

Admin:

Pset #2 due 3/13

Projects!

Today:

Block ciphers:

✓ DES

✓ AES

Modes of operation

✓ Ideal cipher (ECB, CTR, CBC)

Desai's "UFE" mode

Readings:

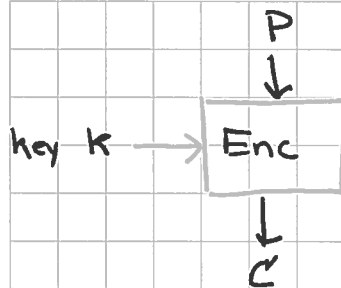
Ferguson Ch 3,

Paar Ch 3,4

Katz Ch 5

Wikipedia: "Block cipher modes of operation"

"Ciphertext stealing"

Block ciphers:

plaintext block

ciphertext block

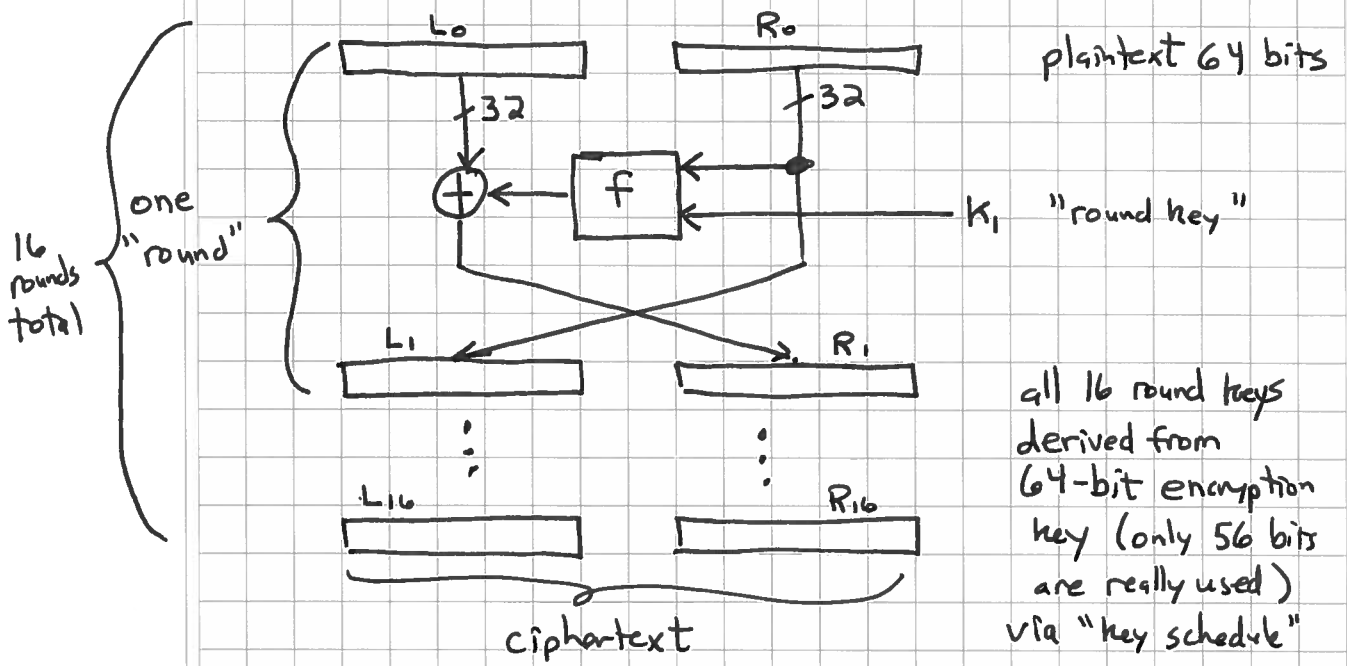
fixed-length P, C, K DES: $|P| = |C| = 64$ bits $|K| = 56$ bitsAES: $|P| = |C| = 128$ bits $|K| = 128, 192, 256$ bits

Use a "mode of operation" to handle variable-length input.

DES

"Data Encryption Standard"
Standardized in 1976. Now deprecated in favor of AES.

"Feistel structure":



Notes: Invertible for any f and any key schedule.

f uses 8 "S-boxes" mapping 6-bits \Rightarrow 4 bits nonlinearly.

Key is too short! (Breackable now quite easily by brute-force)

Subject to differential attacks:

$$\begin{array}{ccc}
 M & \longleftrightarrow & M \oplus \Delta \\
 \downarrow & & \downarrow \\
 \begin{array}{c} k \rightarrow \boxed{\text{DES}} \\ \downarrow \\ C \end{array} & & \begin{array}{c} k \rightarrow \boxed{\text{DES}} \\ \downarrow \\ C + \delta \end{array} \\
 \downarrow & & \downarrow \\
 C & \longleftrightarrow & C + \delta
 \end{array}$$

2^{47} chosen pairs (Biham/Shamir)

Subject to linear attacks:

e.g. if $M_3 \oplus M_{15} \oplus C_2 \oplus K_{14} = 0$ (eqn on bits)
with prob $p = 1/2 + \epsilon$

then need $1/\epsilon^2$ samples to break (Matsui, 2^{43} PT/CT pairs)

