

Admin: Pset #1 back at end of class

Today: Block ciphers
DES (Data Encryption Standard)
AES (Advanced Encryption Standard)
Ideal Block Cipher
Modes of Operation:
ECB
CTR
CBC
CFB
IND-CCA security defn
LFE mode

Block ciphers:



fixed-length P, C, K

DES: $|P| = |C| = 64$ bits $|K| = 56$ bits

AES: $|P| = |C| = 128$ bits $|K| = 128, 192, 256$ bits

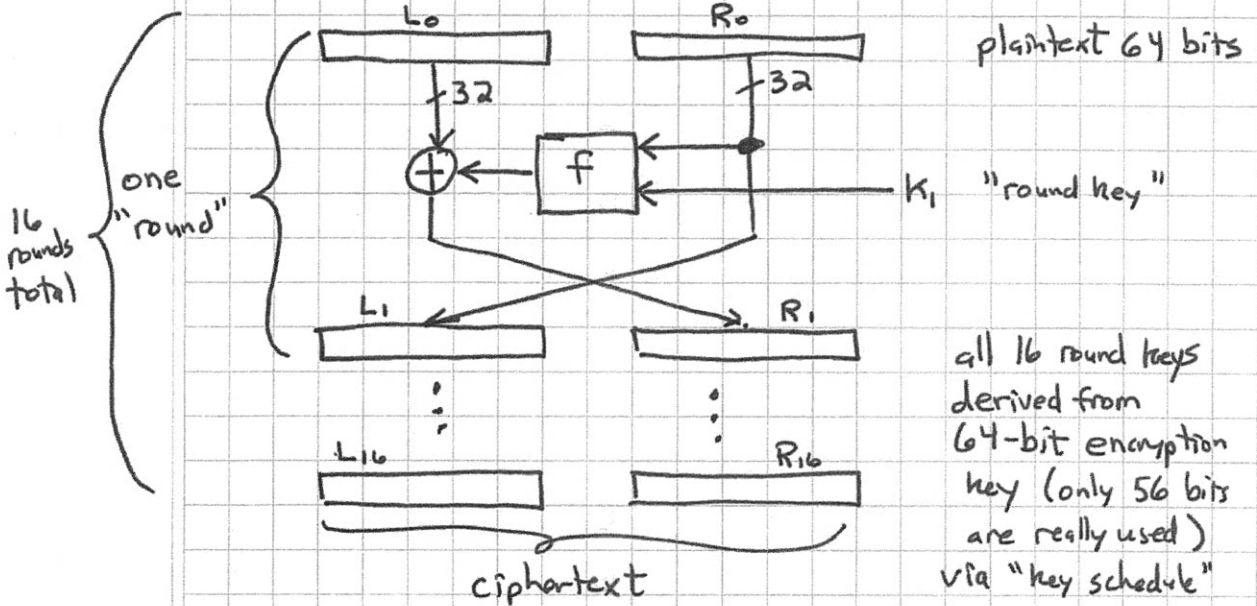
Use a "mode of operation" to handle variable-length input.

DES

"Data Encryption Standard"

Standardized in 1976. Now deprecated in favor of AES.

"Feistel structure":

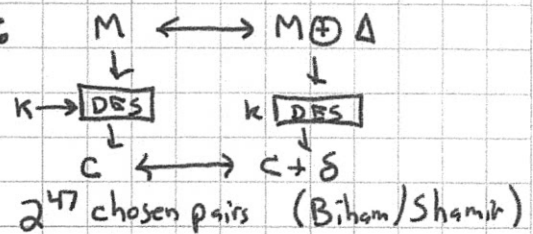


Notes: Invertible for any f and any key schedule.

f uses 8 "S-boxes" mapping 6-bits \Rightarrow 4 bits nonlinearly.

Key is too short! (Breakable now quite easily by brute-force)

Subject to differential attacks:



Subject to linear attacks:

e.g. if $M_3 \oplus M_{15} \oplus C_2 \oplus K_{14} = 0$ (eqn on bits)
with prob $p = 1/2 + \epsilon$

then need $1/\epsilon^2$ samples to break (Matsui, 2^{43} PT/CT pairs)

AES

"Advanced Encryption Standard" (U.S. govt)

Replaces DES

AES "contest" 1997-1999:

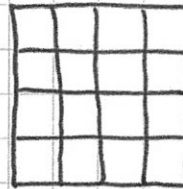
15 algorithms submitted: RC6, Mars, Twofish, Rijndael, ...
 Winner = Rijndael (by Joan Daemen & Vincent Rijmen, (Belgians))

Specs: 128-bit plaintext/ciphertext blocks
 128, 192, or 256-bit key
 10, 12, or 14 rounds (dep. on key length)

Byte-oriented design (some math done in Galois field $GF(2^8)$)

View input as 4x4 byte array:

$4 \times 4 \times 8 = 128$



For version with 128-bit keys, 10 rounds:

- Derive 11 "round keys", each 128 bits (4x4x byte)

- In each round:
 - ① XOR round key
 - ② Substitute bytes (lookup table)
 - ③ Rotate rows (by different amts)
 - ④ Mix each column (by linear opn)

- Output final state

See readings for details.

There are very fast implementations. Also Intel has put supporting hardware into its CPU's.

Security: Good; perhaps # rounds should be a bit larger...

