


## Probability: 1st Idea

- A set of basic experimental outcomes
- A subset of outcomes is an event
- The probability of an event:

$$
\operatorname{Pr}[\text { event }]::=\frac{\text { \# outcomes in event }}{\text { total \#outcomes }}
$$

The Monty Hall Game Applied Probability: Let's Make A Deal (1970's TV Game Show)
$\qquad$

Monty Hall Webpages

http://www.letsmakeadeal.com

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 Albert R Meyer, May 1,2013

> The Monty Hall Game -goats behind two doors - prize behind third door - contestant picks a door - Monty reveals a goat behind an unpicked door - Contest sticks, or switches to the other unopened door

## Analyzing Monty Hall

Marilyn Vos Savant explained Game in magazine -- bombarded by letters (even from PhD's) debating:

1) sticking \& switching equally good
2) switching better


## Analyzing Monty Hall

Determine the outcomes.
-- using a tree of possible steps can help
A) Albert R Meyer, May 1,2013

| Monty Hall STICK strategy  <br> Win by sticking STICK <br> iff  <br> Lose 6  <br> Lose by switching Wins: 6 |
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#":*)Analyzing Monty Hall
    A false conclusion:
    sticking and switching have
    same # winning outcomes, so
    probability of winning
    is the same for both: 1/2.
```


## Analyzing Monty Hall

Another false argument: after door opening, 1 goat and 1 prize are left.


## A false conclusion:

 sticking of id s it/ning have same \# w nin in sutc mes, so probabiliny of winning is the same for both: $1 / 2$.> 胉: Analyzing Monty Hall Another false argument: after door opening, 1 goat and 1 prize are left. Each door is equally likely to have the prize (by symmetry), so both strategies win with probability: $1 / 2$.


## Analyzing Monty Hall

## What's wrong?

Let's look at the outcome tree more carefully.


## （1ix Probability：2nd Idea <br> Outcomes may have differing probabilities！ Not always uniform．

## Finding Probability

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Intuition is important but dangerous．
Stick with 4－part method：
1．Identify outcomes（tree helps）
2．Identify event（winning）
3．Assign outcome probabilities
4．Compute event probabilities
[回娄思 Finding Probability
Intuition is important but dangerous.
Stick with 4-part method:
. Identify outcomes (tree helps)
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