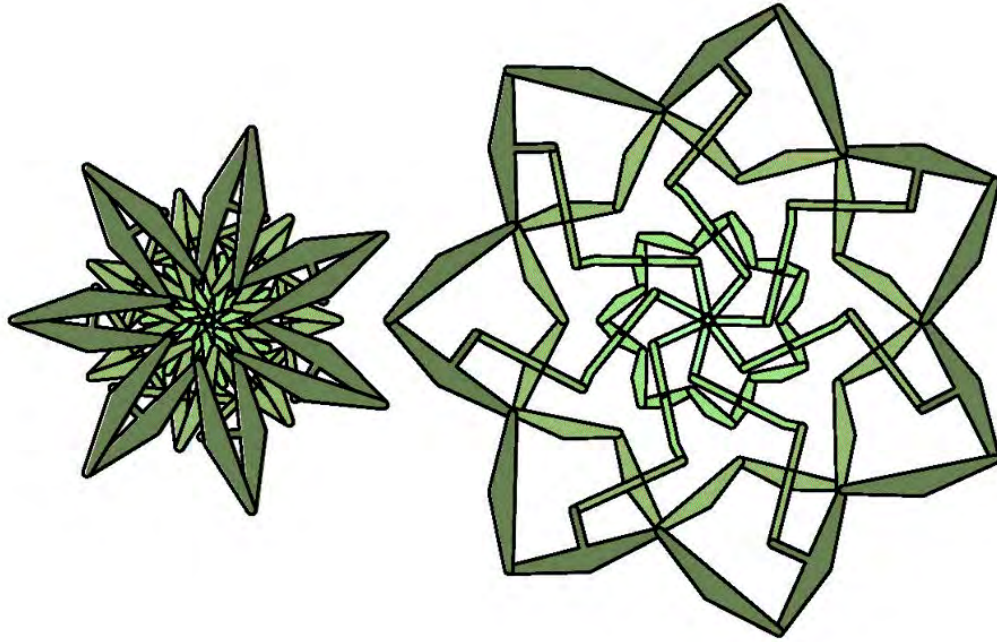
Extended wheel geometry



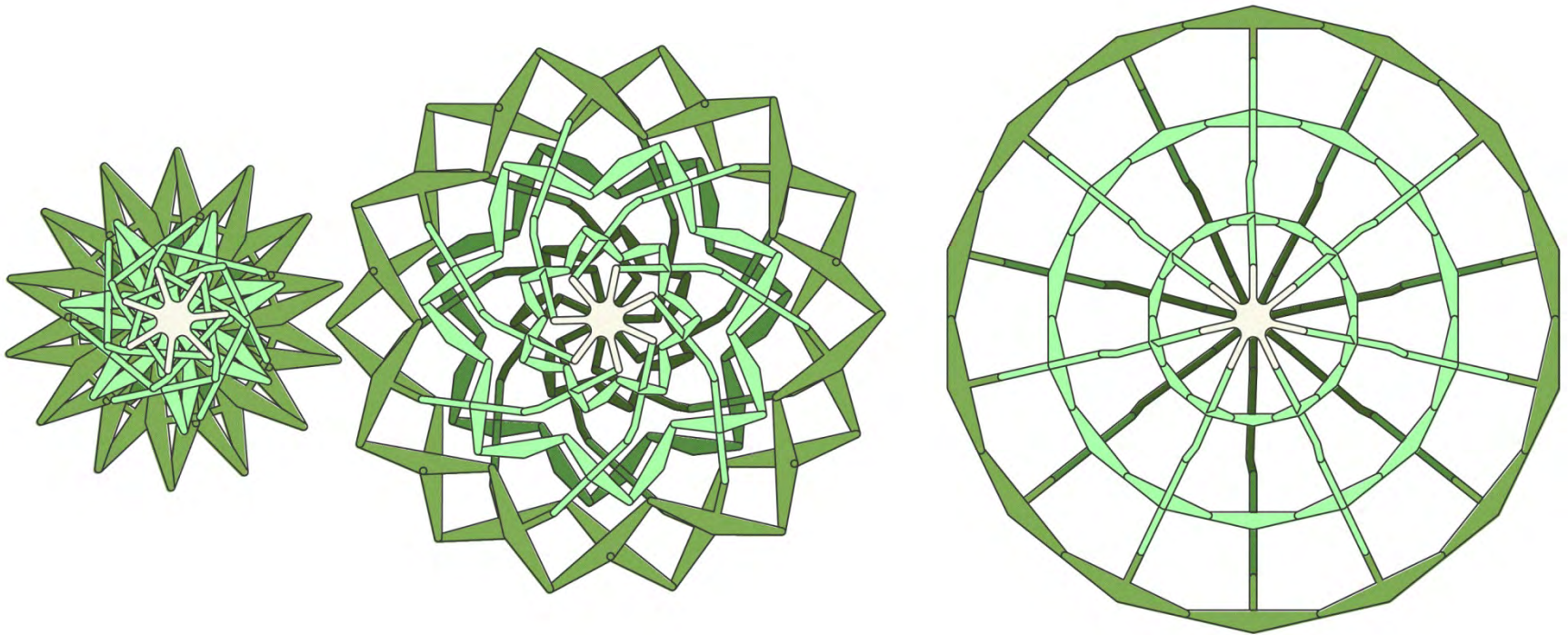
Extended wheel (3d construction)



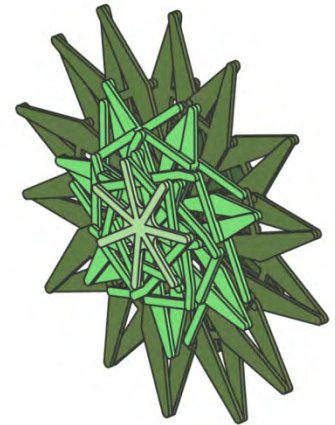
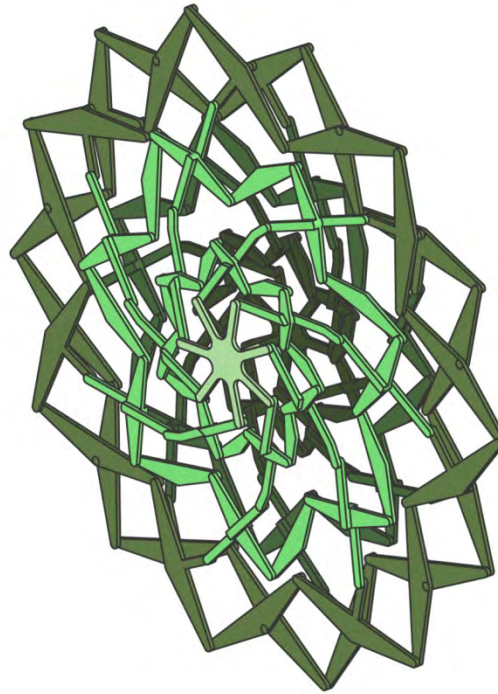
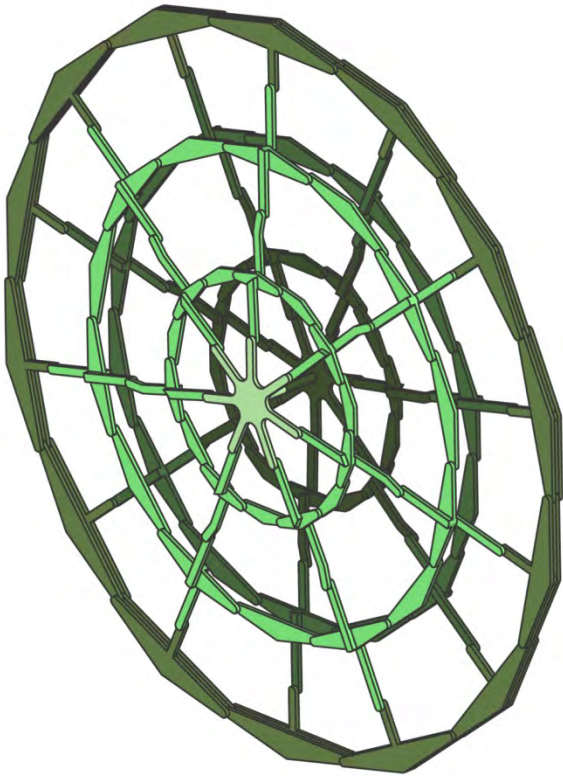
Extended wheel (3d construction)



Extended wheel (doubled construction)



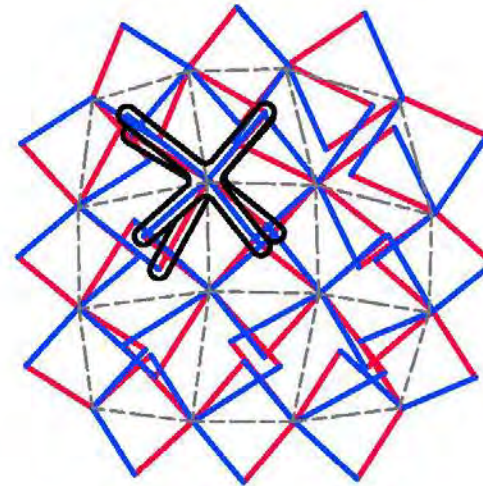
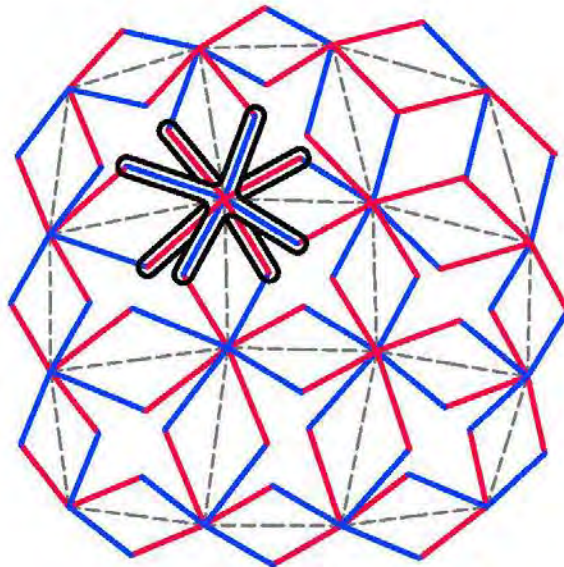
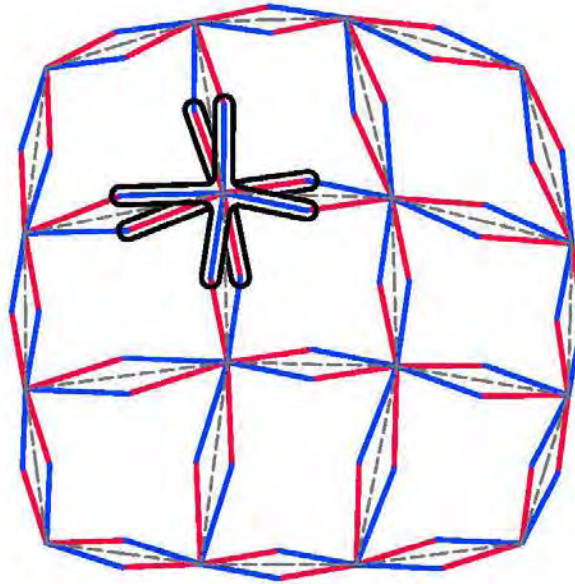
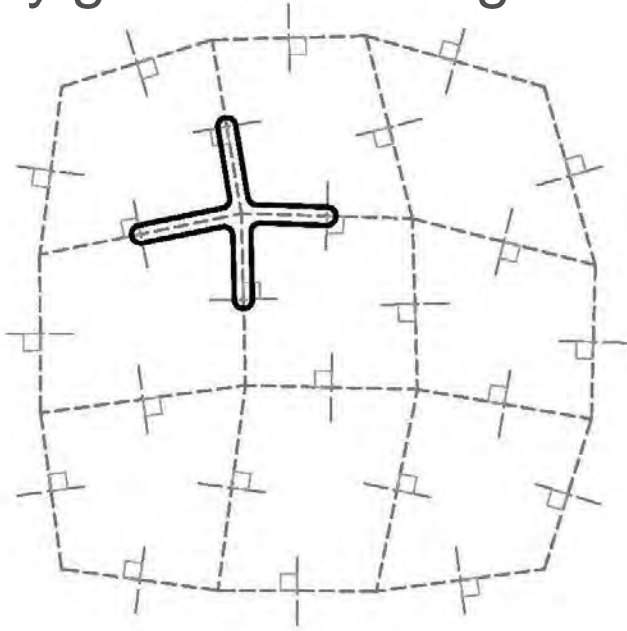
Extended wheel (doubled construction)



