

6.849: Geometric Folding Algorithms

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<http://courses.csail.mit.edu/6.849/spring17/>

Inverted lectures: (new format)

- online video lectures + notes + slides
(from 2010; also bonus videos from 2012)
 - **DEMO**: slide sync & jump, playback speed, required feedback form
- class time for interactivity
 - answering questions
 - additional detail/material of interest
 - guest lectures
 - activities: folding, building, etc.
- * solving problems: solved & unsolved!
 - ~ math, programming, and design
- + optional open problem session (if interest)
- Coauthor software to coordinate in/outside class

DISCUSS

Requirements:

- sign up for account on Coauthor] on website
- short survey of your background
- watch video lecture by NOON on Tuesday
 - e.g. Monday night OR weekend
- fill out form to confirm watching DEMO
- post any questions / feedback to Coauthor
- attend classes (email me about exceptions)
 - generally not videoed
 - solve problems together!
- problem sets ≈ weekly
 - choose your own adventure
 - often: solve 2 out of 3 problemsDEMO
PS1
- project & presentation
 - build/design physical structure
 - implement algorithm/illustration/tool
 - pose open problem
 - research: try to solve an open problem
 - survey subfield (not in textbook)
 - Wikipedia (write/improve several articles)
- textbook: Demaine & O'Rourke. CUP 2007
 - (working on discount)

Geometric folding algorithms:

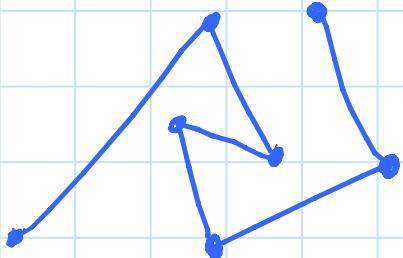
In general: Mathematics & algorithms behind (un)folding of geometric objects

Applications/connections to:

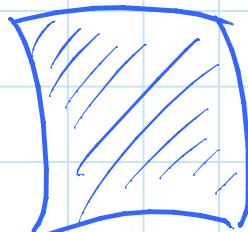
- robotics → arms, Transformers, programmable matter, ...
- graphics → morphing, animation, ...
- mechanics → steam engines, ...
- manufacturing → sheet-metal & tube bending, nanomanufacturing, optics, ...
- medical → stents, drug delivery, ...
- aerospace → telescope deployment, ...
- biology → protein folding & design, ...
- sculpture → origami, interactive sculpture, ...
- architecture → dynamic architecture, deployable/collapsible structures, ...

Geometric objects & rules for folding:

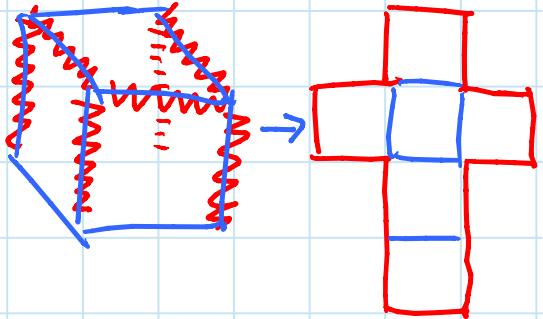
I linkage



II paper



III polyhedron



↪ rigid bars

↪ stay connected

↪ [don't cross]

↪ don't stretch

↪ don't tear

↪ don't cross

↪ cut surface

↪ one piece

↪ no overlap

Problem types:

e.g. can this fold? how?

↗ FOLDABILITY / ANALYSIS

structure

foldings / properties

e.g. how to fold desired shape

Result types:

- UNIVERSALITY: Everything is foldable!

