

Admin:

Pset #1 due today. Pset #2 out.

Today:

E-cash & bitcoin

- Money - basics
- Electronic checks
- Signed coin ID
- Identities
- (Public) Ledgers
- Bitcoin

"Electronic Money"

- What properties should it have?
- " " can " " ?

Atoms vs Bits

- What can "possessing value" (money) mean?
- How can we transfer value?

Easy to answer if we use (gold) atoms to represent value:

- gold atoms are hard to make
- only one person at a time can "own" an atom

Things get complicated if we want to use bits:

- easy to generate bits
- bits can be copied  $\Rightarrow$  double-spending becomes a problem!

(Token-based)

Possession-based vs Account-based methods

- In a possession-based method, owning the representation  $\equiv$  owning the value
- In an account-based method, there is usually some or ledger  $\rightarrow$  TTP who "maintains accounts" (e.g. a "bank"); xactions cause value to be shifted from one acct to another.
- Most "bit-based" methods are account-based.

Simple example: Electronic checks

- Account-based: Bank has  $PK_B, SK_B$
- User has  $PK_U, SK_U, \text{cert on } (U, PK_U) \text{ by bank}$
- Check = 
$$\begin{bmatrix} \text{cert (on } PK_U, \text{ signed by } SK_B) \\ \text{sign}(SK_U, \text{"Pay Bob \$100, date, serial \#"}) \end{bmatrix}$$
- Bank deposits check just once (using ser #)
- Usual problem of overdrawn acct (bad check)
- Bank knows exact details: payer, payee, amt, date
- Merchant " " "

This works.

What else is possible?

Can we make payments more like cash?

G.857 Rinvest

L22.4 4/27/11

## Desirable (?) Properties

- Non-forgable (prevent fraud, inflation)
- Not double-spendable
- Reliability: can "back up" your \$
- Exclusive ownership
- Transferability: A can pay B
- Transitivity: B can use A's payment to pay C
- Variable-denominations
- Divisibility & combinability
- Efficiency (esp. for small cents)
- On-line versus off-line transactions
- Scalability
- anonymity
- ~~security~~ security
- Conversion to "ordinary" money

### traditional:

- medium of exchange
- store of value
- unit of account  
"unit of measure"

G.857 Rivest  
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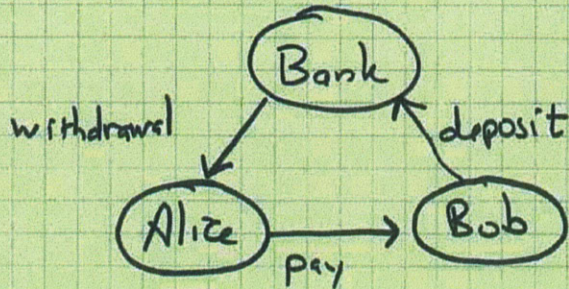
## Double-spending

- essentially a "replay attack"
- if you can backup your \$, then "restore" gives you your spent money back !?
- prevention seems really tough (unless you use atoms)
- detection requires convergence of spending records (e.g. at bank) and large databases (?) **ledger**
- even if you can detect double-spending - what do you do?
  - roll back / deny transaction  
(2<sup>nd</sup> merchant to get some electronic coin can't deposit it)
  - punishing perpetrator may be impossible if we have (true) anonymity: payer is not identifiable
  - furthermore: is payer or payee the culprit?  
(can merchant "frame" consumer?)
  - deterrence may be hard... how to punish  
(pay fine from account?)

Some approaches:

Signed coin ID

Bank (TTP)  
Alice (payer)  
Bob (payee)



3 protocols to support:

- ① withdrawal/authorization  
Alice becomes "able to pay"  
(e.g. cost issuance in check scheme)
  - ② payment
  - ③ deposit
- } life of a "coin"

① withdrawal:

• Bank gives Alice  $R, \text{sign}(sk_B, R)$  ← unforgeable object!  
= coin R is coin ID

• Bank keeps R in database of unspent coins

• Bank debits Alice's acct for withdrawal

② payment:

Alice gives coin to Bob; Bob checks Bank sig

③ deposit:

Bob gives coin to Bank, Bank checks sig & R in DB

Flags R as "spent"

MicroMint (Rivest & Shamir 1996)

Let  $h: \{0,1\}^* \rightarrow \{0,1\}^d$  be a hash fn, where  $d$  is modest.