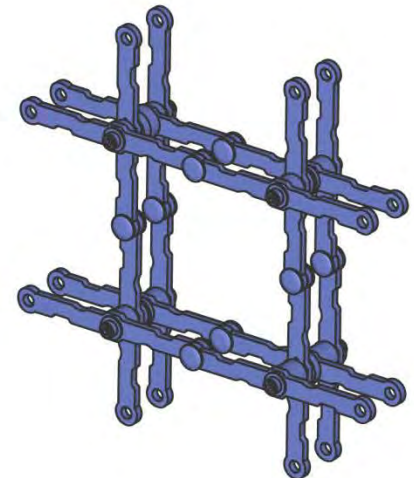
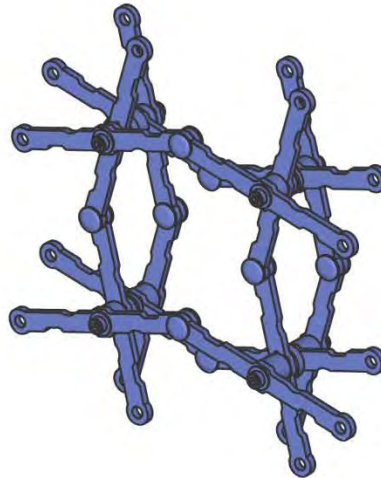
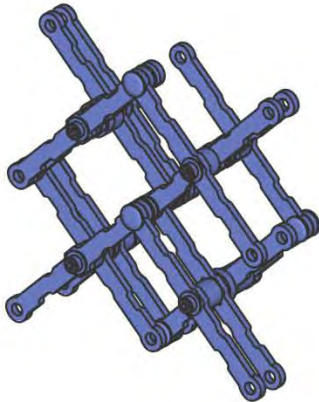
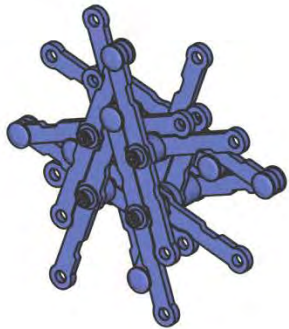
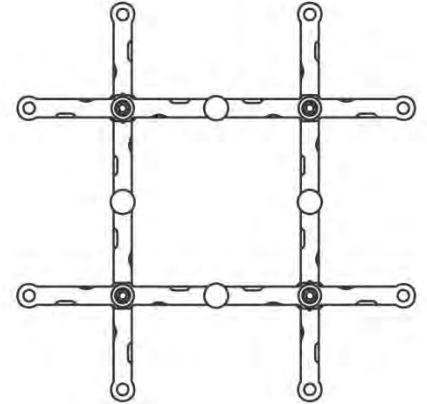
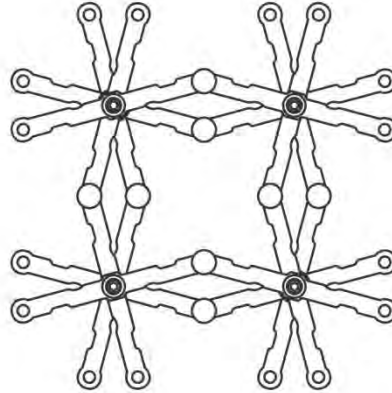
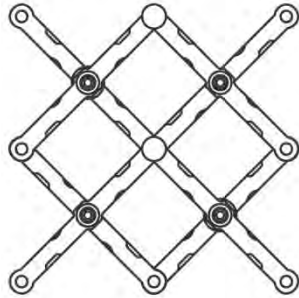
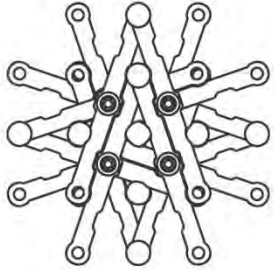


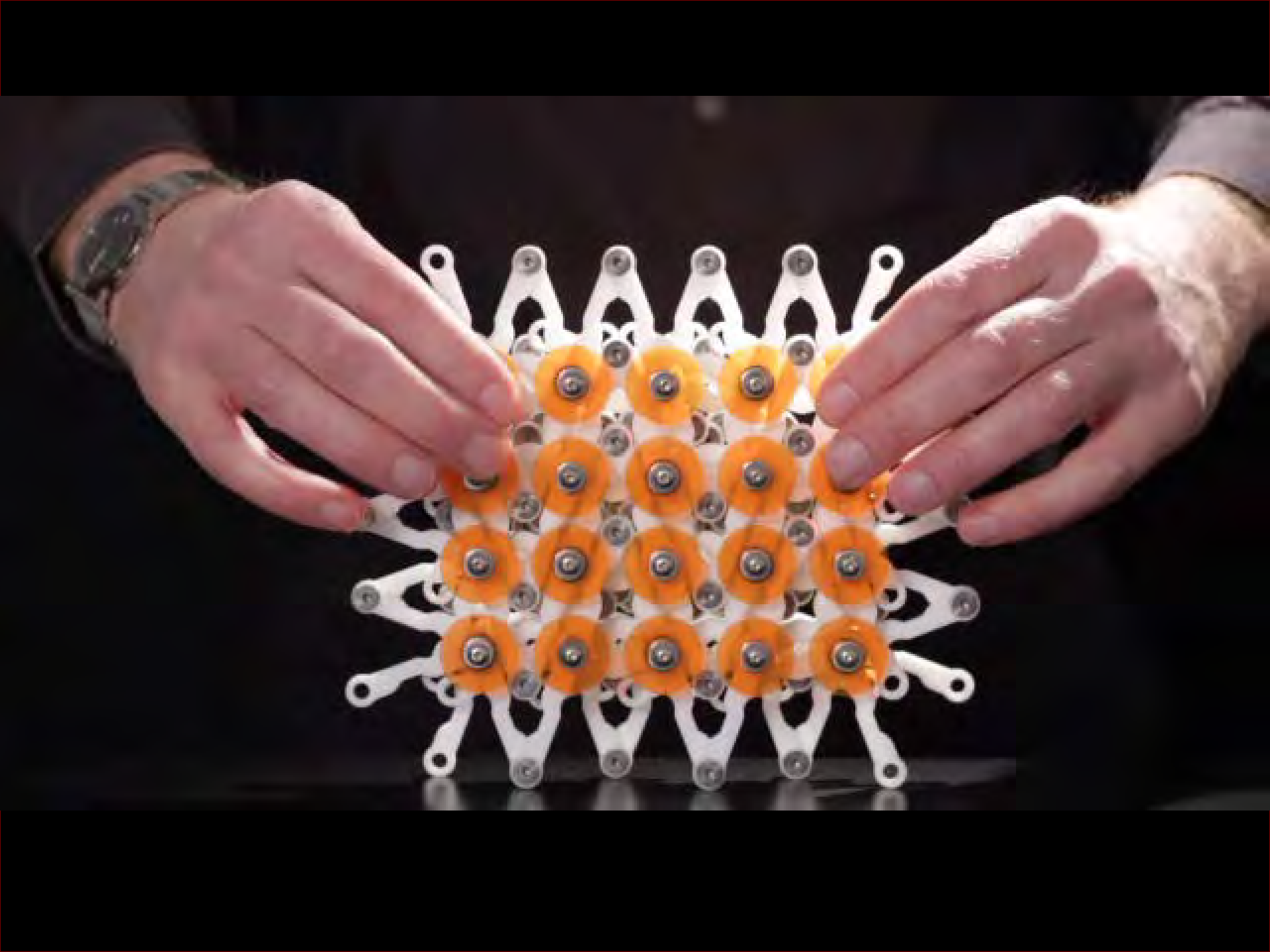
Expanding polygon arrays

4-way grid made of angulated scissors

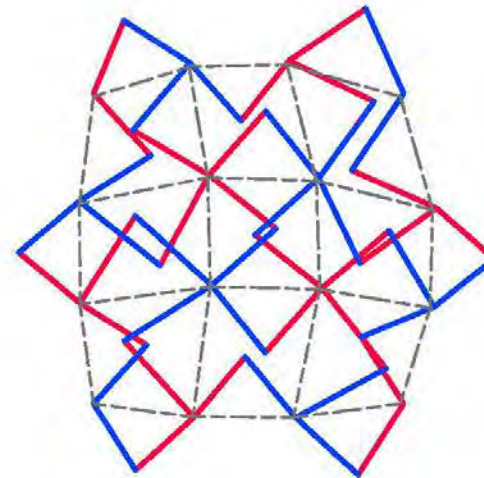
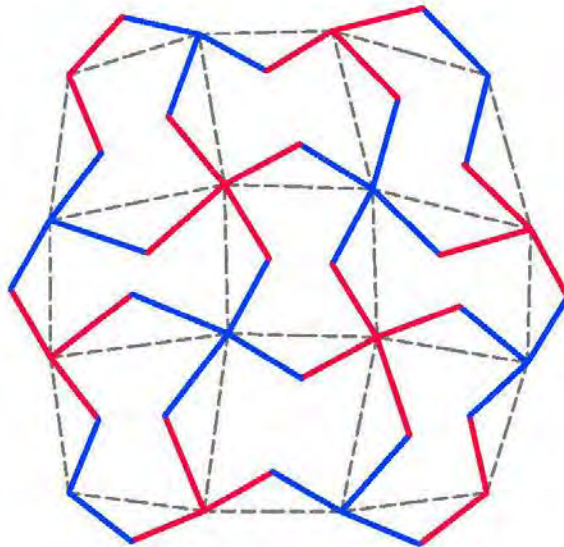
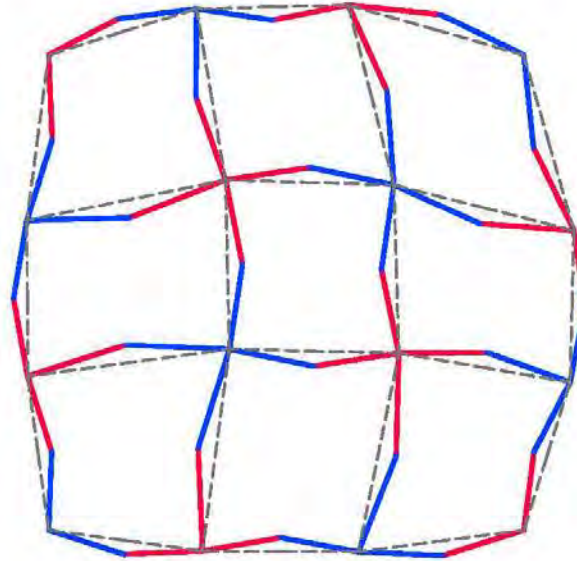
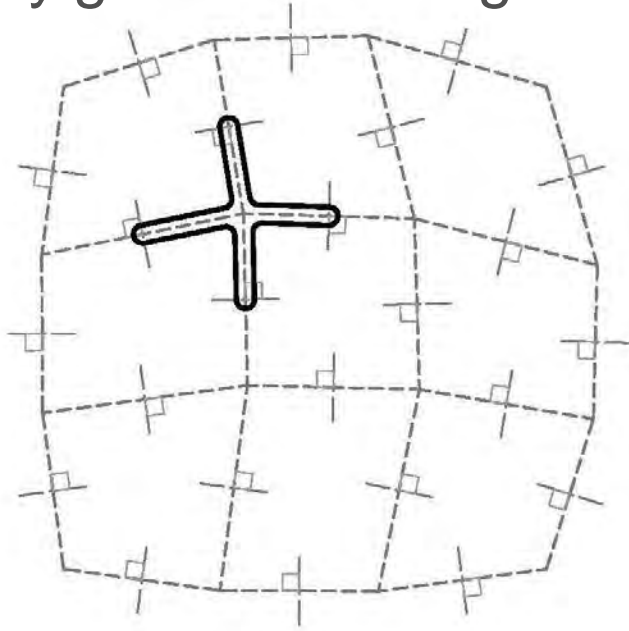


