6.869

Computer Vision and Applications

Prof. Bill Freeman

Tracking

- Density propagation
- Linear Dynamic models / Kalman filter
- Data association
- Multiple models

Readings: F&P Ch 17

Huttenlocher talk

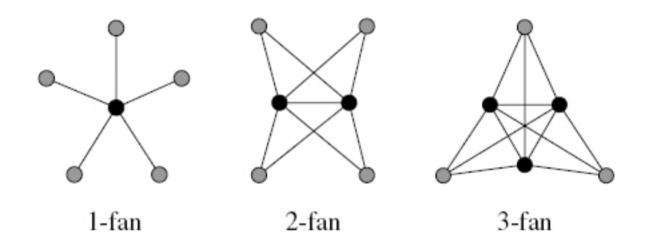


Figure 1. Some k-fans on 6 nodes. The reference nodes are shown in black while the regular nodes are shown in gray.

Huttenlocher talk

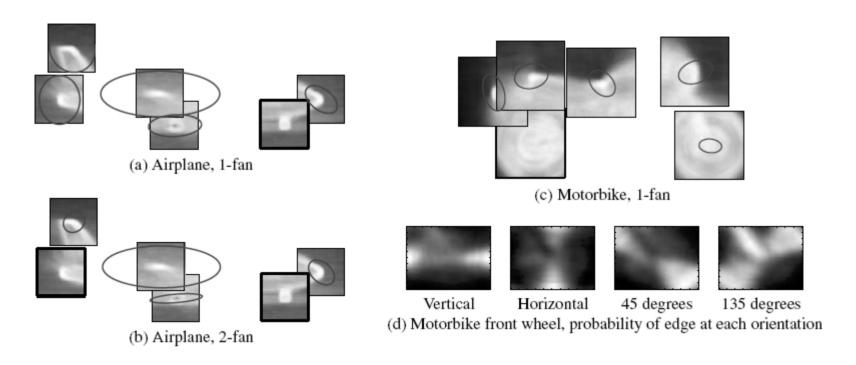


Figure 2. Illustration of some of the learned models. Images (a) through (c) show part appearance models positioned at their mean configuration. The reference parts have a black border around them. The ellipses illustrate the location variances for a non-reference part given the locations of the references. High intensity pixels represent high edge probabilities. For clarity, just the probability of an edge is shown, although the actual models capture probabilities of each individual edge orientation. In (d), the probability map template for each edge orientation is shown for a sample part (the front wheel of the motorbike model). Note how the locations of parts in the 2-fan airplane model are more constrained than in the 1-fan model.

Huttenlocher talk



Figure 4. Sample localization results. In each of these cases all parts were localized correctly.

Schedule

- Thursday, April 28:
 - Kalman filter, PS4 due.
- Tuesday, May 3:
 - Tracking articulated objects, Exam 2 out
- Thursday, May 5:
 - How to write papers & give talks, Exam 2 due
- Tuesday, May 10:
 - Motion microscopy, separating shading and paint ("fun things my group is doing")
- Thursday, May 12:
 - 5-10 min. student project presentations, projects due.

Tracking Applications

- Motion capture
- Recognition from motion
- Surveillance
- Targeting

Things to consider in tracking

What are the

- Real world dynamics
- Approximate / assumed model
- Observation / measurement process

Density propogation

- Tracking == Inference over time
- Much simplification is possible with linear dynamics and Gaussian probability models

Outline

- Recursive filters
- State abstraction
- Density propagation
- Linear Dynamic models / Kalman filter
- Data association
- Multiple models

Tracking and Recursive estimation

- Real-time / interactive imperative.
- Task: At each time point, re-compute estimate of position or pose.
 - At time n, fit model to data using time 0...n
 - At time n+1, fit model to data using time 0...n+1
- Repeat batch fit every time?

Recursive estimation

- Decompose estimation problem
 - part that depends on new observation
 - part that can be computed from previous history

• E.g., running average:

$$\mathbf{a}_{\mathsf{t}} = \alpha \ \mathbf{a}_{\mathsf{t-1}} + (1-\alpha) \ \mathbf{y}_{\mathsf{t}}$$

- Linear Gaussian models: Kalman Filter
- First, general framework...

Tracking

• Very general model:

- We assume there are moving objects, which have an underlying state X
- There are measurements Y, some of which are functions of this state
- There is a clock
 - at each tick, the state changes
 - at each tick, we get a new observation

Examples

- object is ball, state is 3D position+velocity, measurements are stereo pairs
- object is person, state is body configuration, measurements are frames, clock is in camera (30 fps)

Three main issues in tracking

- **Prediction:** we have seen y_0, \ldots, y_{i-1} what state does this set of measurements predict for the *i*'th frame? to solve this problem, we need to obtain a representation of $P(X_i|Y_0=y_0,\ldots,Y_{i-1}=y_{i-1})$.
- Data association: Some of the measurements obtained from the *i*-th frame may tell us about the object's state. Typically, we use $P(X_i|Y_0 = y_0, ..., Y_{i-1} = y_{i-1})$ to identify these measurements.
- Correction: now that we have y_i the relevant measurements we need to compute a representation of $P(X_i|Y_0=y_0,\ldots,Y_i=y_i)$.

Simplifying Assumptions

• Only the immediate past matters: formally, we require

$$P(X_i|X_1,...,X_{i-1}) = P(X_i|X_{i-1})$$

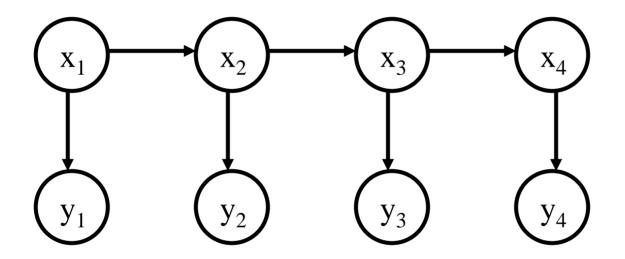
This assumption hugely simplifies the design of algorithms, as we shall see; furthermore, it isn't terribly restrictive if we're clever about interpreting X_i as we shall show in the next section.

• Measurements depend only on the current state: we assume that Y_i is conditionally independent of all other measurements given X_i . This means that

$$P(\boldsymbol{Y}_i, \boldsymbol{Y}_j, \dots \boldsymbol{Y}_k | \boldsymbol{X}_i) = P(\boldsymbol{Y}_i | \boldsymbol{X}_i) P(\boldsymbol{Y}_j, \dots, \boldsymbol{Y}_k | \boldsymbol{X}_i)$$

Again, this isn't a particularly restrictive or controversial assumption, but it yields important simplifications.

Kalman filter graphical model



Tracking as induction

- Assume data association is done
 - we'll talk about this later; a dangerous assumption
- Do correction for the 0'th frame
- Assume we have corrected estimate for i'th frame
 - show we can do prediction for i+1, correction for i+1

Base case

Firstly, we assume that we have $P(X_0)$

$$P(\mathbf{X}_0|\mathbf{Y}_0 = \mathbf{y}_0) = \frac{P(\mathbf{y}_0|\mathbf{X}_0)P(\mathbf{X}_0)}{P(\mathbf{y}_0)}$$

$$\propto P(\boldsymbol{y}_0|\boldsymbol{X}_0)P(\boldsymbol{X}_0)$$

Induction step

Prediction

Prediction involves representing

$$P(\boldsymbol{X}_i|\boldsymbol{y}_0,\ldots,\boldsymbol{y}_{i-1})$$

given

$$P(\boldsymbol{X}_{i-1}|\boldsymbol{y}_0,\ldots,\boldsymbol{y}_{i-1}).$$

Our independence assumptions make it possible to write

$$P(X_{i}|y_{0},...,y_{i-1}) = \int P(X_{i},X_{i-1}|y_{0},...,y_{i-1})dX_{i-1}$$

$$= \int P(X_{i}|X_{i-1},y_{0},...,y_{i-1})P(X_{i-1}|y_{0},...,y_{i-1})dX_{i-1}$$

$$= \int P(X_{i}|X_{i-1})P(X_{i-1}|y_{0},...,y_{i-1})dX_{i-1}$$

Update step

Correction

Correction involves obtaining a representation of

$$P(\boldsymbol{X}_i|\boldsymbol{y}_0,\ldots,\boldsymbol{y}_i)$$

given

$$P(\boldsymbol{X}_i|\boldsymbol{y}_0,\ldots,\boldsymbol{y}_{i-1})$$

Our independence assumptions make it possible to write

$$P(\boldsymbol{X}_{i}|\boldsymbol{y}_{0},...,\boldsymbol{y}_{i}) = \frac{P(\boldsymbol{X}_{i},\boldsymbol{y}_{0},...,\boldsymbol{y}_{i})}{P(\boldsymbol{y}_{0},...,\boldsymbol{y}_{i})}$$