To find a k-way collision, find

$$x_1, x_2, \dots, x_k \quad (\text{all distinct})$$

s.t.

$$h(x_1) = h(x_2) = \dots = h(x_k) \quad [\text{Verification easy}]$$

By generalized "birthday paradox" arguments need about  $2^{d(k-1)/k}$  hashes to find a k-way collision.

(E.g.  $n^{2/3}$  for a 3-way collision, where  $n = 2^d$ )

Looking at  $C$  times as many yields  $\approx C^k$  collisions (great economy of scale).

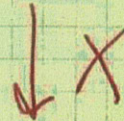
MicroMint: coin is a k-way collision.

Efficient generation seems to require some memory (e.g.  $n^{1/3}$  memory).

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- Not very efficient - bank has to sign each coin!
- Double-spending can be a problem!
- Check scheme better - merchant can't frame user!

## Peppercorn (Micali & Rivest)



- "probabilistic payments":
  - paying 10¢  $\equiv$  paying \$10 with probability 1/100  
(micropayment)  $\approx$  (macropayment, sometimes)
- based on electronic checks method
- Alice pays Bob 10¢ as follows:
  - She gives Bob electronic check for \$10 that contains condition: "This check valid if and only if E is true" (where E holds with probability 1/100)
- Bob must be able to test if E is true
  - if so, he can deposit check
  - if not, he throws check away (but gives Alice her purchase)
  - he gets paid correctly on the average  
(law of large numbers)
- Alice should not be able to tell if E is true when she writes check (else she can filter checks...)
- Bank should be able to tell if E is true (so "bad checks" where E is false, don't get deposited).

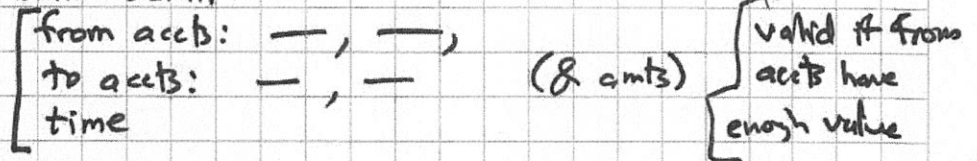


# Bitcoin:

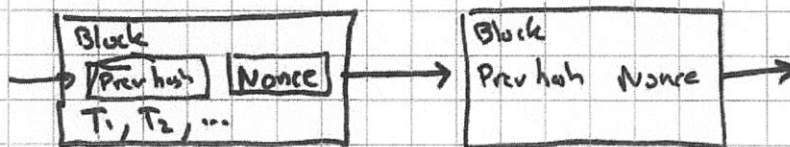
- ID's are PK's (used for signing transactions) ECDSA
- public ledger records all transactions (account-based) PK = acct name
- money created by/for those maintaining ledger ("miners")  
no other way to create money

(digest: discuss need for loans!)

• transaction detail:



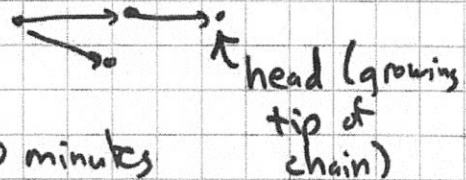
• ledger detail: "block chain"



block valid if hash (block) begins with enough zeros & Tx's valid

no TTP!

need to search nonces to find one that works (like hash cash)  
solved blocks are "published"  
longest chain wins



difficulty level adapts to yield ≈ one solution every 10 minutes

wait for enough (6) confirmations

view blockchain.info

ledger is transaction log

implies account balances

verifying a transaction  
involves checking account balances

### Issues:

#### • Scalability?

- can it do e.g. 4000 tps (like Visa?)
- blocks may reach 1/2 GB, block num is only 306B or so
- ECDSA signature verification main computational need

#### • Phasing out of miner's fee?

(in 2140 or so ... 21M BTC)  
xact fees

(reward halves every 4 years)  
25 BTC/block now

#### • Act-based but no loans!

(Can't create money by giving a loan, as you can with current monetary system.)

Like "gold standard" in terms of "coin creation"

#### • Protocol vulnerabilities:

- large pool of miners (>50%)
- "majority is not enough" (Eyal/Sirer)