4-way grid made of angulated scissors

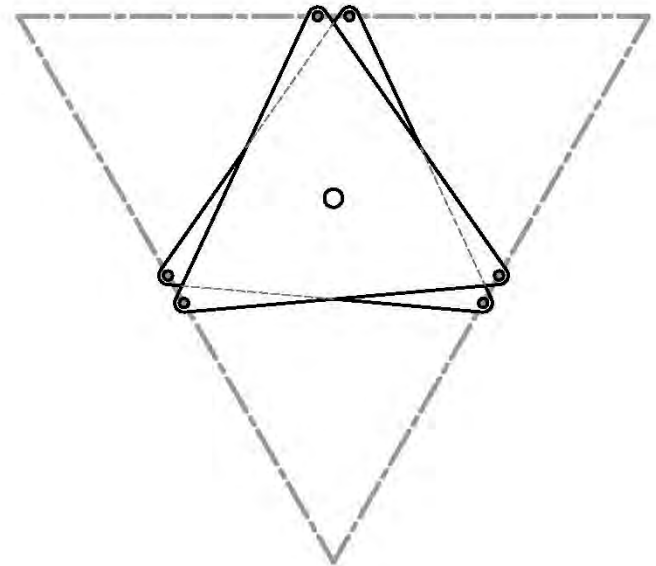
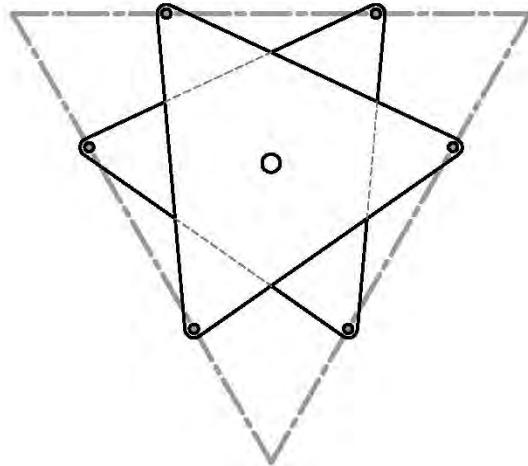
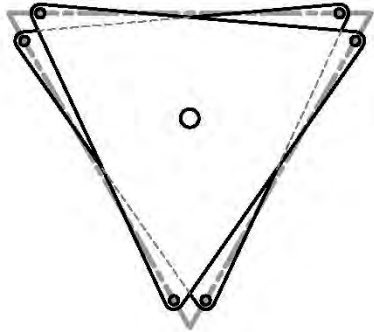




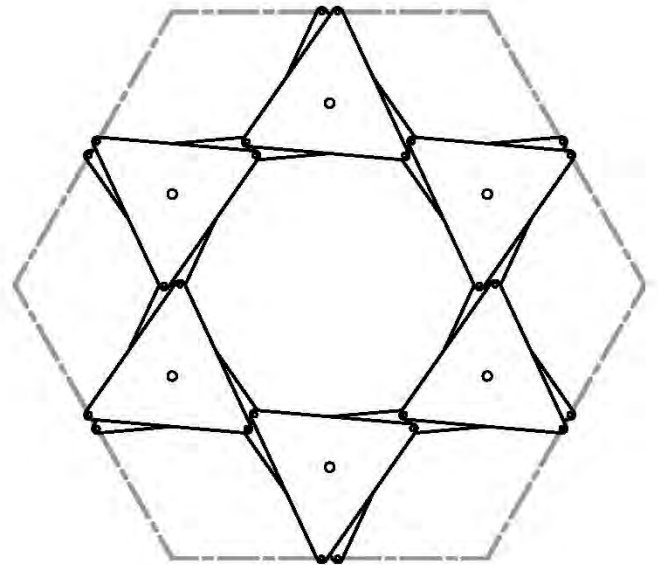
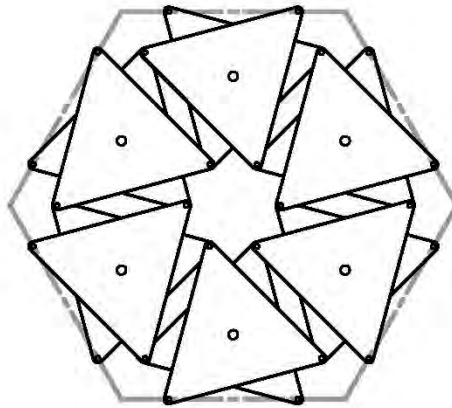
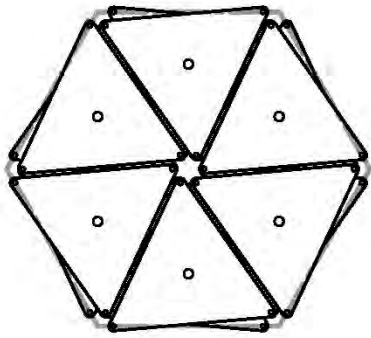
4-way grid made of angulated links (not doubled)



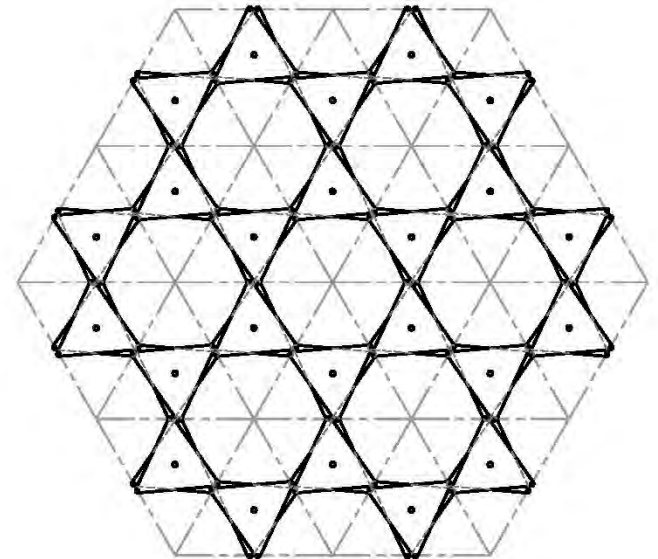
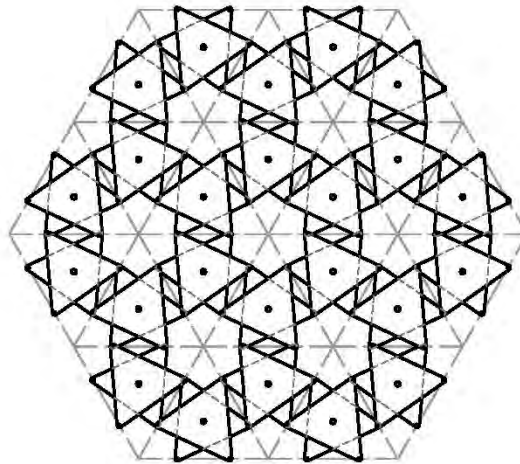
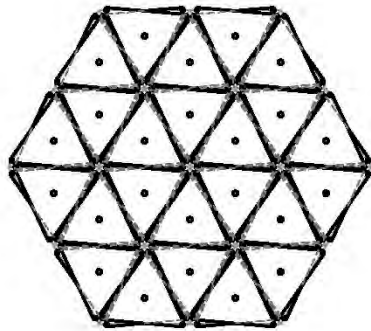
3-way scissor (doubled triangle)



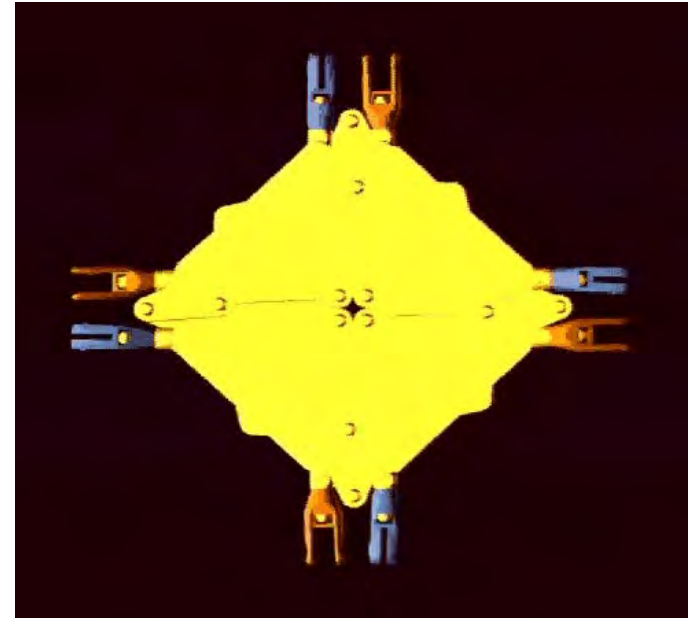
3-way scissor (doubled triangle)



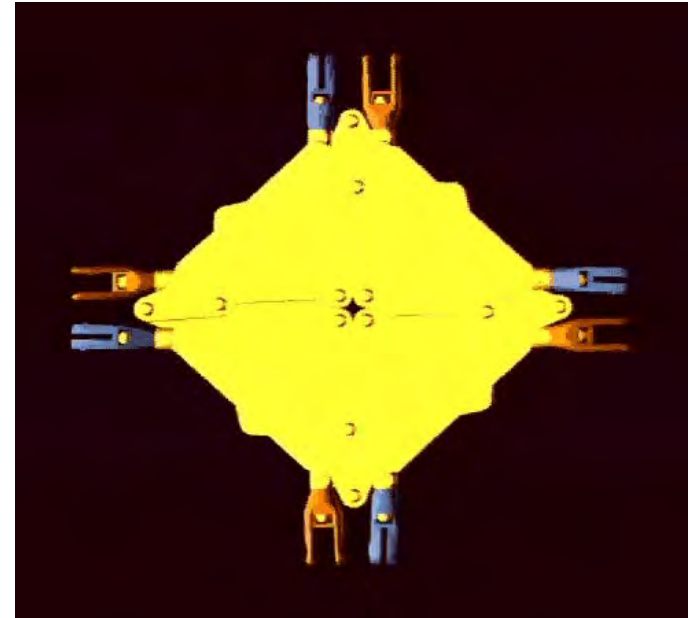
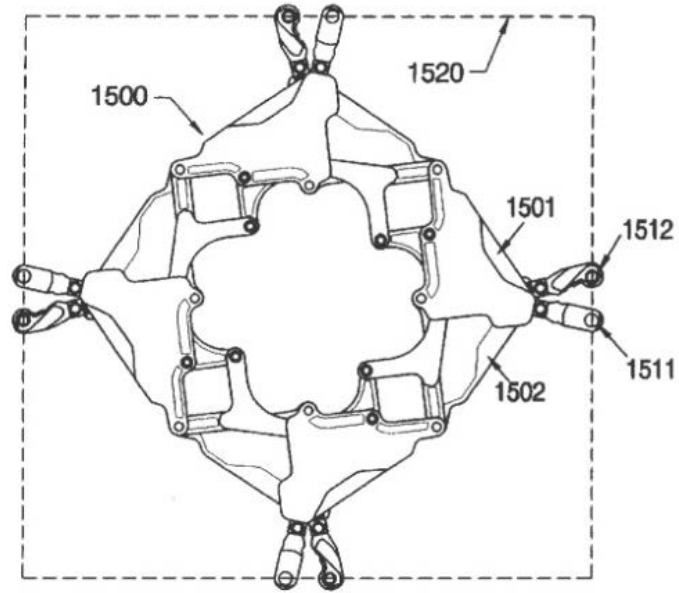
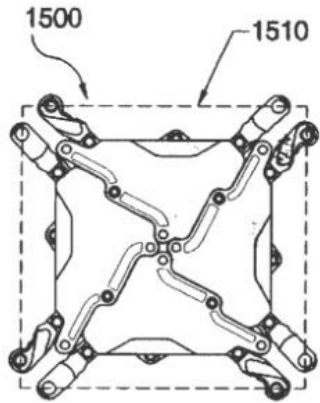
3-way scissor (doubled triangle)