$$= \frac{P(\boldsymbol{y}_{i}|\boldsymbol{X}_{i},\boldsymbol{y}_{0},...,\boldsymbol{y}_{i-1})P(\boldsymbol{X}_{i}|\boldsymbol{y}_{0},...,\boldsymbol{y}_{i-1})P(\boldsymbol{y}_{0},...,\boldsymbol{y}_{i-1})}{P(\boldsymbol{y}_{0},...,\boldsymbol{y}_{i})}$$

$$= P(\boldsymbol{y}_{i}|\boldsymbol{X}_{i})P(\boldsymbol{X}_{i}|\boldsymbol{y}_{0},...,\boldsymbol{y}_{i-1})\frac{P(\boldsymbol{y}_{0},...,\boldsymbol{y}_{i-1})}{P(\boldsymbol{y}_{0},...,\boldsymbol{y}_{i})}$$

$$= \frac{P(\boldsymbol{y}_{i}|\boldsymbol{X}_{i})P(\boldsymbol{X}_{i}|\boldsymbol{y}_{0},...,\boldsymbol{y}_{i-1})}{\int P(\boldsymbol{y}_{i}|\boldsymbol{X}_{i})P(\boldsymbol{X}_{i}|\boldsymbol{y}_{0},...,\boldsymbol{y}_{i-1})d\boldsymbol{X}_{i}}$$

Linear dynamic models

• A linear dynamic model has the form

$$\mathbf{x}_{i} = N(\mathbf{D}_{i-1}\mathbf{x}_{i-1}; \Sigma_{d_{i}})$$

$$\mathbf{y}_i = N(\mathbf{M}_i \mathbf{x}_i; \Sigma_{m_i})$$

• This is much, much more general than it looks, and extremely powerful

Examples

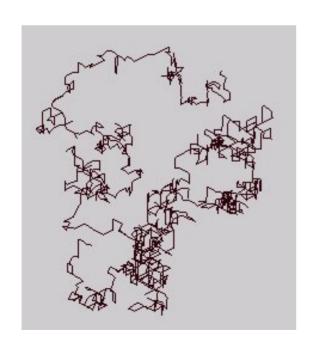
$$\mathbf{x}_{i} = N(\mathbf{D}_{i-1}\mathbf{x}_{i-1}; \Sigma_{d_{i}})$$

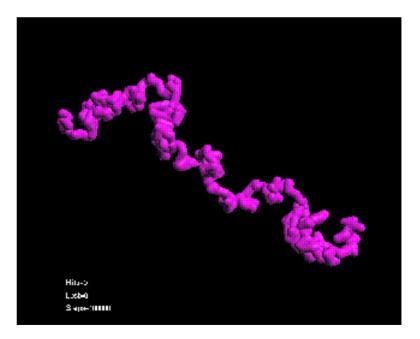
$$\mathbf{y}_i = N(\mathbf{M}_i \mathbf{x}_i; \Sigma_{m_i})$$

• Drifting points

 assume that the new position of the point is the old one, plus noise

$$\mathbf{D} = \mathbf{Id}$$





Constant velocity

$$\mathbf{x}_{i} = N(\mathbf{D}_{i-1}\mathbf{x}_{i-1}; \Sigma_{d_{i}})$$

$$\mathbf{y}_i = N(\mathbf{M}_i \mathbf{x}_i; \Sigma_{m_i})$$

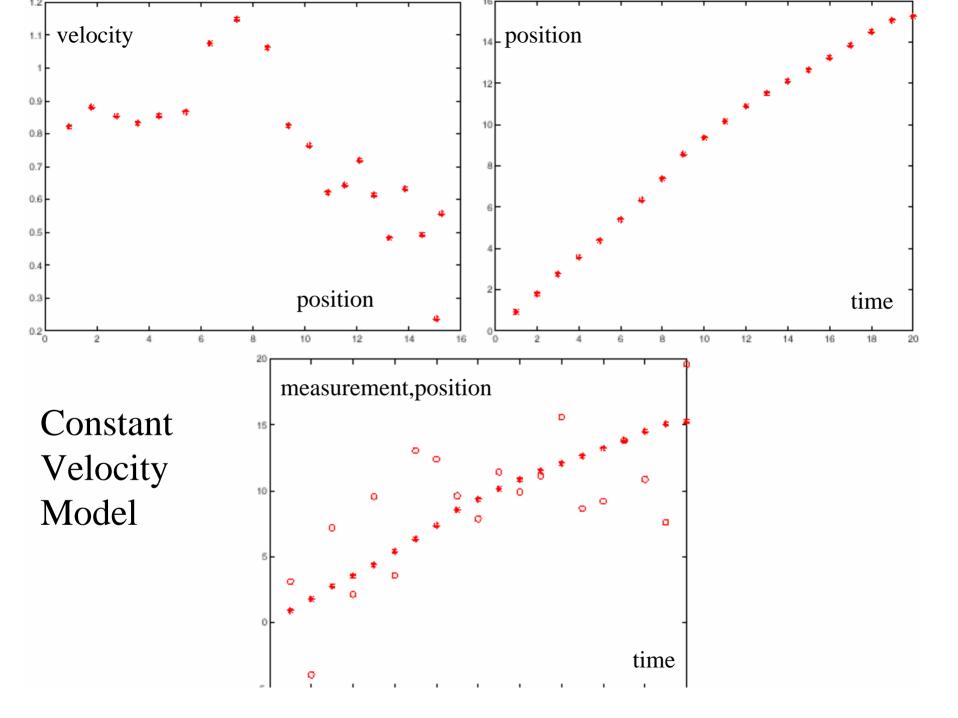
• We have

$$u_i = u_{i-1} + \Delta t v_{i-1} + \varepsilon_i$$
$$v_i = v_{i-1} + \zeta_i$$

- (the Greek letters denote noise terms)
- Stack (u, v) into a single state vector

$$\begin{pmatrix} u \\ v \end{pmatrix}_{i} = \begin{pmatrix} 1 & \Delta t \\ 0 & 1 \end{pmatrix} \begin{pmatrix} u \\ v \end{pmatrix}_{i-1} + \text{noise}$$

which is the form we had above



Constant acceleration

$$\mathbf{x}_{i} = N(\mathbf{D}_{i-1}\mathbf{x}_{i-1}; \Sigma_{d_{i}})$$

$$\mathbf{y}_i = N \Big(\mathbf{M}_i \mathbf{x}_i; \Sigma_{m_i} \Big)$$

We have

$$u_{i} = u_{i-1} + \Delta t v_{i-1} + \varepsilon_{i}$$

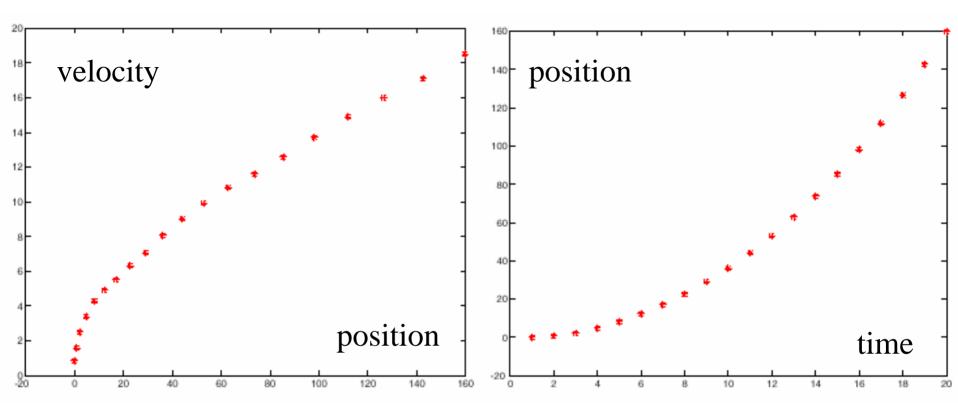
$$v_{i} = v_{i-1} + \Delta t a_{i-1} + \varsigma_{i}$$

$$a_{i} = a_{i-1} + \xi_{i}$$

- (the Greek letters denote noise terms)
- Stack (u, v) into a single state vector

$$\begin{pmatrix} u \\ v \\ a \end{pmatrix}_{i} = \begin{pmatrix} 1 & \Delta t & 0 \\ 0 & 1 & \Delta t \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} u \\ v \\ a \end{pmatrix}_{i-1} + \text{noise}$$

which is the form we had above



Constant Acceleration Model

Periodic motion

$$\mathbf{x}_{i} = N(\mathbf{D}_{i-1}\mathbf{x}_{i-1}; \Sigma_{d_{i}})$$

$$\mathbf{y}_{i} = N(\mathbf{M}_{i}\mathbf{x}_{i}; \Sigma_{m_{i}})$$

Assume we have a point, moving on a line with a periodic movement defined with a differential eq:

$$rac{d^2p}{dt^2} = -p$$

can be defined as

$$\frac{d\boldsymbol{u}}{dt} = \left(\begin{array}{cc} 0 & 1\\ -1 & 0 \end{array}\right) \boldsymbol{u} = \mathcal{S}\boldsymbol{u}$$

with state defined as stacked position and velocity u=(p, v)