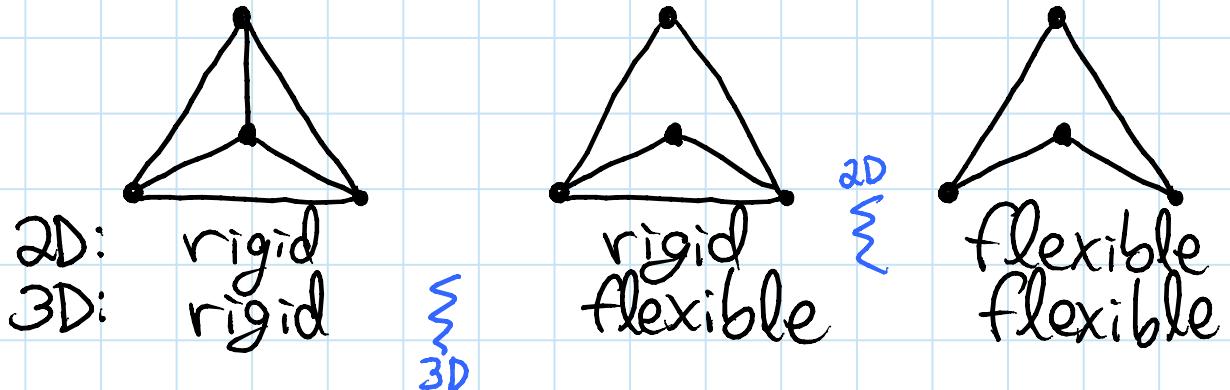
(& here's an algorithm to do it)

- DECISION: Efficient algorithm to decide foldability

- HARDNESS: Computationally intractable
to decide foldability

I LINKAGES:

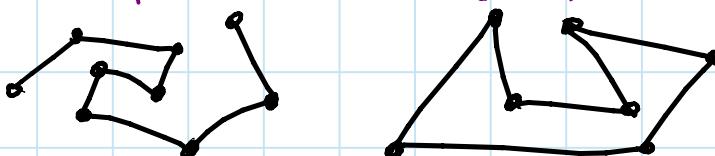
Rigidity: which linkages fold at all?



- efficient characterization in 2D
- **OPEN**: 3D

Universality: which linkages can fold into all possible configurations?

- 2D chains/polygons: UNIVERSAL
[Connelly, Demaine, Rote 2000; Streinu 2000;
Cantarella, Demaine, Iben, O'Brien 2004]



- 3D chains: CAN LOCK
[Cantarella & Johnston 1998] (related to protein folding)



- 4D⁺ chains: UNIVERSAL
[Cocan & O'Rourke 2001]

II PAPER:

Foldability: which crease patterns fold flat?

- NP-hard

[Bern & Hayes 1996]

& [Akitaya, Cheung, Demaine, Horiyama, Hull, Ku, Tachi, Uehara 2015]

(\Rightarrow likely no efficient algorithm)

Design: what shapes can be folded?

- universal: any 2D polygon, 3D polyhedron.
2-color pattern (inefficiently)

[Demaine, Demaine, Mitchell 2001]

- Origamizer: practical [Tachi 2006;
Demaine & Tachi]

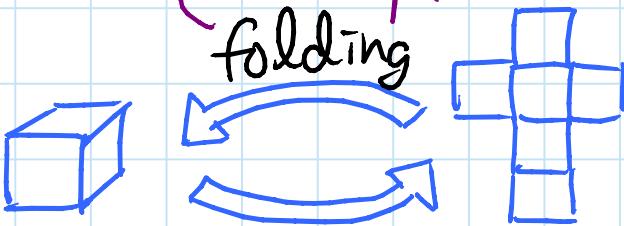
- maze folding: fold extruded orthogonal graph
with scale factor 3 (independent of maze)

[Demaine, Demaine, Ku 2010]

- fold & cut: any set of line segments can be
aligned by flat folding [Demaine, Demaine, Lubiw 1998;
Bern, Demaine, Eppstein, Hayes 1998]

III POLYHEDRA:

[Metamorphosis of the Cube]



Polyhedron
convex
general

edge general
OPEN YES
NO **OPEN**

IV HINGED DISSECTIONS:

- any finite set of polygons of same area can be folded from one chain of polygons (without collision)

[Abbott, Abel, Charlton, Demaine, Demaine, Komninos, 2008]



Solved & open problems!

DEMO COAUTHOR