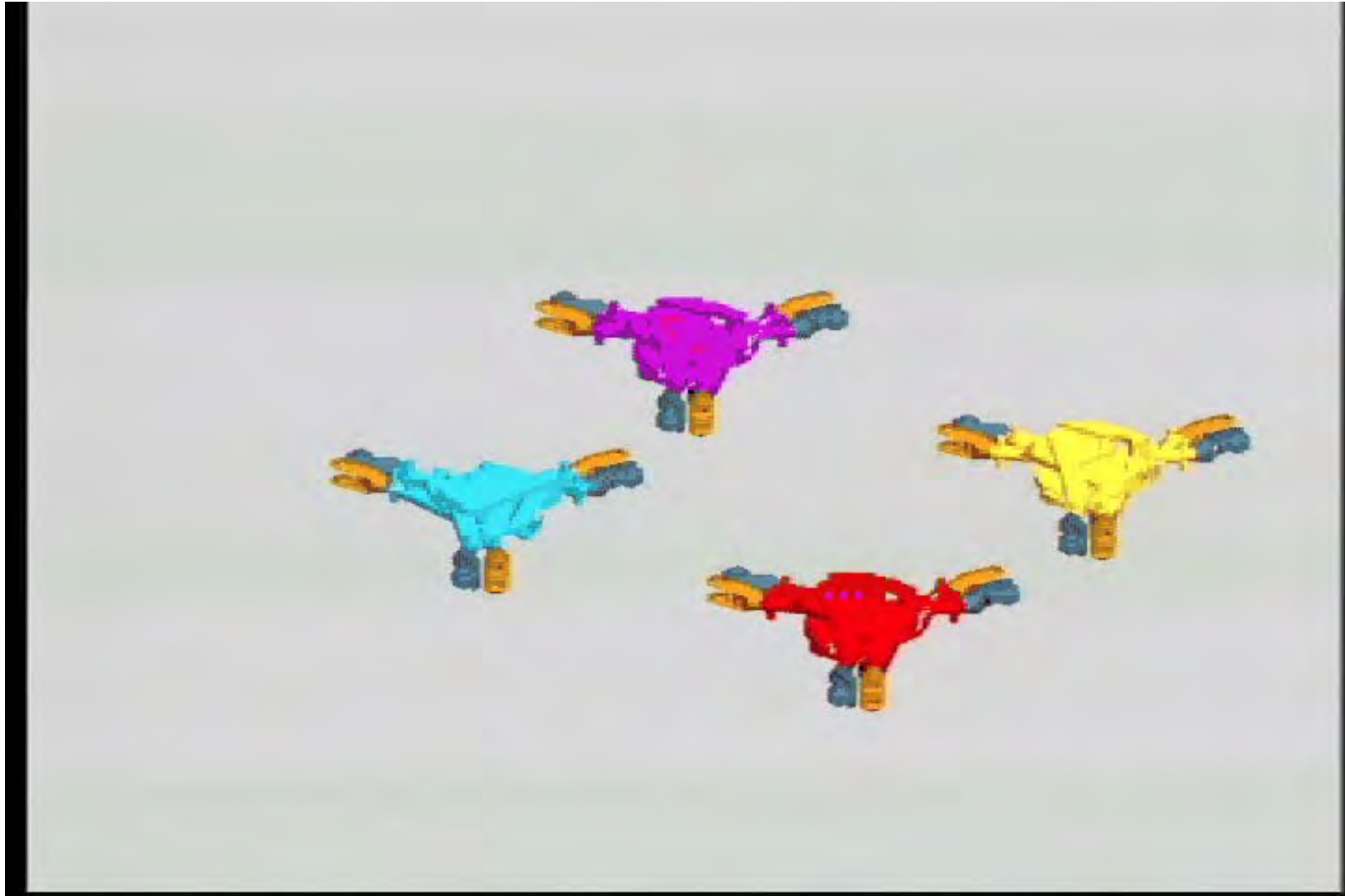
Expandagon construction system



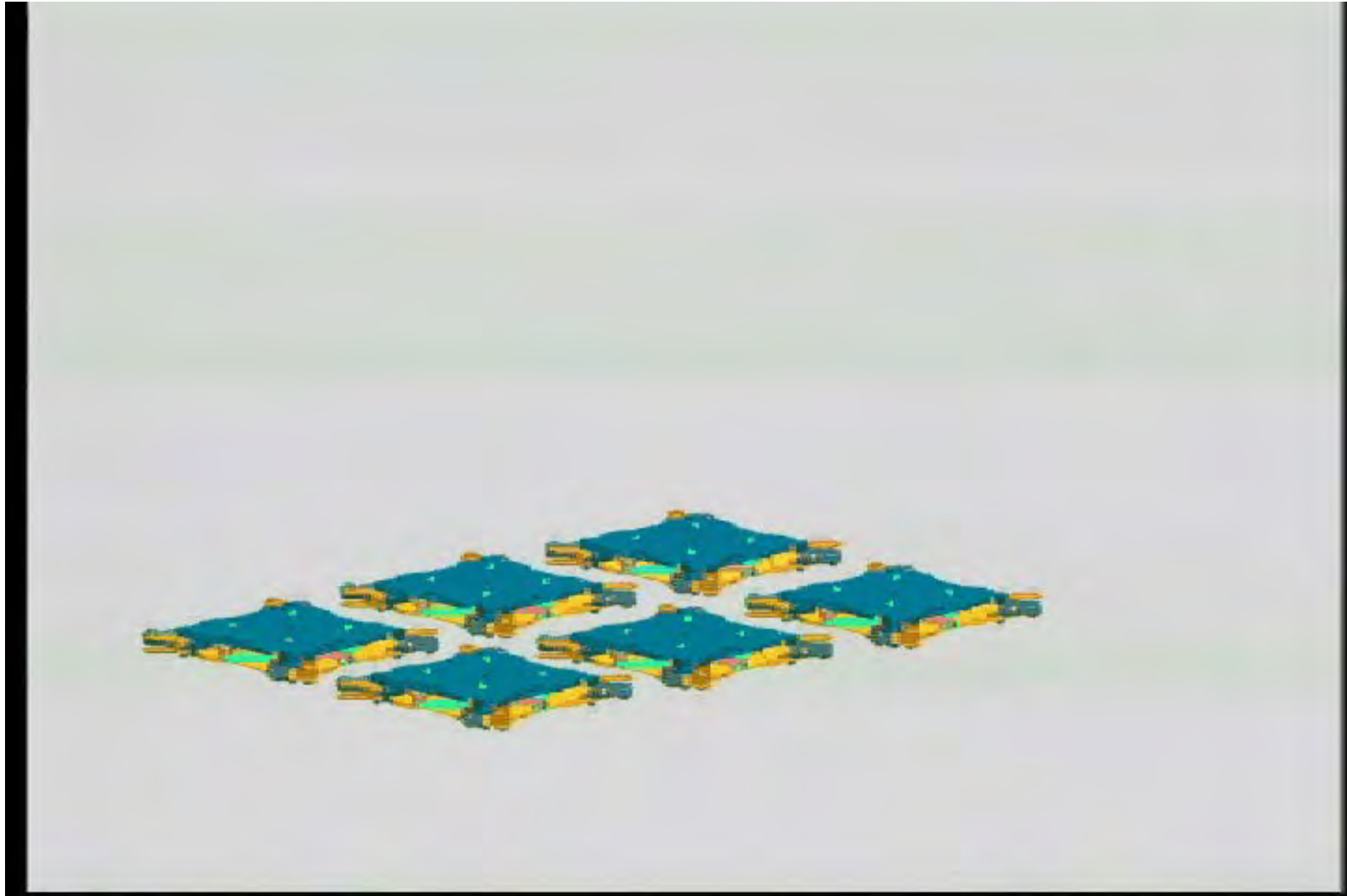
Dynamic envelope



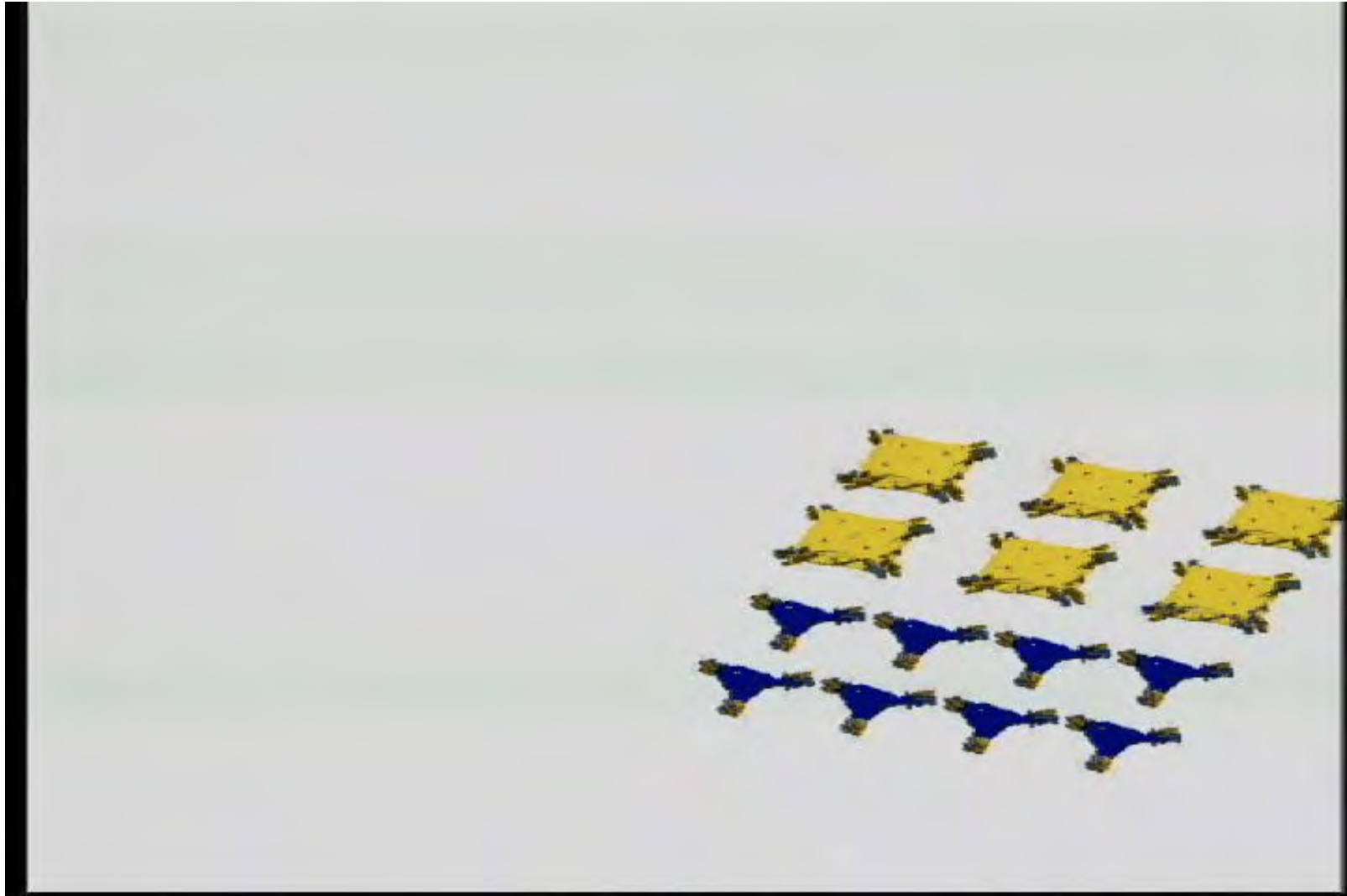
Expandagon assembly



Expandagon assembly

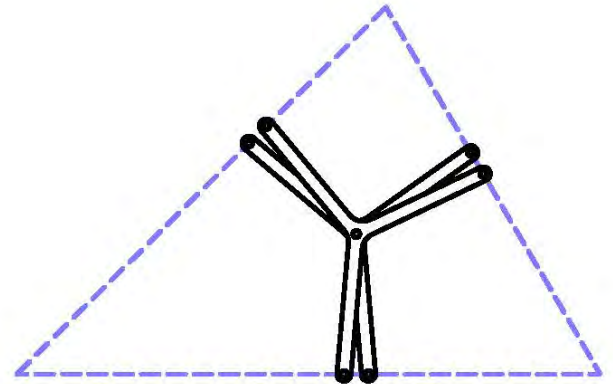
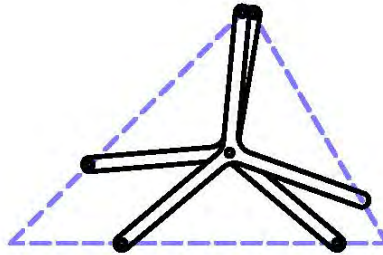
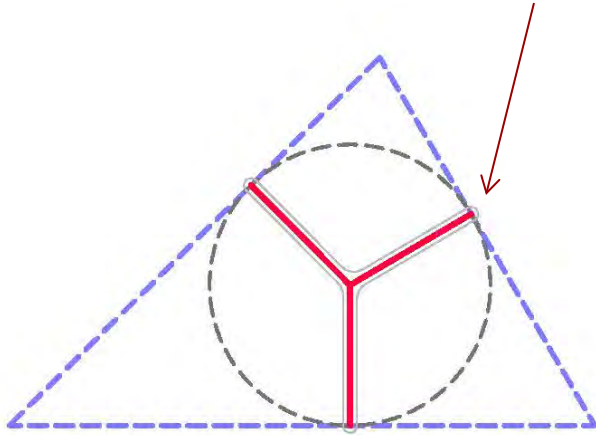


Expandagon assembly



General method for expanding triangle (edges preserved)