Periodic motion

$$\mathbf{x}_{i} = N(\mathbf{D}_{i-1}\mathbf{x}_{i-1}; \Sigma_{d_{i}})$$

$$\mathbf{y}_i = N(\mathbf{M}_i \mathbf{x}_i; \Sigma_{m_i})$$

$$rac{doldsymbol{u}}{dt} = \left(egin{array}{cc} 0 & 1 \ -1 & 0 \end{array}
ight)oldsymbol{u} = \mathcal{S}oldsymbol{u}$$

Take discrete approximation....(e.g., forward Euler integration with ∆t stepsize.)

$$u_i = u_{i-1} + \Delta t \frac{du}{dt}$$

$$= u_{i-1} + \Delta t \mathcal{S} u_{i-1}$$

$$= \begin{pmatrix} 1 & \Delta t \\ -\Delta t & 1 \end{pmatrix} u_{i-1}$$

Higher order models

• Independence assumption

$$P(x_i|x_1,...,x_{i-1}) = P(x_i|x_{i-1}).$$

- Velocity and/or acceleration augmented position
- Constant velocity model equivalent to

$$P(p_i|p_1,...,p_{i-1}) = N(p_{i-1} + (p_{i-1} - p_{i-2}), \Sigma_{d_i})$$

- velocity == $p_{i-1} p_{i-2}$
- acceleration == $(p_{i-1} p_{i-2}) (p_{i-2} p_{i-3})$
- could also use p_{i-4} etc.

The Kalman Filter

• Key ideas:

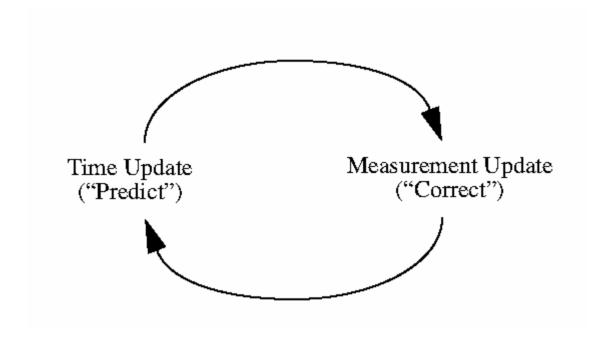
- Linear models interact uniquely well with Gaussian noise - make the prior Gaussian, everything else Gaussian and the calculations are easy
- Gaussians are really easy to represent --- once you know the mean and covariance, you're done

Recall the three main issues in tracking

- **Prediction:** we have seen y_0, \ldots, y_{i-1} what state does this set of measurements predict for the *i*'th frame? to solve this problem, we need to obtain a representation of $P(X_i|Y_0=y_0,\ldots,Y_{i-1}=y_{i-1})$.
- Data association: Some of the measurements obtained from the *i*-th frame may tell us about the object's state. Typically, we use $P(X_i|Y_0 = y_0, ..., Y_{i-1} = y_{i-1})$ to identify these measurements.
- Correction: now that we have y_i the relevant measurements we need to compute a representation of $P(X_i|Y_0=y_0,\ldots,Y_i=y_i)$.

(Ignore data association for now)

The Kalman Filter



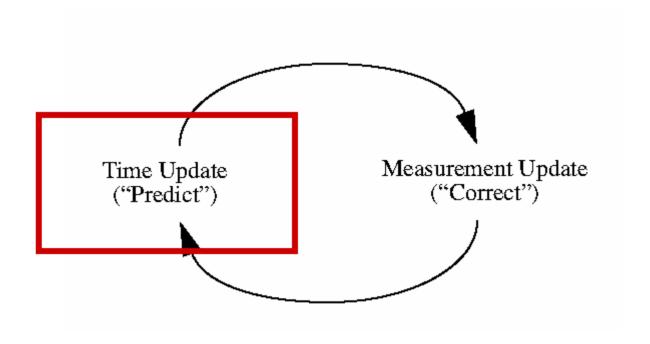
The Kalman Filter in 1D

 $x_i \sim N(d_i x_{i-1}, \sigma_{d_i}^2)$

Dynamic Model

• Notation $y_i \sim N(m_i x_i, \sigma_{m_i}^2)$ mean of $P(X_i | y_0, \dots, y_{i-1})$ as $\overline{X_i} \leftarrow$ Predicted mean mean of $P(X_i | y_0, \dots, y_i)$ as $\overline{X_i}^+ \leftarrow$ Corrected mean the standard deviation of $P(X_i | y_0, \dots, y_{i-1})$ as σ_i^- of $P(X_i | y_0, \dots, y_i)$ as σ_i^+

The Kalman Filter



Prediction for 1D Kalman filter

• The new state is obtained by

$$x_i \sim N(d_i x_{i-1}, \sigma_{d_i}^2)$$

- multiplying old state by known constant
- adding zero-mean noise

- Therefore, predicted mean for new state is
 - constant times mean for old state
- Old variance is normal random variable
 - variance is multiplied by square of constant
 - and variance of noise is added.

$$\overline{X}_{i}^{-} = d_{i} \overline{X}_{i-1}^{+} \qquad (\sigma_{i}^{-})^{2} = \sigma_{d_{i}}^{2} + (d_{i} \sigma_{i-1}^{+})^{2}$$

Dynamic Model:

$$x_i \sim N(d_i x_{i-1}, \sigma_{d_i})$$

$$y_i \sim N(m_i x_i, \sigma_{m_i})$$

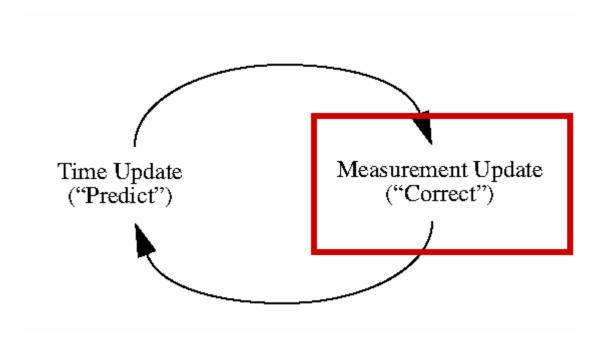
Start Assumptions: \overline{x}_0^- and σ_0^- are known

Update Equations: Prediction

$$\overline{x}_i^- = d_i \overline{x}_{i-1}^+$$

$$\sigma_i^-=\sqrt{\sigma_{d_i}^2+(d_i\sigma_{i-1}^+)^2}$$

The Kalman Filter



Correction for 1D Kalman filter

$$x_i^+ = \left(rac{\overline{x}_i^-\sigma_{m_i}^2 + m_i y_i (\sigma_i^-)^2}{\sigma_{m_i}^2 + m_i^2 (\sigma_i^-)^2}
ight)$$

$$\sigma_{i}^{+} = \sqrt{\frac{\sigma_{m_{i}}^{2}(\sigma_{i}^{-})^{2}}{(\sigma_{m_{i}}^{2} + m_{i}^{2}(\sigma_{i}^{-})^{2})}}$$

Notice:

- if measurement noise is small,
 we rely mainly on the measurement,
- if it's large, mainly on the prediction
- $-\sigma$ does not depend on y

Dynamic Model:

$$x_i \sim N(d_i x_{i-1}, \sigma_{d_i})$$

$$y_i \sim N(m_i x_i, \sigma_{m_i})$$

Start Assumptions: \overline{x}_0^- and σ_0^- are known

Update Equations: Prediction

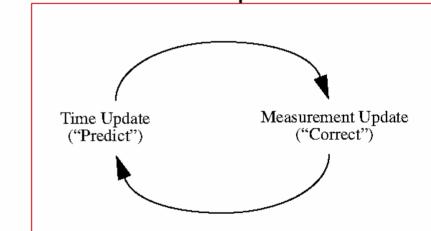
$$\overline{x}_i^- = d_i \overline{x}_{i-1}^+$$

