Problem Set 6, Part a

Due: Thursday, May 8, 2008

Reading:

Borowsky, Gafni, Lynch, Rajsbaum paper. Attiya, Welch, Section 5.3.2 (optional). Attie, Guerraoui, Kouznetsov, Lynch, Rajsbaum paper

Reading for next week:

Chapter 9 from the Herlihy, Shavit book. (See course web site.) Herlihy, Luchango, Moir, and Schere paper on Software Transactional Memory. Dice, Shalev, and Shavit paper on Transactional Locking.

Problems:

- 1. As noted in class, the BGLR paper has a liveness bug in the main protocol. Namely, a simulating process i may repeatedly decide to select the same process j to perform a snapshot, using safe-agreement, neglecting some other process j'.
 - (a) Why doesn't the task structure of process i, which has a separate task for each simulated process, ensure progress for all the simulated processes?
 - (b) Give a simple modification to the given code that would fix this problem, and guarantee that all the simulated processes get fair turns.
- 2. Consider the *approximate agreement* problem, expressed as a decision problem as follows: The value domain V is the set of rational numbers. For any input vector I of elements of V, the allowable output vectors are those for which (a) every element is in the range of the values in I, and (b) the difference between any two output values is at most one.

Suppose we are given a 10-process, 2-fault-tolerant asynchronous shared memory algorithm A that solves approximate agreement, using read/write shared registers. Describe clearly how we can use algorithm A and the BG-simulation results to obtain a 3-process wait-free asynchronous shared memory algorithm to solve approximate agreement, again using read/write shared registers.

- 3. For each of the following pairs of resilient (fault-tolerant) atomic objects, A and B, say whether or not A can be implemented using an unlimited number of B's, plus an unlimited number of reliable read/write registers. Prove your answers.
 - (a) A is an 8-process 3-resilient consensus atomic object, and B is a 4-process 2-resilient consensus atomic object.
 - (b) A is an 8-process 4-resilient 2-consensus (AKA 2-set-consensus) atomic object, and B is a 4-process 3-resilient consensus atomic object. (For this part and the next, it will prove useful to consult Section 5 of the AGKLR paper.)
 - (c) A is an 8-process 4-resilient 4-consensus atomic object, and B is a 4-process 2-resilient consensus atomic object. (Hint: you may find it helpful to connect processes to more than one object.)