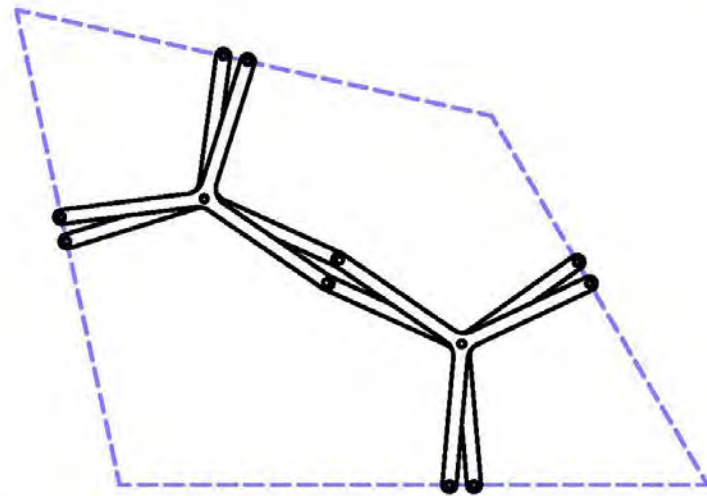
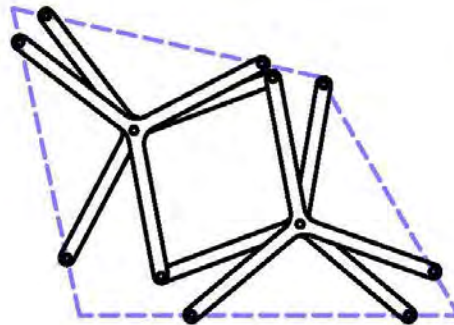
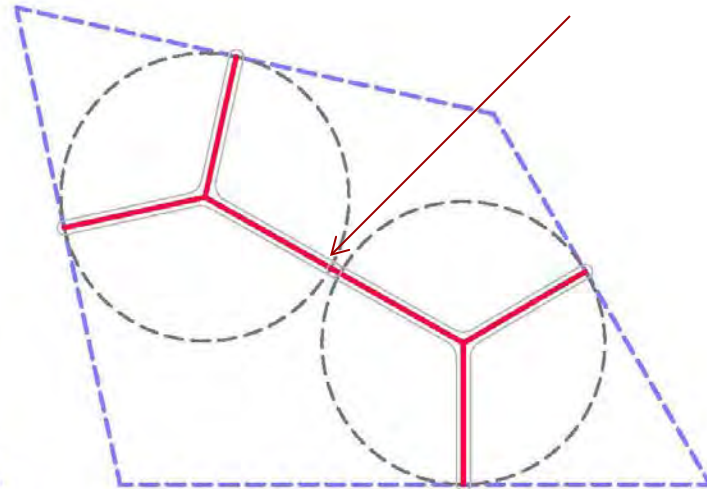
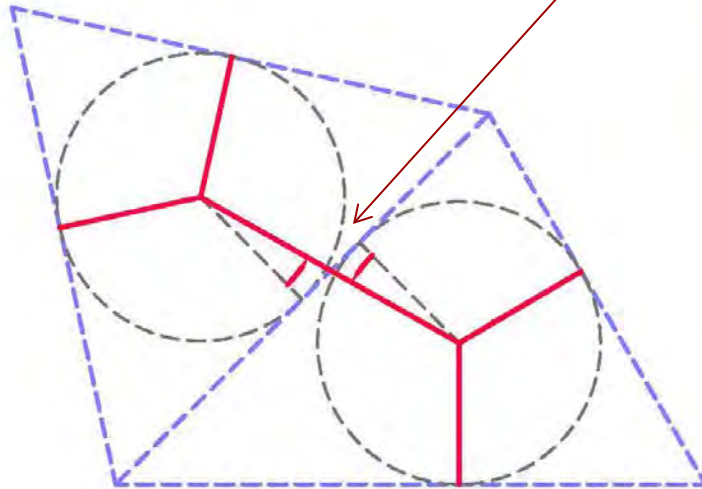
Draw lines orthogonal to edges that connect to center of tangent circle



General method for expanding quadrilateral (edges preserved)

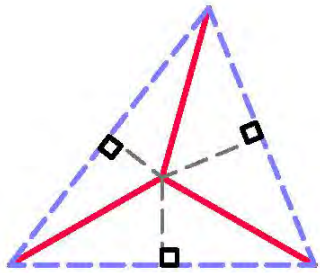
Divide quadrilateral into 2 triangles & connect
centers of tangent circles

Mid-point of connecting line

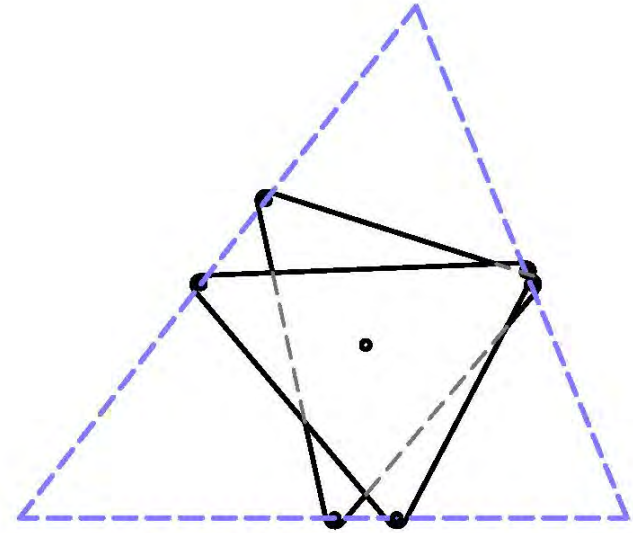
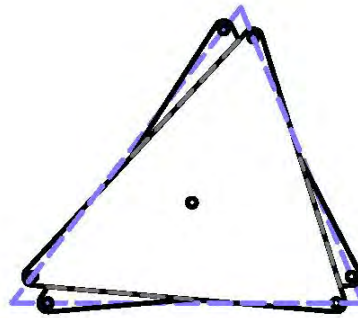
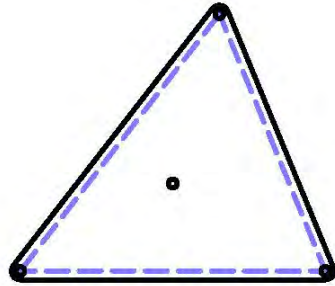


Alternate method for expanding triangle (edges preserved)

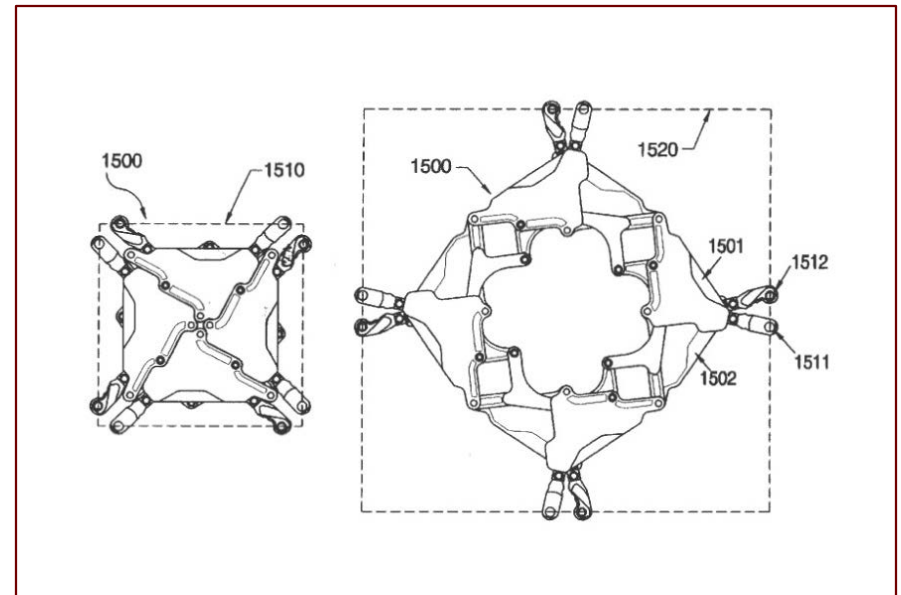
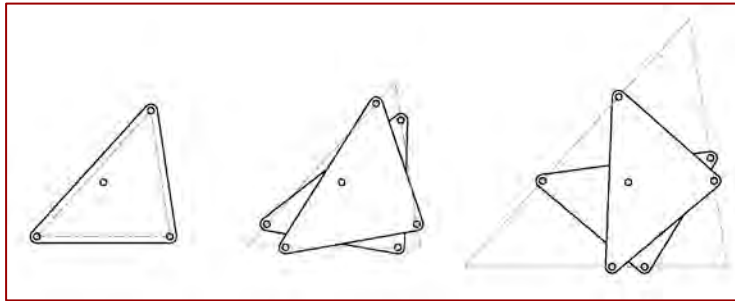
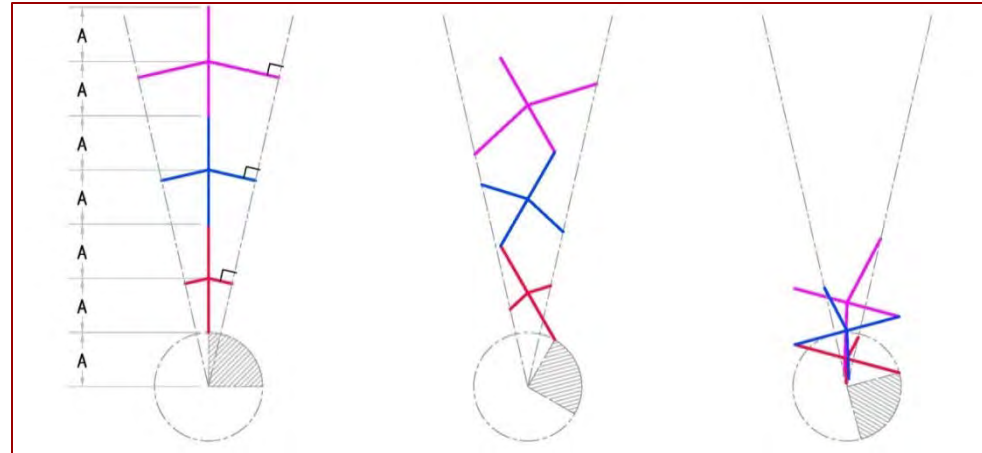
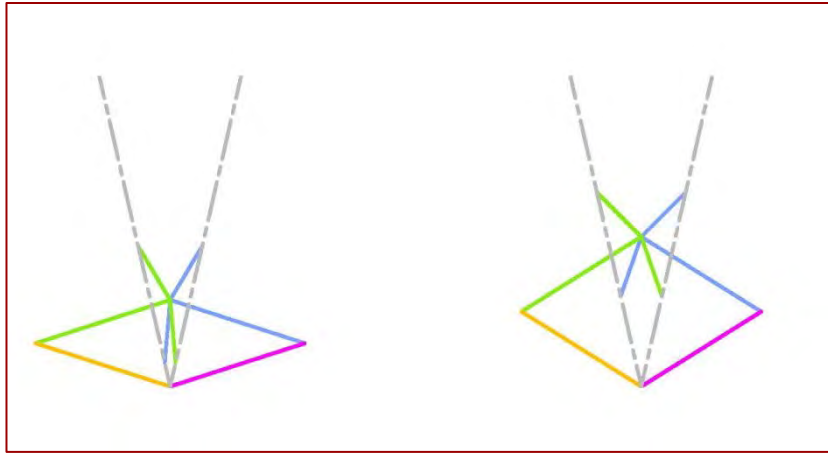
Draw lines orthogonal to edges to find center point