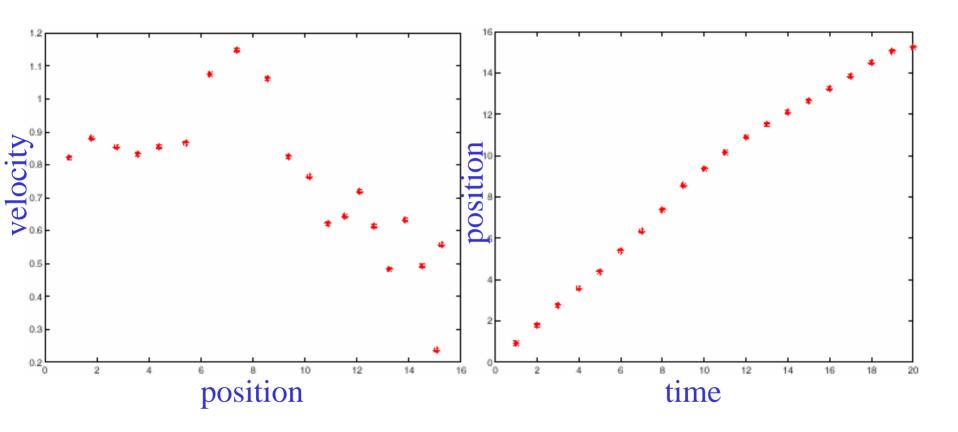
$$\sigma_i^-=\sqrt{\sigma_{d_i}^2+(d_i\sigma_{i-1}^+)^2}$$

Update Equations: Correction

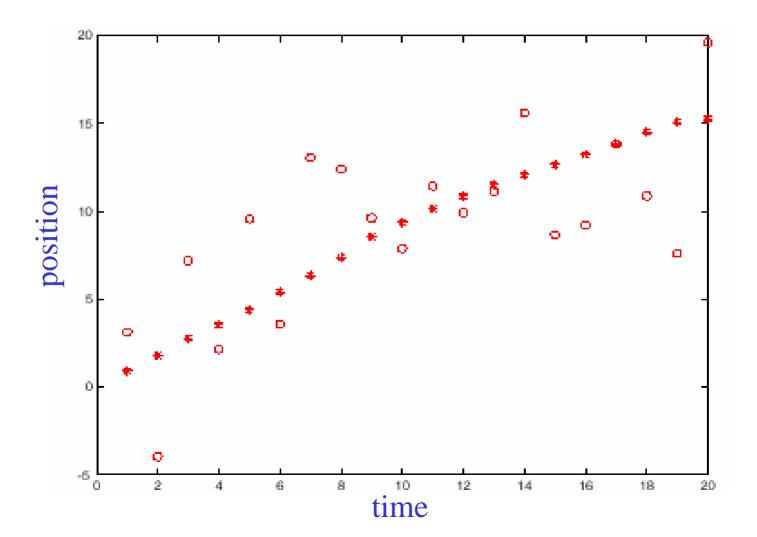
$$x_i^+ = \left(rac{\overline{x_i^-}\sigma_{m_i}^2 + m_i y_i (\sigma_i^-)^2}{\sigma_{m_i}^2 + m_i^2 (\sigma_i^-)^2}
ight)$$

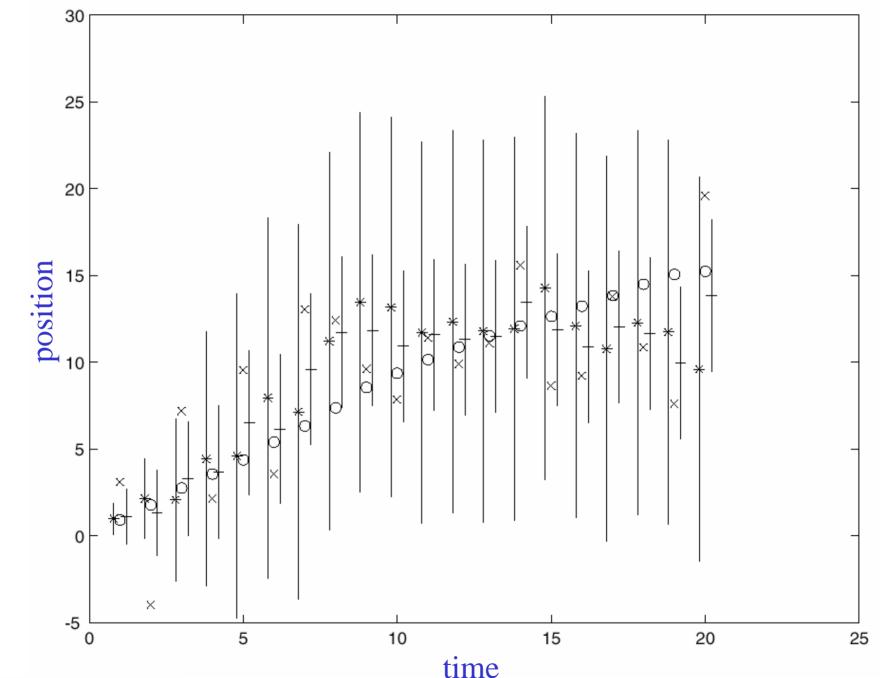
$$\sigma_{i}^{+} = \sqrt{ \left(rac{\sigma_{m_{i}}^{2}(\sigma_{i}^{-})^{2}}{(\sigma_{m_{i}}^{2} + m_{i}^{2}(\sigma_{i}^{-})^{2})}
ight) }$$



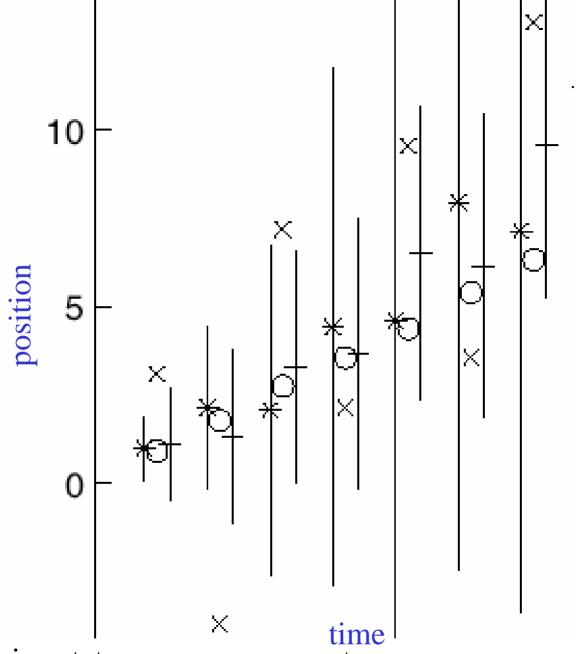


Constant Velocity Model





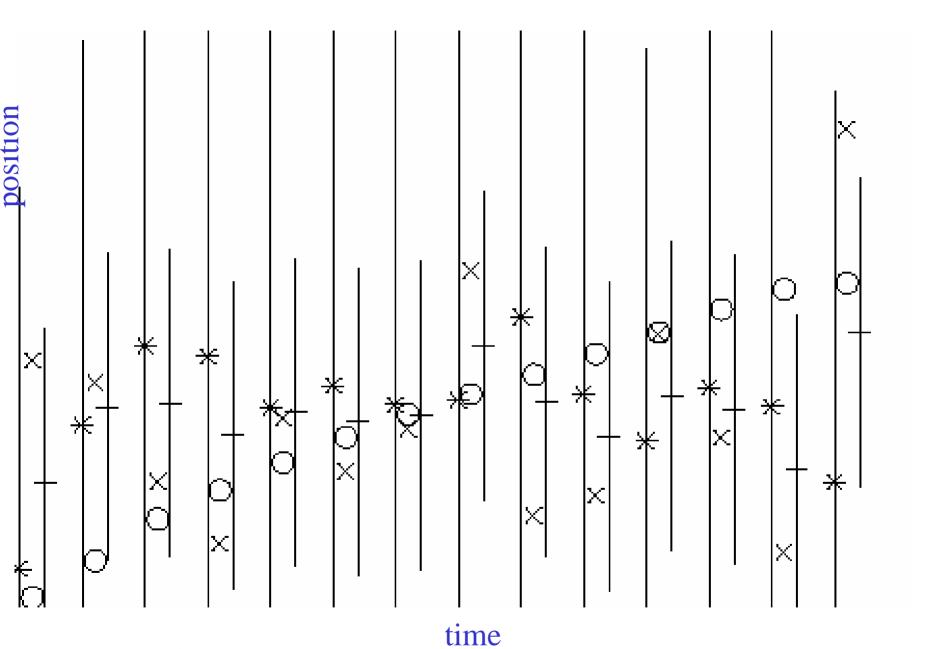
The *-s give \overline{x}_i^- , +-s give \overline{x}_i^+ , vertical bars are 3 standard deviation bars



The o-s give state, x-s measurement.