AES

"Advanced Encryption Standard" (U.S. govt)

Replaces DES

AES "contest" 1997-1999:

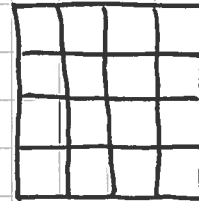
15 algorithms submitted: RC6, Mars, Twofish, Rijndael, ...
Winner = Rijndael (by Joan Daemen & Vincent Rijmen, (Belgians))

Specs: 128-bit plaintext/ciphertext blocks
128, 192, or 256-bit key
10, 12, or 14 rounds (dep. on key length)

Byte-oriented design (some math done in Galois field $GF(2^8)$)

View input as 4x4 byte array:

$$4 \times 4 \times 8 = 128$$



For version with 128-bit keys, 10 rounds:

- Derive 11 "round keys", each 128 bits (4x4x byte)

- In each round:
 - ① XOR round key
 - ② Substitute bytes (lookup table)
 - ③ Rotate rows (by different amts)
 - ④ Mix each column (by linear opn)

- Output final state

See readings for details.

There are very fast implementations. Also Intel has put supporting hardware into its CPU's.

Security: Good; perhaps # rounds should be a bit larger...

(last round has another round key XORed in instead of mix-column)

For practical purposes, can treat AES as ideal block cipher:

[For each key, mapping $\text{Enc}(K, \cdot)$ is a random independent permutation of $\{0,1\}^{128}$ to itself.

Modes of Operation:

How to encrypt variable-length messages? (using AES)

"ECB" = "Electronic code book"

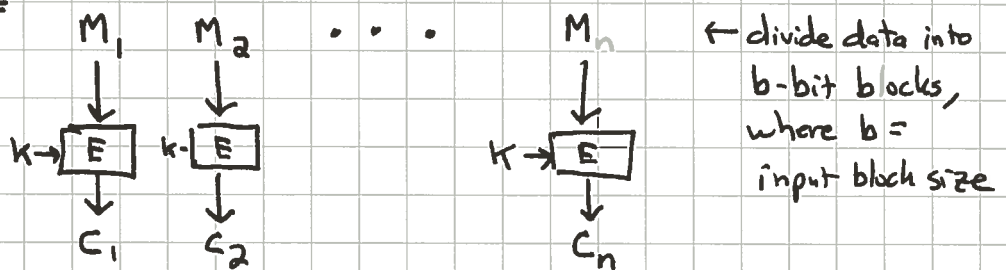
"CTR" = "Counter mode"

"CBC" = "Cipher-block chaining" (& CBC-MAC)

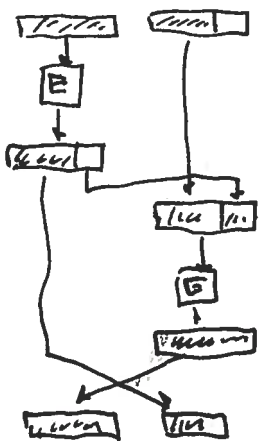
"CFB" = "Cipher feedback"

... (others...)

ECB:



Ciphertext stealing



To handle data that is not a multiple of b bits in length:

• Append a "1" bit (always)

• Append enough "0" bits to make length a multiple of b bits.

This gives invertible (1-1) "padding" operation.

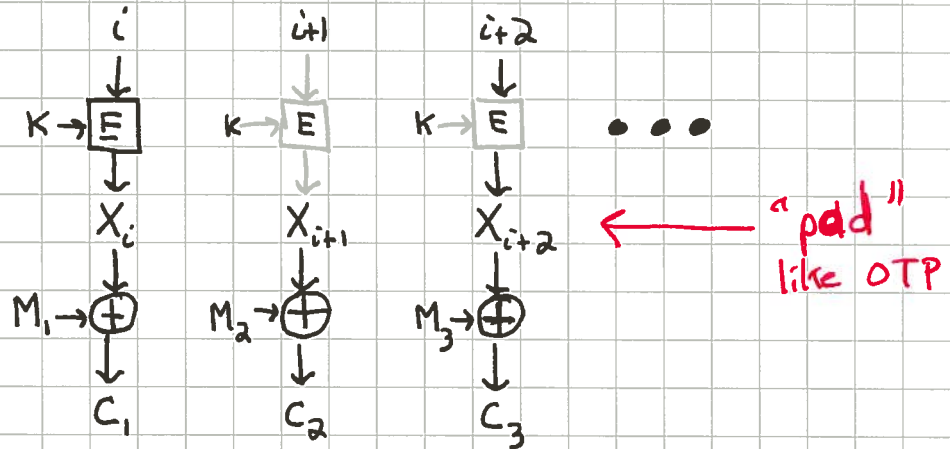
Pad before encryption; unpad after decryption.

ECB preserves many patterns: repeated message blocks
 \Rightarrow repeated ciphertext blocks

ECB really only good for encrypting random data
 (e.g. keys)

CTR (Counter mode):

Generate a PR (pseudorandom) sequence by encrypting $i, i+1, \dots$
XOR with message to obtain ciphertext.



Initial counter value can be transmitted first:

i, C_1, C_2, \dots

Of course, no counter value should be re-used!