Construct link from Original triangle



Kinematic units



Constant angle perimeter linkages

Geometric construction - wheel

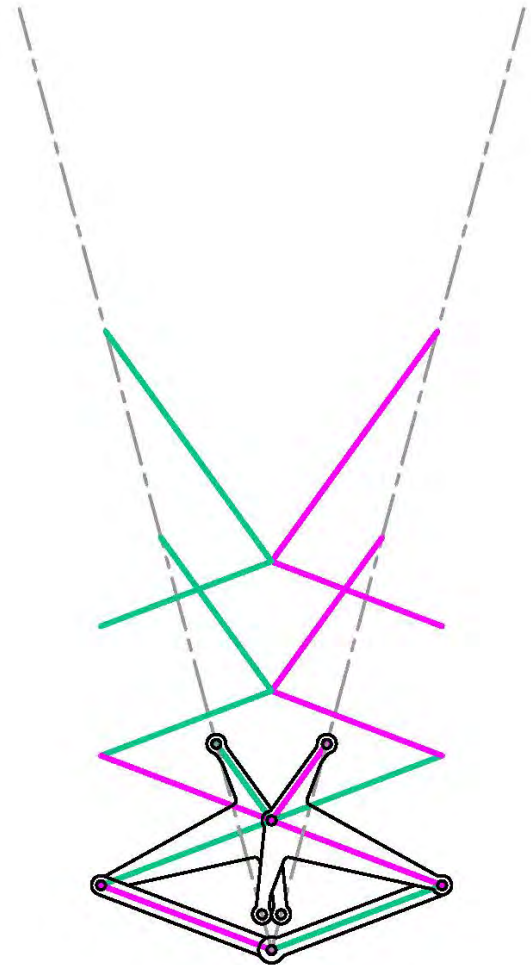
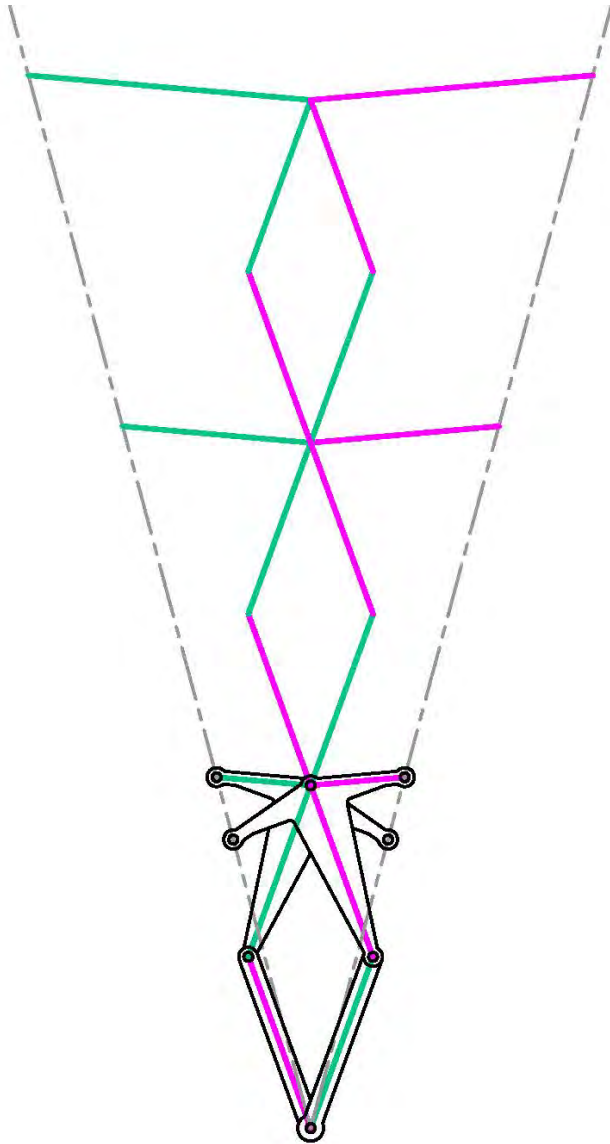


scissor
element



Scissor / spoke
element

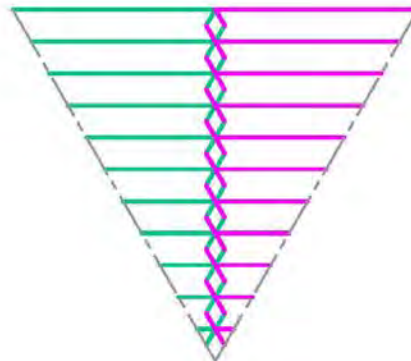
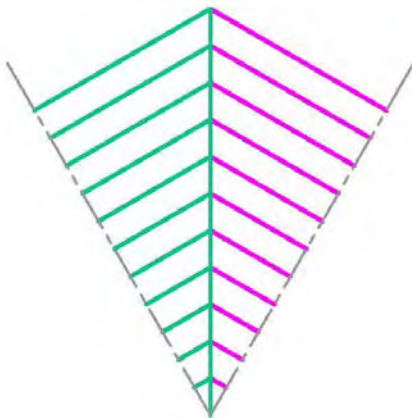
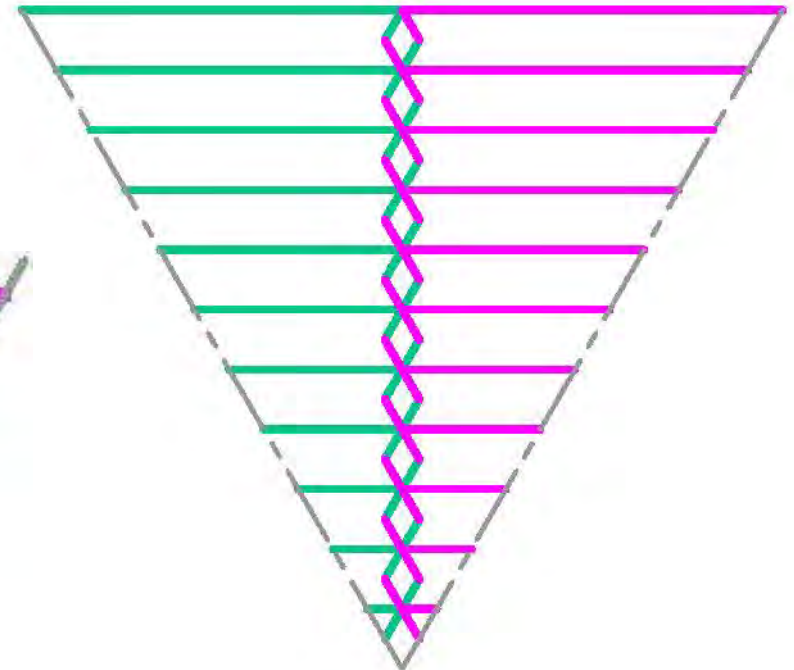
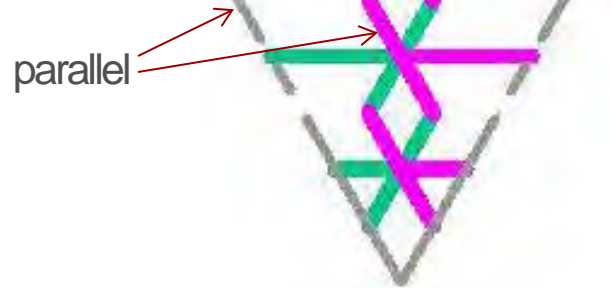
Tong linkage with points forming constant angle



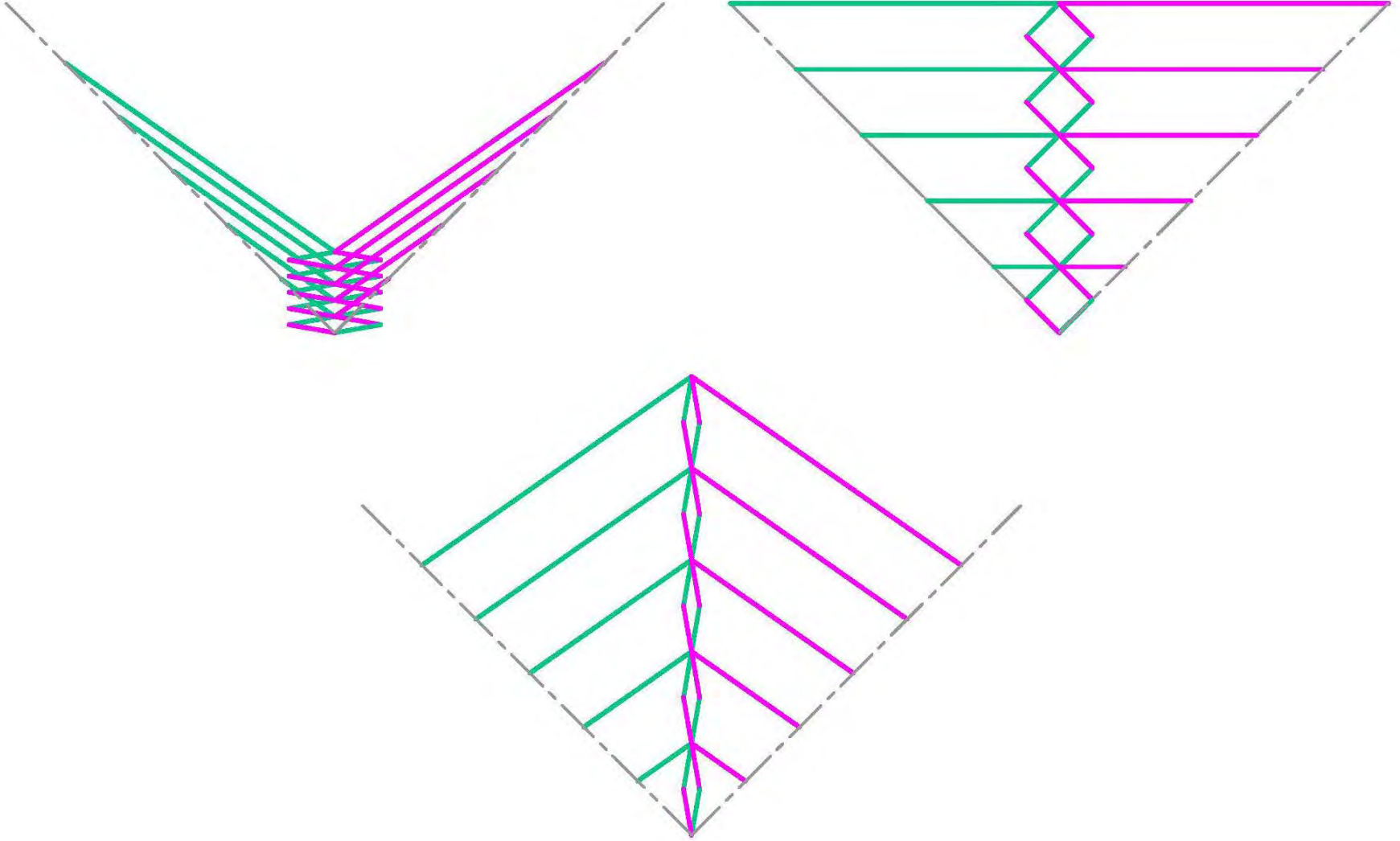
Tong linkage with points forming constant angle

Construction method:

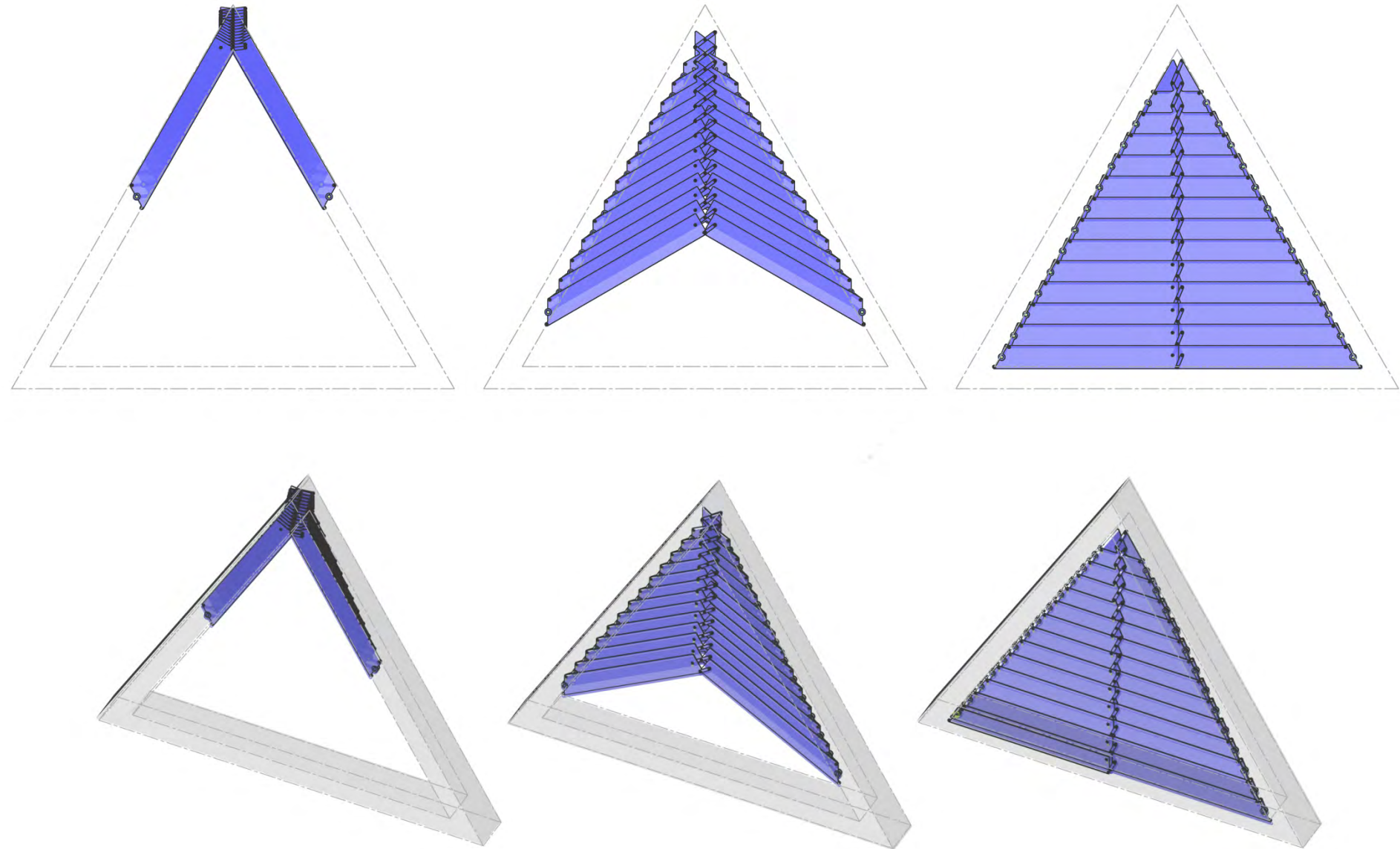
- Set tong linkage with deployment angle parallel to perimeter
- Draw lines (orthogonal to main axis of tong) from crossing points to perimeter lines
- Form links with 3 pivots as indicated