The *-s give \overline{x}_i^- , +-s give \overline{x}_i^+ , vertical bars are 3 standard deviation bars

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The o-s give state, x-s measurement.

The *-s give \overline{x}_i^- , +-s give \overline{x}_i^+ , vertical bars are 3 standard deviation bars

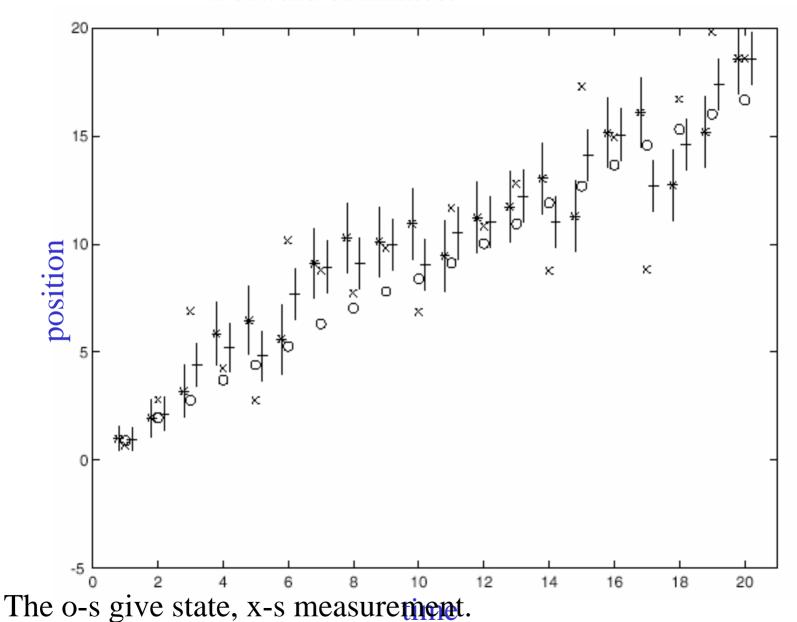
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Smoothing

• Idea

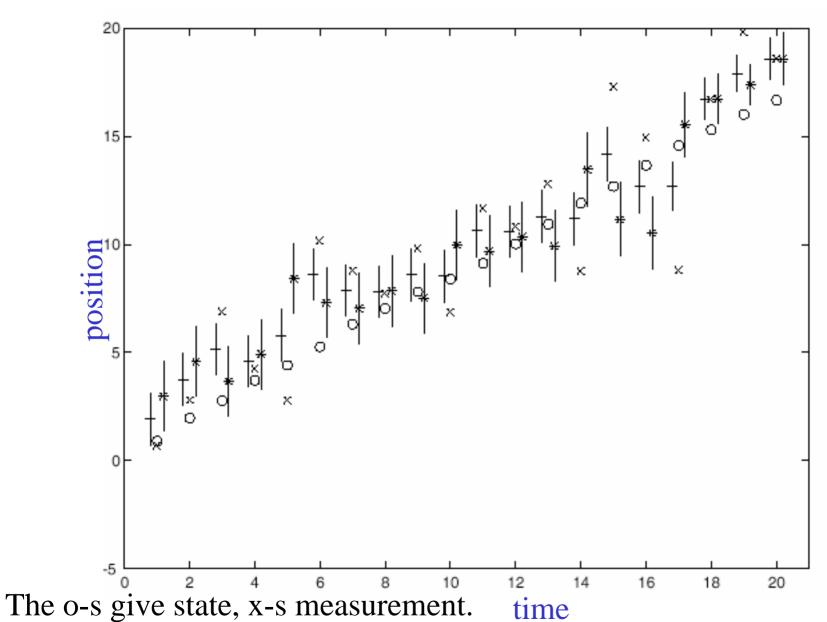
- We don't have the best estimate of state what about the future?
- Run two filters, one moving forward, the other backward in time.
- Now combine state estimates
 - The crucial point here is that we can obtain a smoothed estimate by viewing the backward filter's prediction as yet another measurement for the forward filter

Forward estimates.



The *-s give \overline{x}_i^- , +-s give \overline{x}_i^+ , vertical bars are 3 standard deviation bars

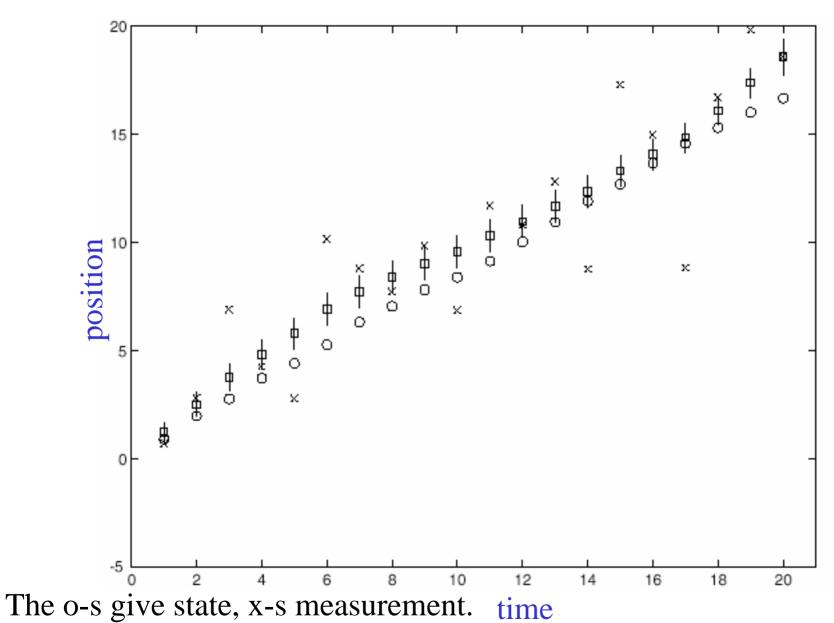
Backward estimates.



The *-s give \overline{x}_i^- , +-s give \overline{x}_i^+ , vertical bars are 3 standard deviation bars

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Combined forward-backward estimates.



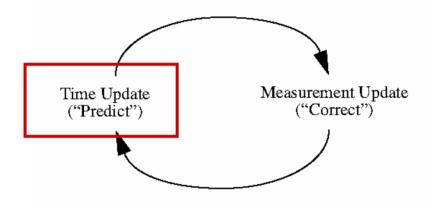
The o-s give state, x-s measurement. The *-s give \overline{x}_i^- , +-s give \overline{x}_i^+ , vertical bars are 3 standard deviation bars

n-D

Generalization to n-D is straightforward but more complex.

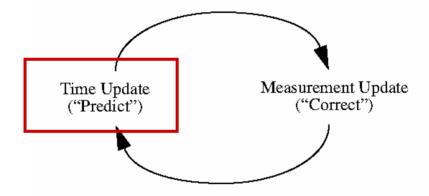
n-D

Generalization to n-D is straightforward but more complex.



n-D Prediction

Generalization to n-D is straightforward but more complex.



Prediction:

Multiply estimate at prior time with forward model:

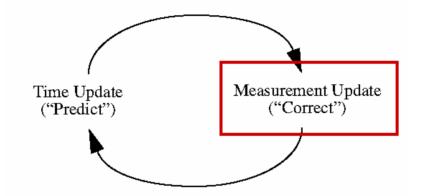
$$\overline{\boldsymbol{x}}_i^- = \mathcal{D}_i \overline{\boldsymbol{x}}_{i-1}^+$$

Propagate covariance through model and add new noise:

$$\Sigma_i^- = \Sigma_{d_i} + \mathcal{D}_i \sigma_{i-1}^+ \mathcal{D}_i$$

n-D Correction

Generalization to n-D is straightforward but more complex.