For practical purposes, can treat AES as ideal block cipher:

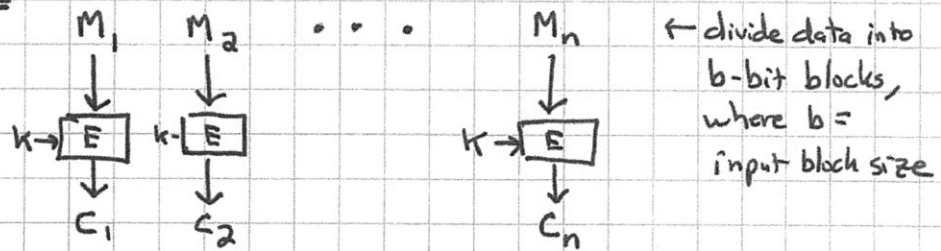
[For each key, mapping $Enc(K, \cdot)$ is a random independent permutation of $\{0, 1\}^{128}$ to itself.

Modes of Operation:

How to encrypt variable-length messages? (using AES)

- "ECB" = "Electronic code book"
- "CTR" = "Counter mode"
- "CBC" = "Cipher-block chaining" (& CBC-MAC)
- "CFB" = "Cipher feedback"
- ... (others, ...)

ECB:



To handle data that is not a multiple of b bits in length:

- Append a "1" bit (always)
- Append enough "0" bits to make length a multiple of b bits.

This gives invertible (1-1) "padding" operation.

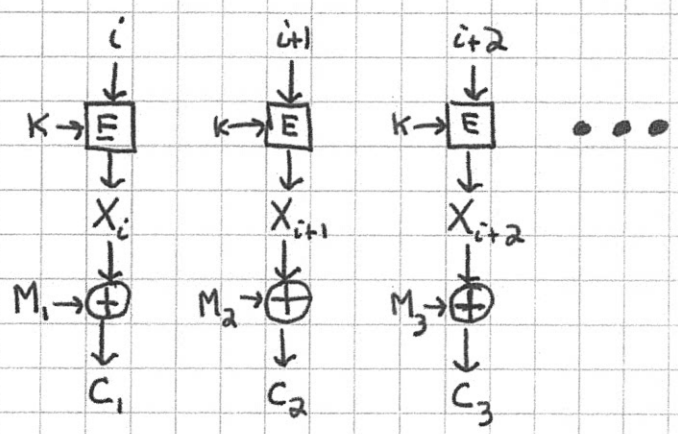
Pad before encryption; unpad after decryption.

ECB preserves many patterns: repeated message blocks
 ⇒ repeated ciphertext blocks

ECB really only good for encrypting random data (e.g. keys)

CTR (Counter mode):

Generate a PR (pseudorandom) sequence by encrypting $i, i+1, \dots$.
XOR with message to obtain ciphertext.



Initial counter value can be transmitted first:

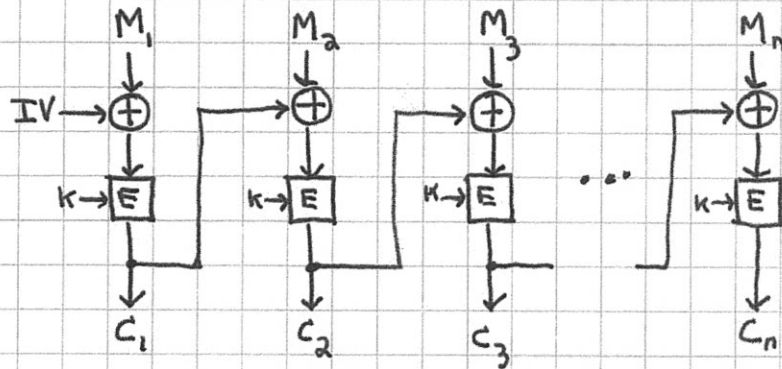
i, C_1, C_2, \dots

Of course, no counter value should be re-used!

CBC (Cipher-block chaining):

Choose IV ("initialization value") randomly, then use each C_i as "IV" for M_{i+1} . Transmit IV with ciphertext:

$$IV, C_1, C_2, \dots, C_n$$



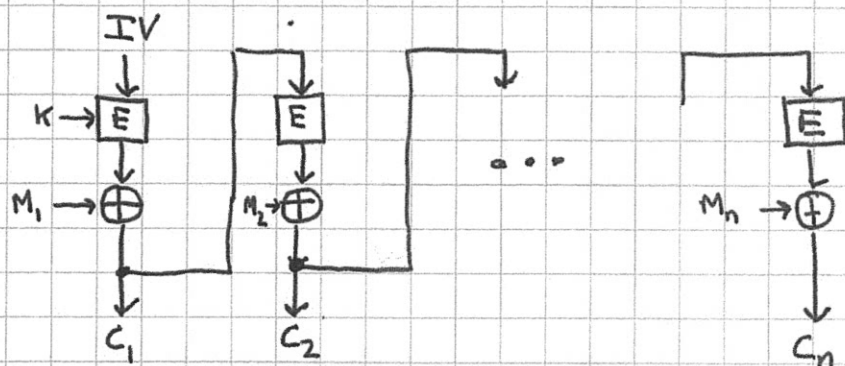
Decryption easy, and parallelizable (∴ little error propagation)

Lookup "ciphertext stealing" for cute way of handling messages that are not a multiple of b bits in length. This method give ciphertext length = message length.

Last block C_n is the "CBC-MAC" (CBC Message Authentication code) for message M . [A fixed IV is used here.] The MAC is a "cryptographic checksum" (more later...) (If messages have variable length then key for last block should be different.)

CFB (Cipher feedback mode)

Similar to CBC mode. Uses random IV transmitted with ciphertext.



If M is not a multiple of b bits in length, can just transmit shortened ciphertext. (No need for ciphertext stealing.)