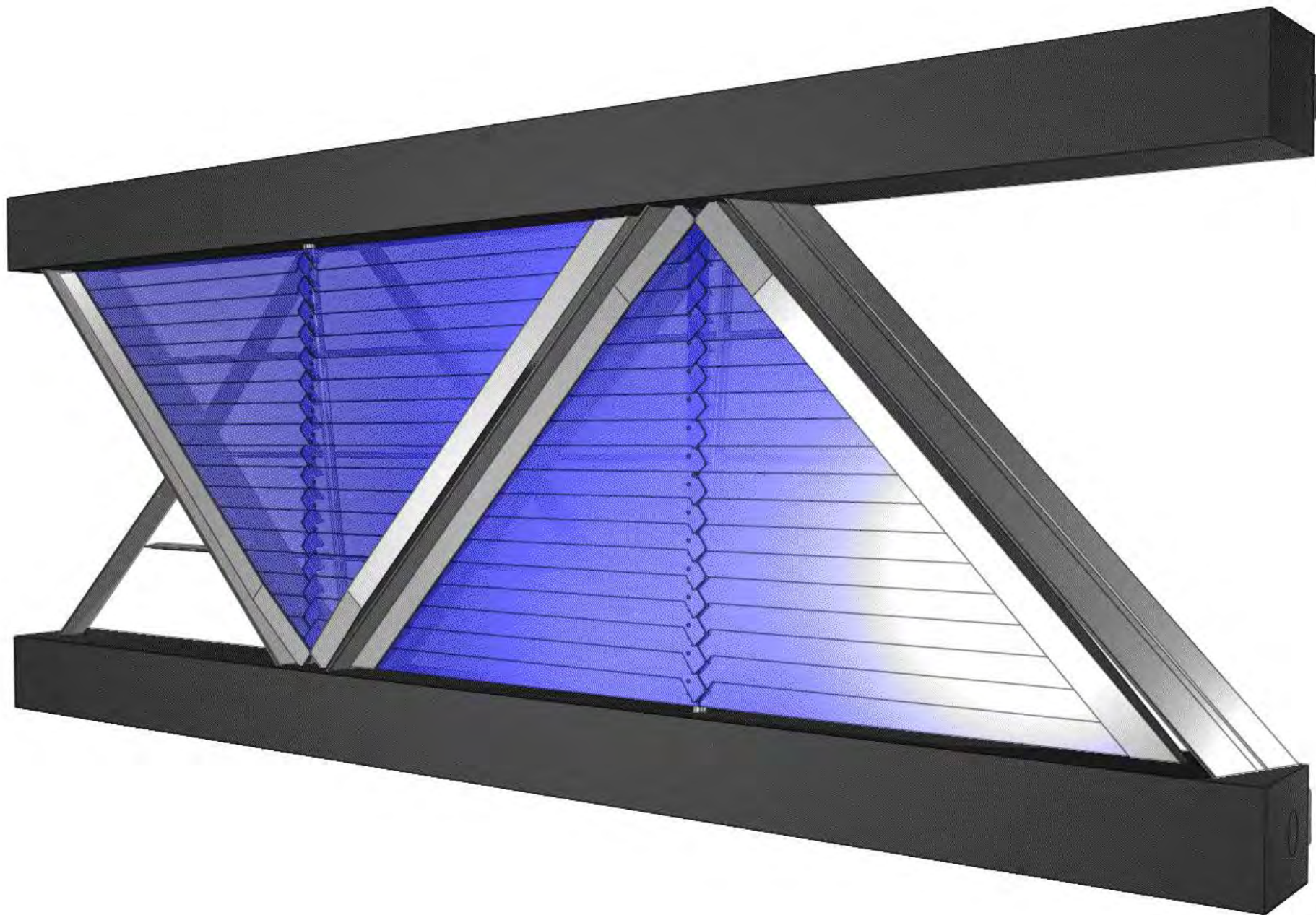


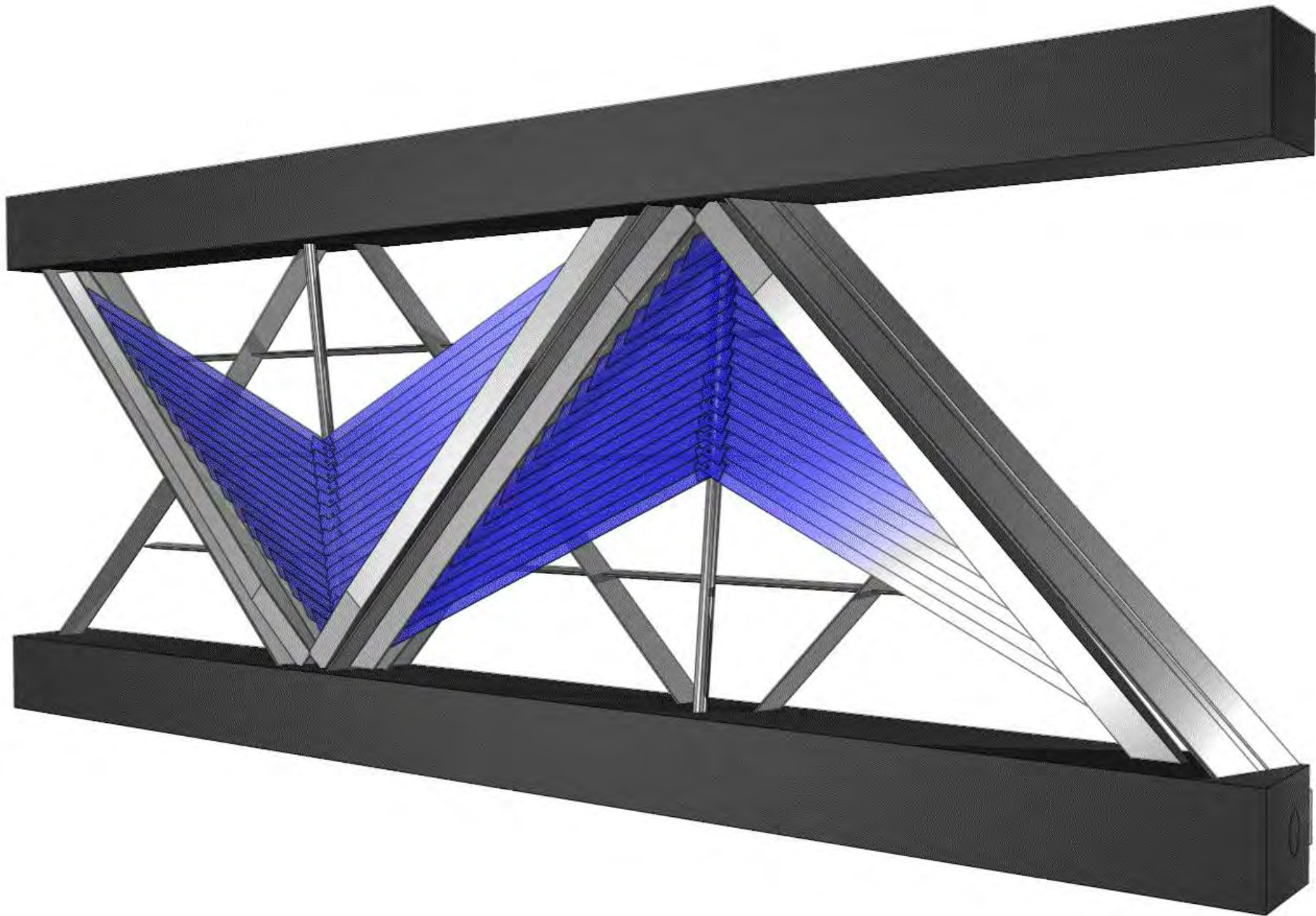
Scissor with perimeter of constant angle



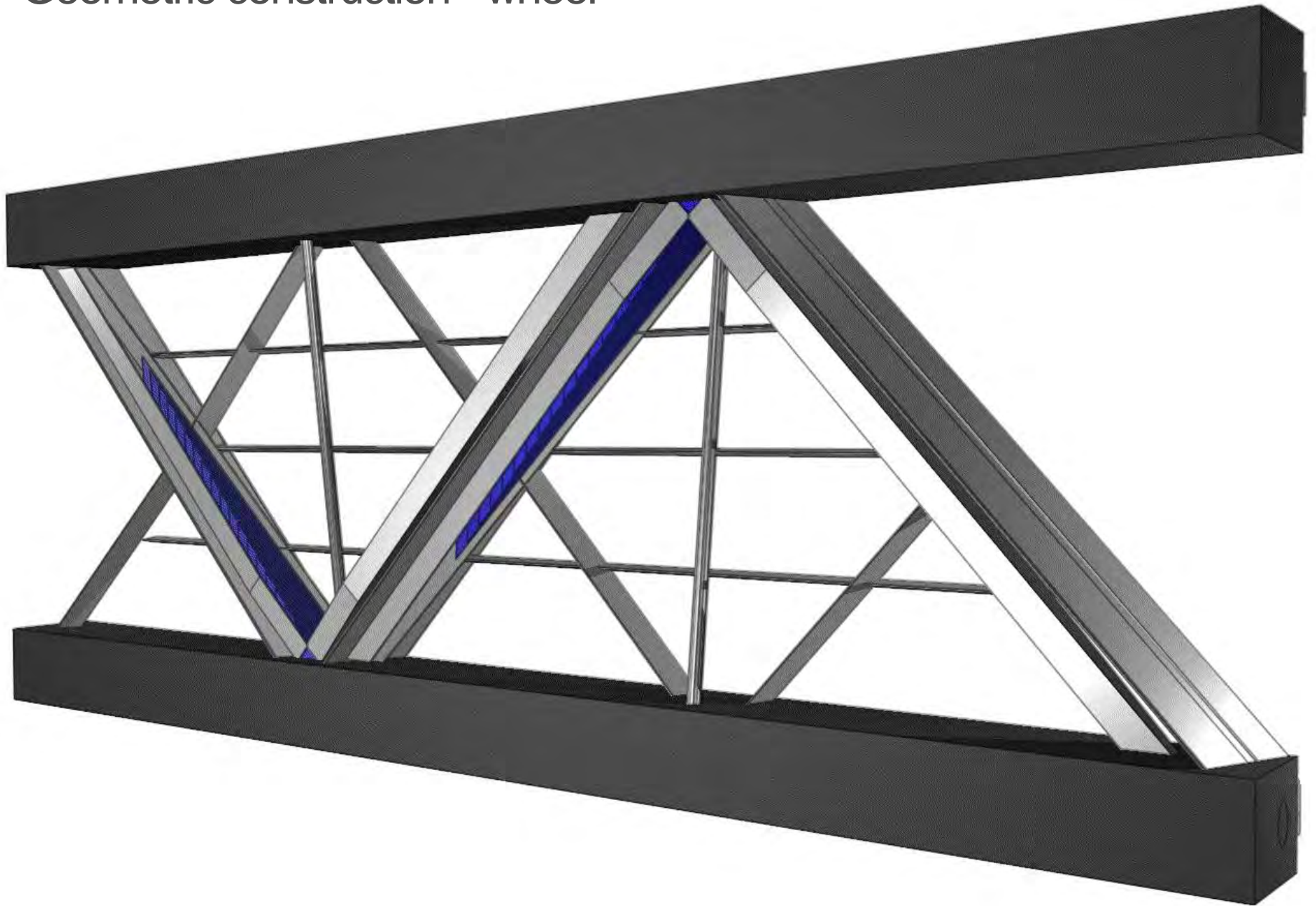
Scissor with perimeter of constant angle