Correction:

• Update *a priori* estimate with measurement to form *a posteriori*

n-D correction

Find linear filter on innovations

$$\overline{\boldsymbol{x}}_{i}^{+} = \overline{\boldsymbol{x}}_{i}^{-} + \mathcal{K}_{i} \left[\boldsymbol{y}_{i} - \mathcal{M}_{i} \overline{\boldsymbol{x}}_{i}^{-} \right]$$

which minimizes a posteriori error covariance:

$$E\left[\left(x-\overline{x^{+}}\right)^{T}\left(x-\overline{x^{+}}\right)\right]$$

K is the Kalman Gain matrix. A solution is

$$\mathcal{K}_i = \Sigma_i^- \mathcal{M}_i^T \left[\mathcal{M}_i \Sigma_i^- \mathcal{M}_i^T + \Sigma_{m_i} \right]^{-1}$$

Kalman Gain Matrix

$$\overline{oldsymbol{x}}_{i}^{+} = \overline{oldsymbol{x}}_{i}^{-} + \mathcal{K}_{i} \left[oldsymbol{y}_{i} - \mathcal{M}_{i} \overline{oldsymbol{x}}_{i}^{-}
ight]$$

$$\mathcal{K}_{i} = \Sigma_{i}^{-} \mathcal{M}_{i}^{T} \left[\mathcal{M}_{i} \Sigma_{i}^{-} \mathcal{M}_{i}^{T} + \Sigma_{m_{i}} \right]^{-1}$$

As measurement becomes more reliable, K weights residual more heavily,

$$\lim_{\Sigma_m \to 0} K_i = M^{-1}$$

As prior covariance approaches 0, measurements are ignored:

$$\lim_{\Sigma_i^- \to 0} K_i = 0$$

Dynamic Model:

$$\boldsymbol{x}_i \sim N(\mathcal{D}_i \boldsymbol{x}_{i-1}, \Sigma_{d_i})$$

$$y_i \sim N(\mathcal{M}_i x_i, \Sigma_{m_i})$$

Start Assumptions: $\overline{\boldsymbol{x}}_0^-$ and Σ_0^- are known

Update Equations: Prediction

$$\overline{oldsymbol{x}}_i^- = \mathcal{D}_i \overline{oldsymbol{x}}_{i-1}^+$$

$$\Sigma_i^- = \Sigma_{d_i} + \mathcal{D}_i \sigma_{i-1}^+ \mathcal{D}_i$$

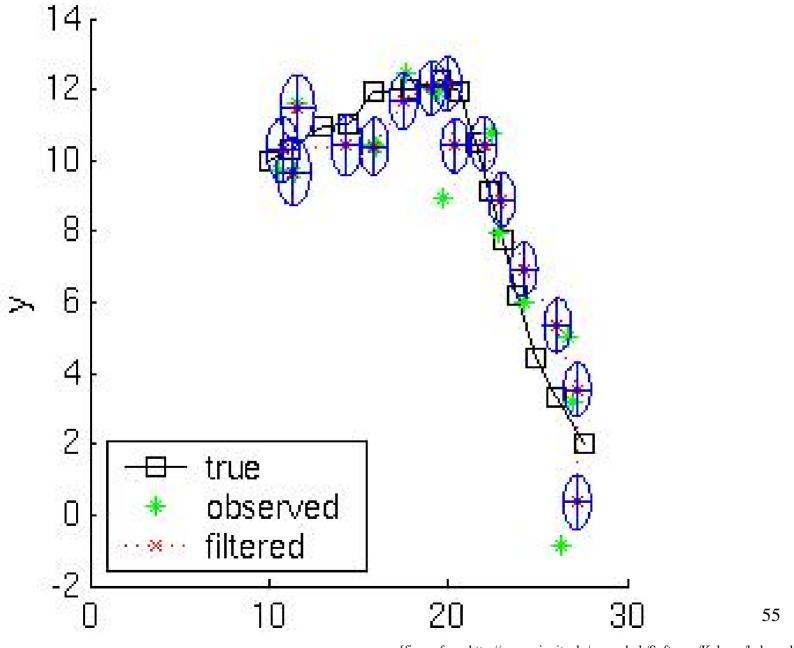
Update Equations: Correction

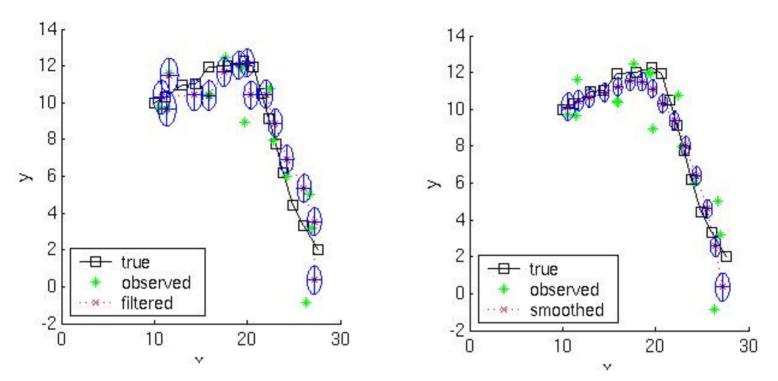
$$\mathcal{K}_i = \Sigma_i^- \mathcal{M}_i^T \left[\mathcal{M}_i \Sigma_i^- \mathcal{M}_i^T + \Sigma_{m_i} \right]^{-1}$$

$$oldsymbol{\overline{x}}_{i}^{+} = oldsymbol{\overline{x}}_{i}^{-} + \mathcal{K}_{i} \left[oldsymbol{y}_{i} - \mathcal{M}_{i} oldsymbol{\overline{x}}_{i}^{-}
ight]$$

$$\Sigma_i^+ = [Id - \mathcal{K}_i \mathcal{M}_i] \Sigma_i^-$$

2-D constant velocity example from Kevin Murphy's Matlab toolbox





- 2-D constant velocity example from Kevin Murphy's Matlab toolbox
- MSE of filtered estimate is 4.9; of smoothed estimate. 3.2.
- Not only is the smoothed estimate better, but we know that it is better, as illustrated by the smaller uncertainty ellipses
- Note how the smoothed ellipses are larger at the ends, because these points have seen less data.
- Also, note how rapidly the filtered ellipses reach their steady-state ("Ricatti") values.

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Data Association

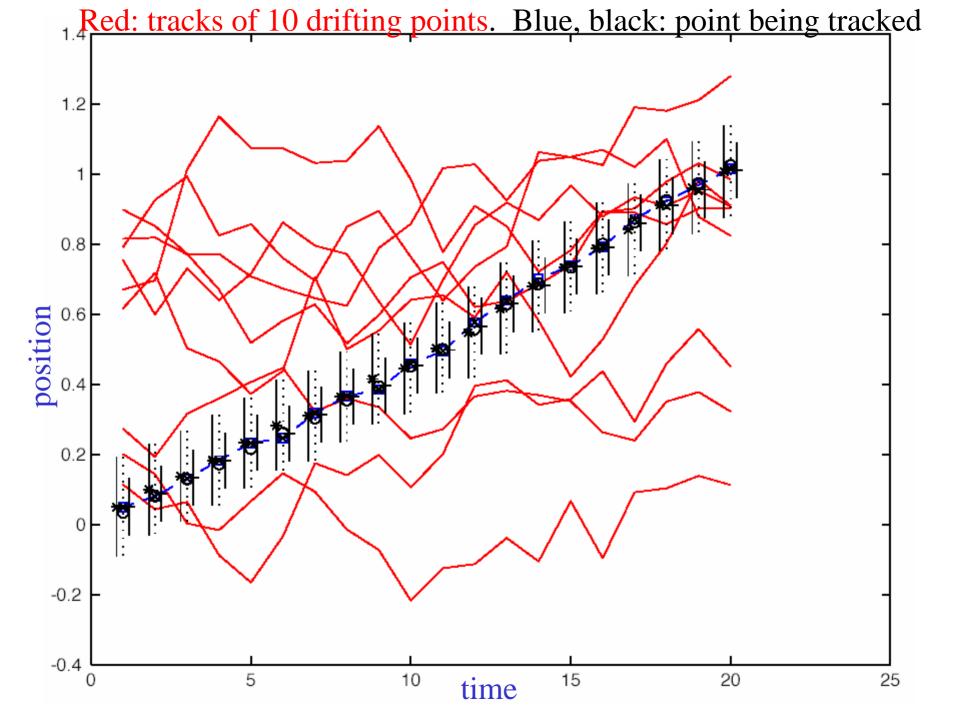
In real world y_i have clutter as well as data...

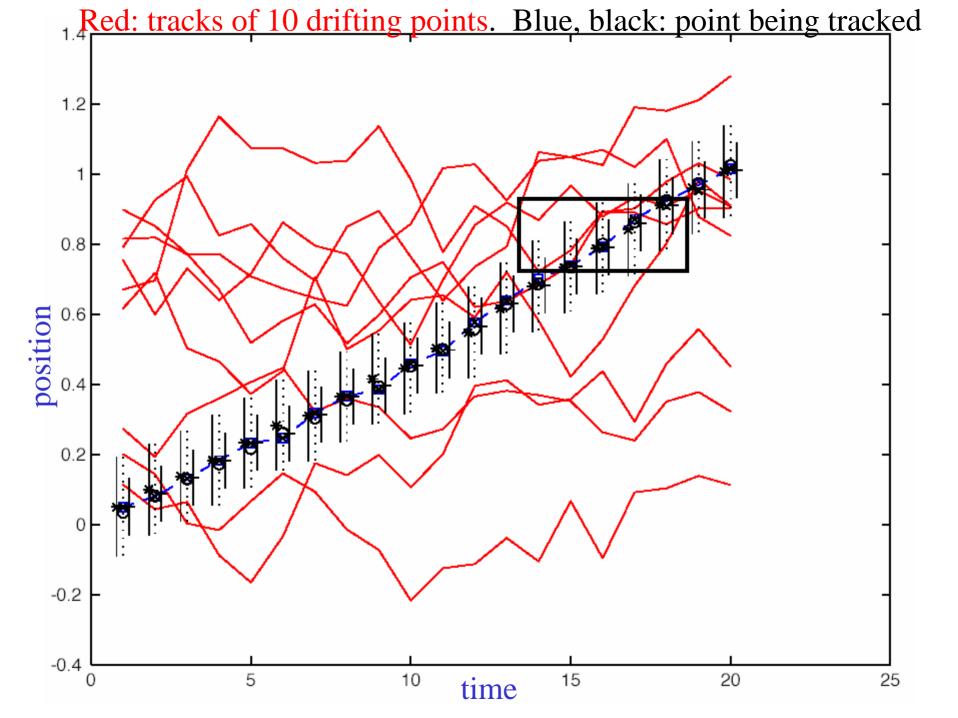
E.g., match radar returns to set of aircraft trajectories.

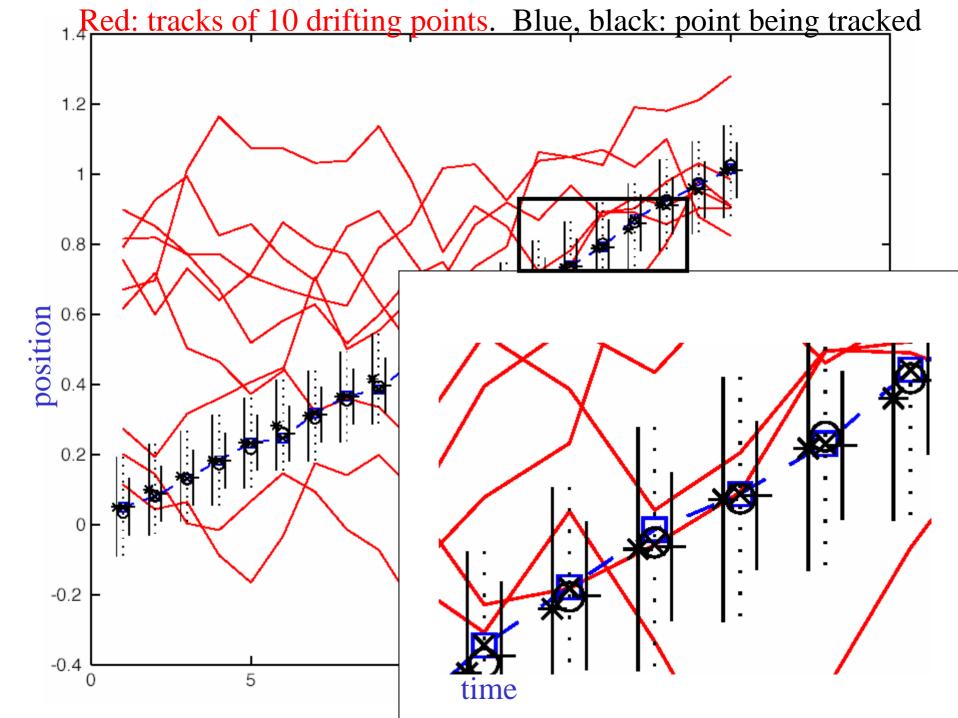
Data Association

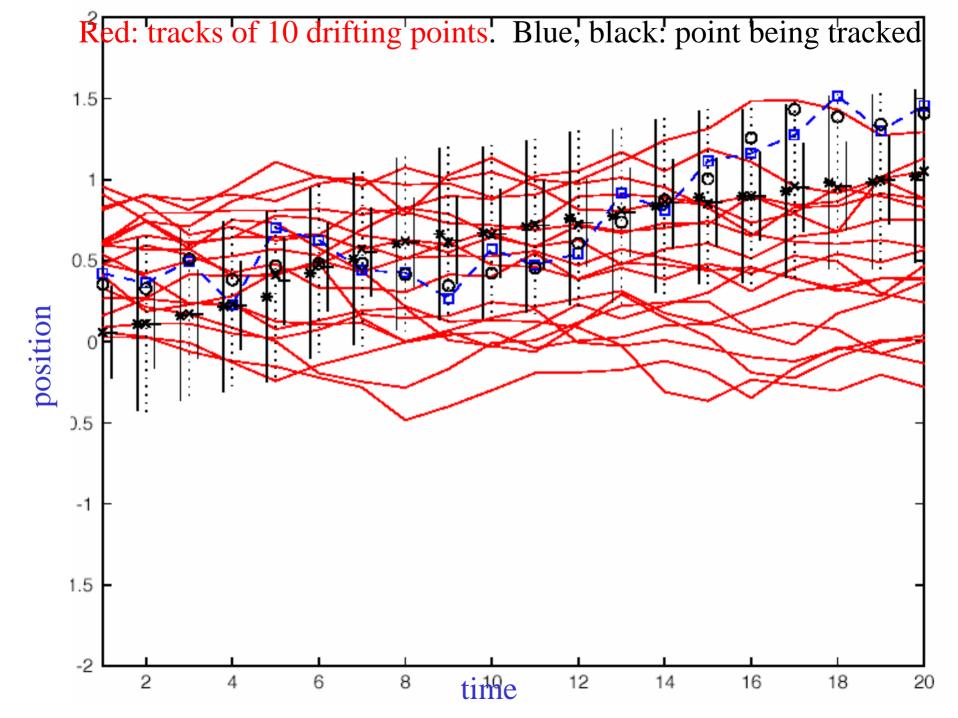
Approaches:

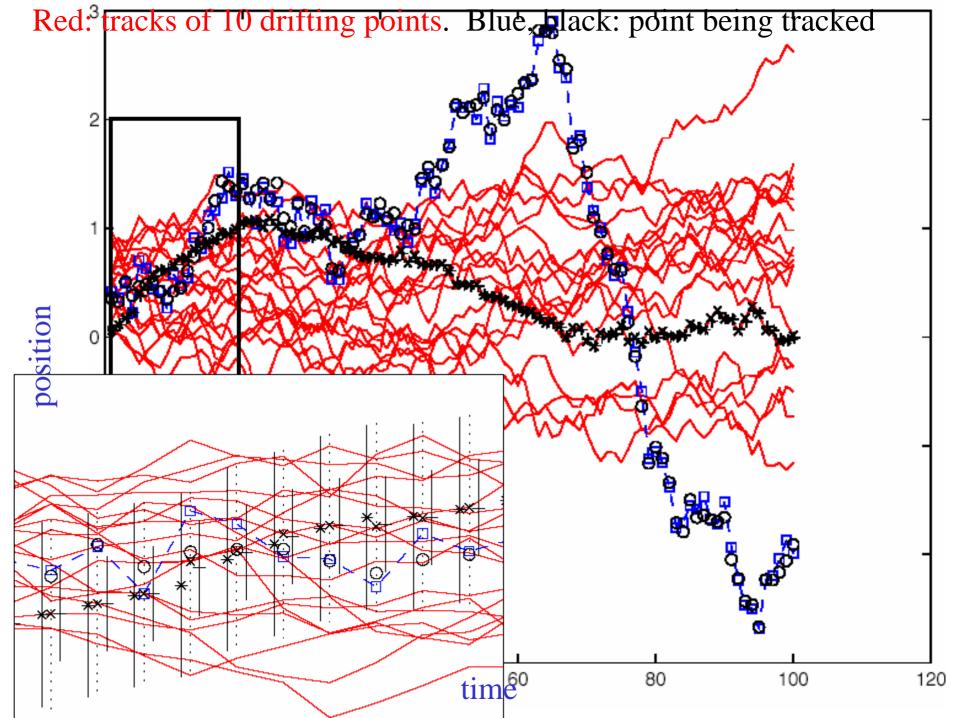
- Nearest neighbours
 - choose the measurement with highest probability given predicted state
 - popular, but can lead to catastrophe
- Probabilistic Data Association
 - combine measurements, weighting by probability given predicted state
 - gate using predicted state











Abrupt changes

What if environment is sometimes unpredictable?