Geometric construction - wheel





Building Programmable Matter

Daniela Rus
CSAIL, MIT

B. An, E. Demaine, C. Detweiler, K. Gilpin, K. Kotay,

M. Schwager, M. Vona, R. Wood, S-K. Yun

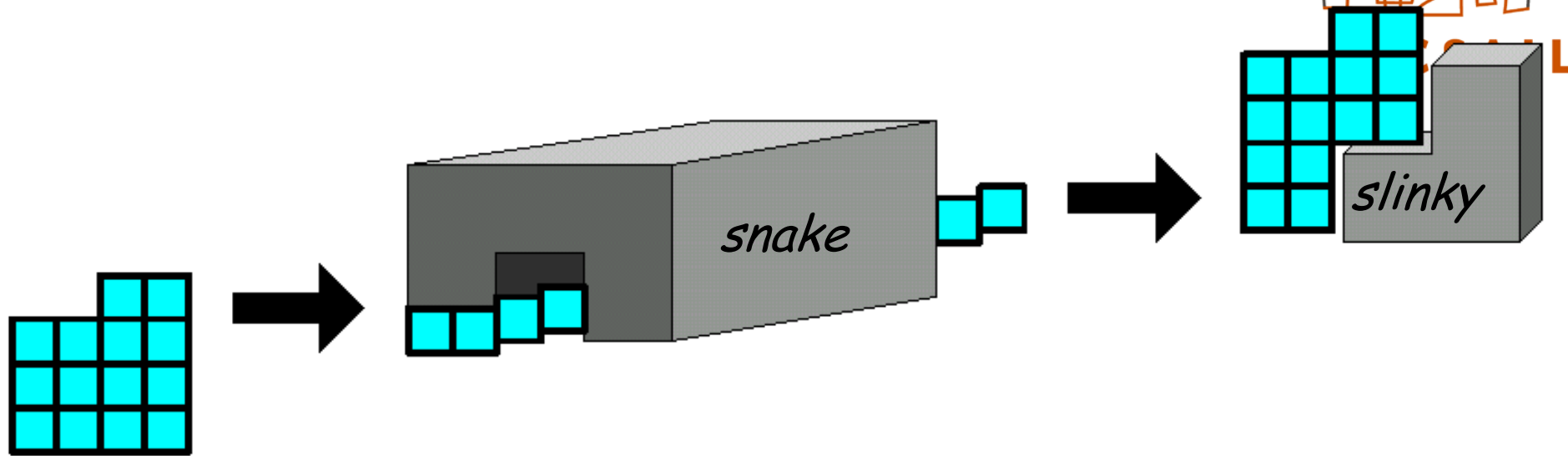
2/25/2013

Convergence of Materials and Machines

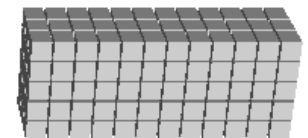
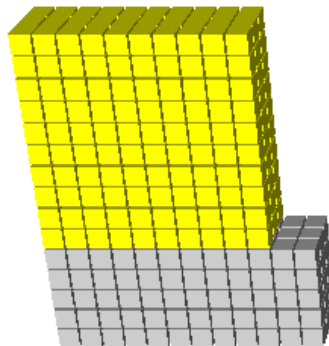


- *Great progress in materials*
- *Machines are increasingly more powerful and smaller*
 - *Convergence of machines and material*

Self-reconfiguring machines



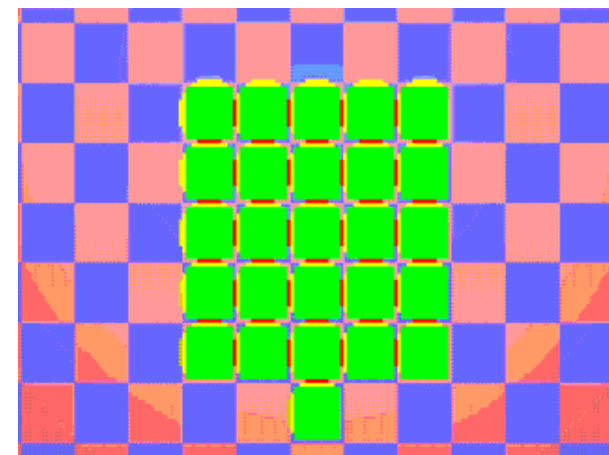
- *Multiple modules*
- *Physically connected*
- *Autonomous structural change*
- *Multiple functionalities--reusable*
- *Robots with variable architecture*
- *Self-assembly*
- *Self-reconfiguration*
- *Self-repair*



Actuation by Scaling: Crystal Module (1999)



- *Unit-compressible*
- *Self-contained units*
 - Computation
 - Communication
 - Power
- *28 built*
- *Local comm*
- *~ 200 g*

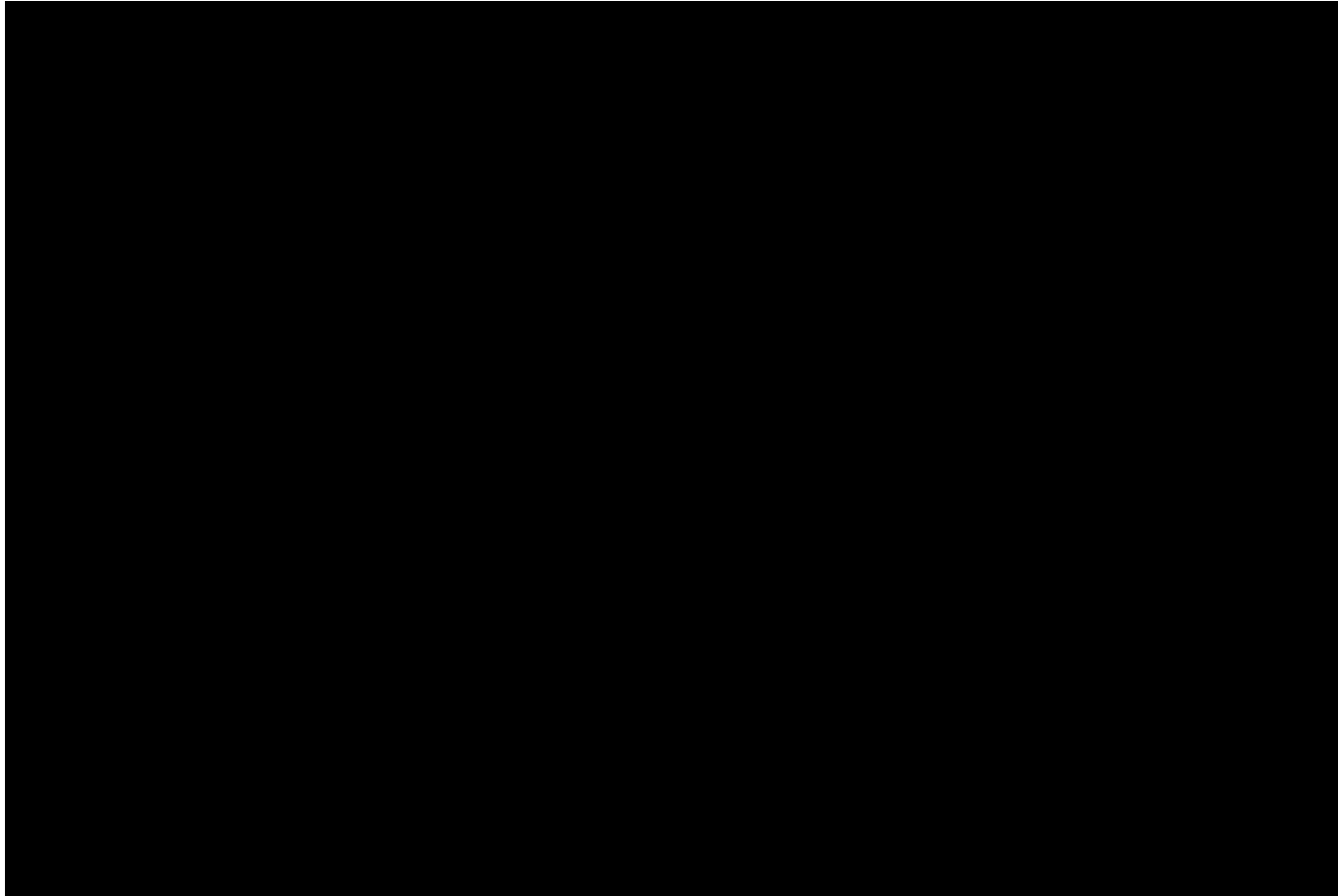


module relocation $O(1)$

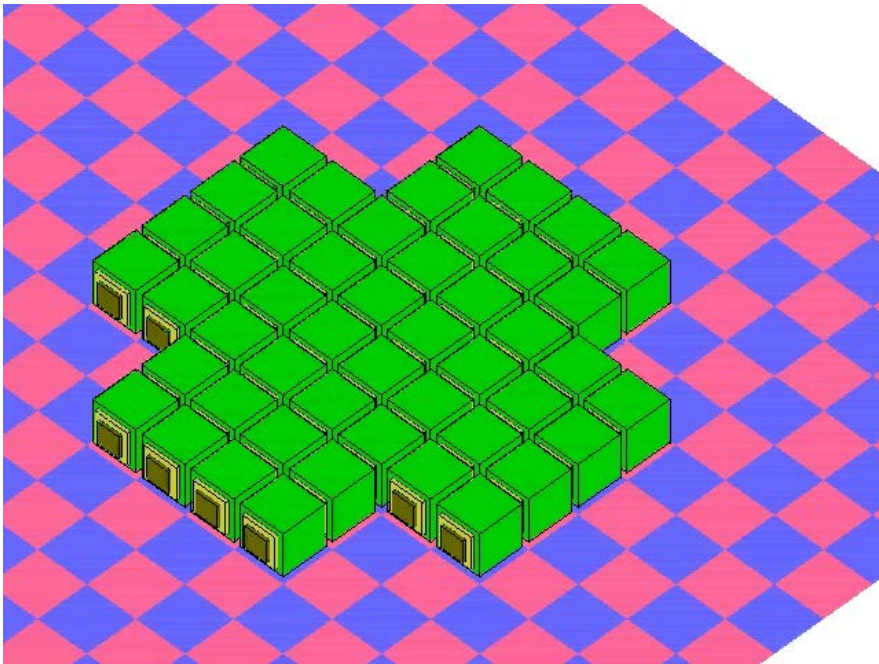
Computing Challenges:

- Self-reconfiguration (SR) planning when modules can travel through the volume of the structure (not just on the surface)
- Defining the class of achievable structures, defining force/torque requirements
- Scalability: Parallelism and Decentralization

Group Locomotion

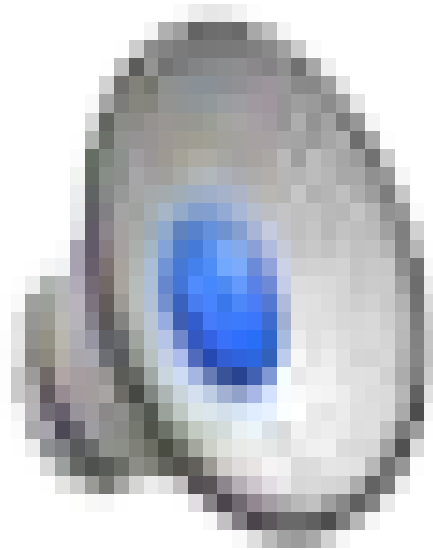


Distributed Reconfiguration Planning



- **Provably correct**
- **Distributed matching on difference between start and goal**
- **No deadlock**
- **Maximal parallelism**
- **Relies on actuation by scaling**

The Umbrella Project



Crystalline Theory

[Aloupis, Collette, Damian, Demaine, El-Khechen, Flatland, Langerman, O'Rourke, Pinciu, Ramaswami, Sacristán, Wuhler 2007–2009]

- Algorithms to morph n modules in 2D or 3D from one configuration to any other (up to constant resolution) using
 - $O(n)$ moves
 - $O(\log n)$ time (rounds)*
- With constant-strength robots:
 - $O(n^2)$ moves
 - $O(n)$ time (rounds)

simulation

simulation

*currently only in 2D, $O(n \lg n)$ moves, not in place