Do people move with constant velocity?

Test several models of assumed dynamics, use the best.

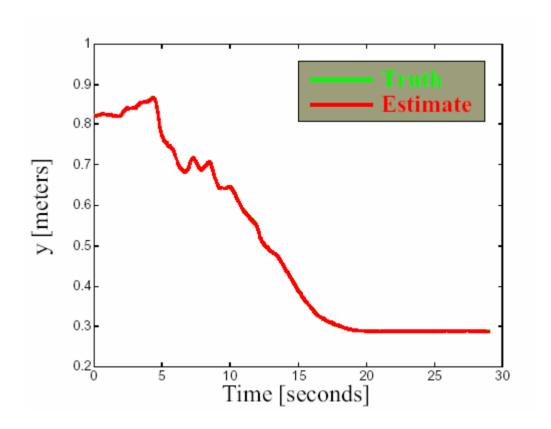
Multiple model filters

Test several models of assumed dynamics

```
KF\mu_1 X_{\mu_1} p(\mu_1 \mid z, \prod_{\mu_1}) \widehat{\mathbf{x}} \mathbf{x} \mathbf{x}
```

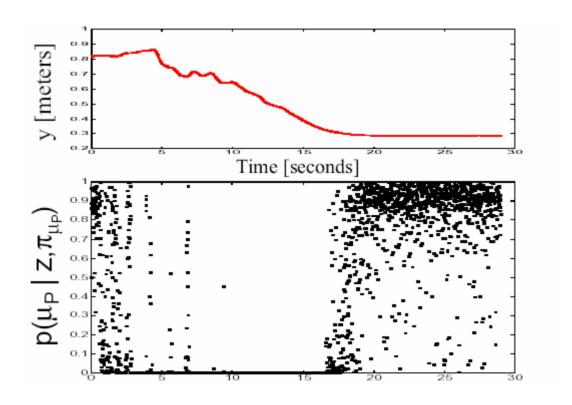
MM estimate

Two models: Position (P), Position+Velocity (PV)



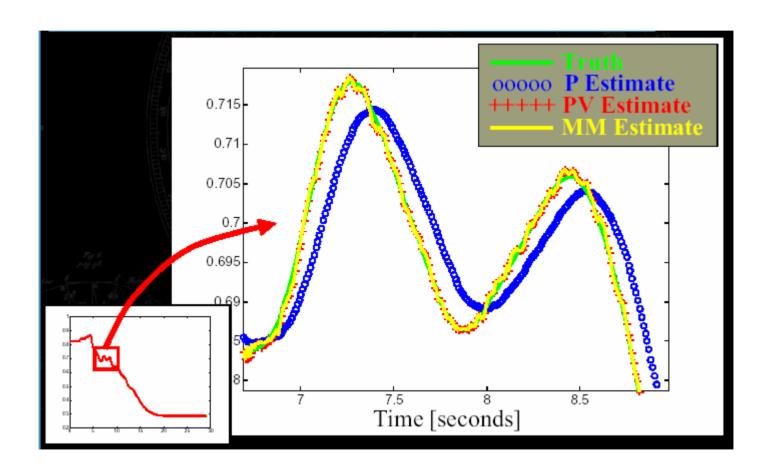
[figure from Welsh and Bishop 2601]

P likelihood



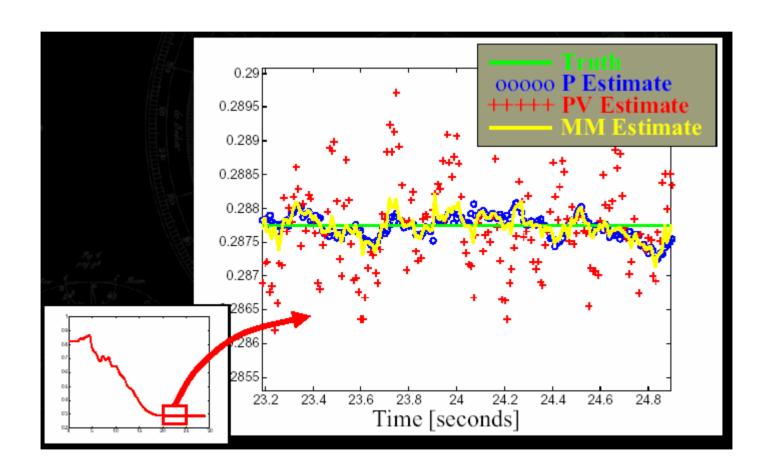
[figure from Welsh and Bishop 2601]

No lag



[figure from Welsh and Bishop 2601]

Smooth when still



[figure from Welsh and Bishop 2601]

Resources

Kalman filter homepage

http://www.cs.unc.edu/~welch/kalman/

• Kevin Murphy's Matlab toolbox:

http://www.ai.mit.edu/~murphyk/Software/Kalman/k alman.html

Jepson, Fleet, and El-Maraghi tracker

IEEE Conference on Computer Vision and and Pattern Recognition, Kauai, 2001, Vol. I, pp. 415-422

Robust Online Appearance Models for Visual Tracking

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Jepson, Fleet, and El-Maraghi tracker



Figure 4. The adaptation of the model during tracking. (top) The target region in selected frames 200, 300, 480. (bottom) The stable component's mixing probability (left) and mean (right) for the selected frames.



Jepson, Fleet, and El-Maraghi tracker

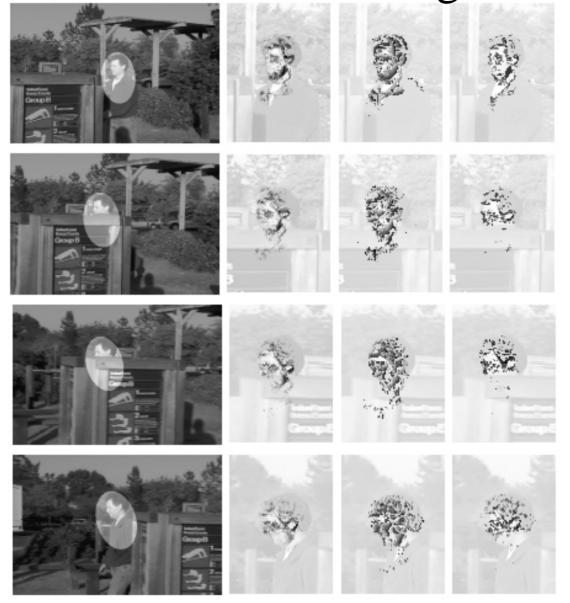


Figure 3. Each row shows, from left to right, the tracking region, the stable component's mixing probability $m_s(\mathbf{x}, t)$, mean $\mu_s(\mathbf{x}, t)$, and ownership probability $o_s(\mathbf{x}, t)$. The rows correspond to frames 244, 259, 274, and 289, top to bottom. Note the model persistence and the drop in data ownership within the occluded region.

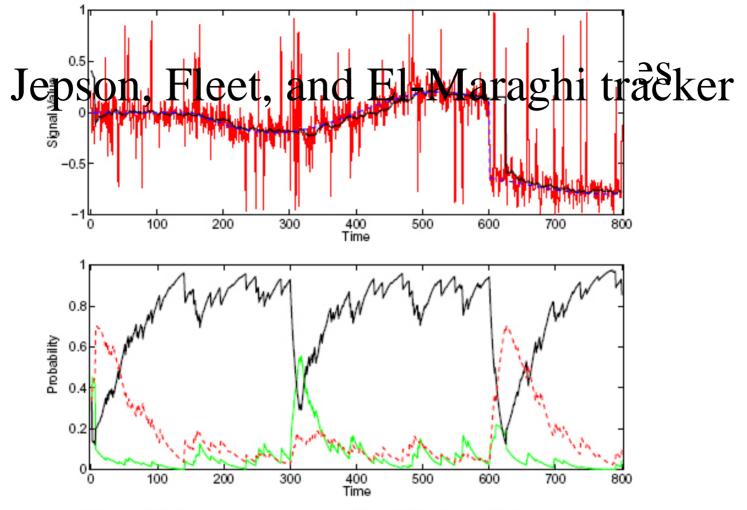


Figure 2. Estimation using on-line EM. (top) The original data (thin red) with true state (dashed blue) and the estimated mean of the stable process (thick black). The noise is a mixture of Gaussian and uniform densities, with mixing probabilities (0.9, 0.1), except for 15 frames at 300 which are pure outliers. (bottom) Mixing probabilities for \mathcal{S} (black), \mathcal{W} (dashed red), and the \mathcal{L} (light green).

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