

Mathematics for Computer Science MIT 6.042J/18.062J

# The Law of Large Numbers

Albert R Mever

May 13, 2013

## What the mean means

The mean value of a fair die roll is 3.5, but we will never roll 3.5. So why do we care what the mean is? We believe that after many rolls, the average roll will be near 35



Albert R Mever

May 13, 2013



### What probability means

$$\Pr[\text{roll 6}] = \frac{1}{6}$$

We believe that after many rolls, the fraction of 6's will be near 1/6.



#### Jacob D. Bernoulli (1659-1705)

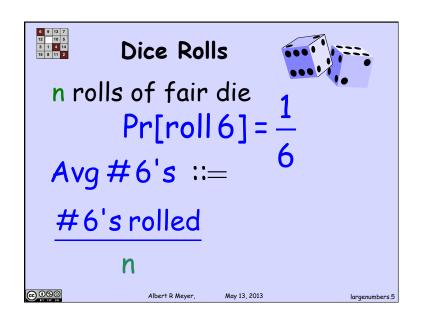
Even the stupidest man —by some instinct of nature per se and by no previous instruction (this is truly amazing) –knows for sure that the more observations ...that are taken, the less the danger will be of straying from the mark.

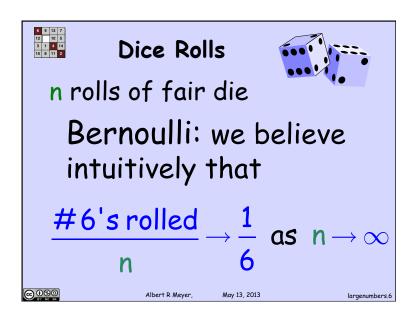
--- Ars Conjectandi (The Art of Guessing), 1713\*

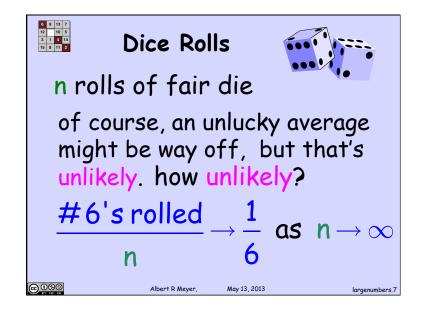
http://www.dartmouth.edu/~chance/teaching aids/books articles/probability book/book.html

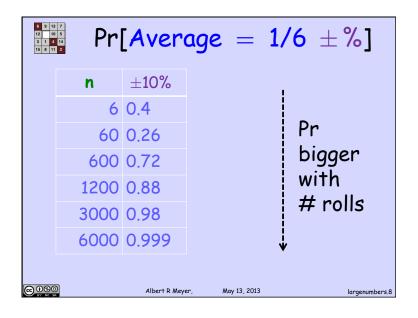
Albert R Mever

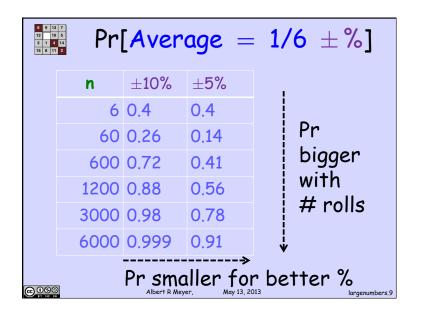
May 13 2013

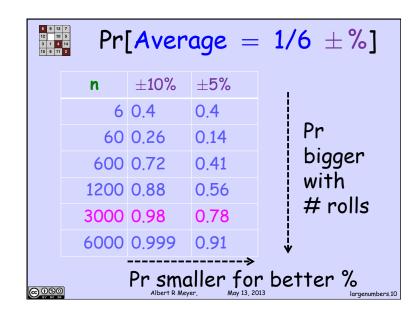


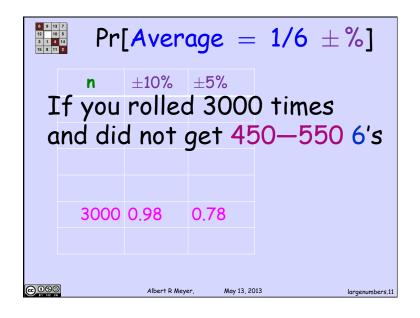


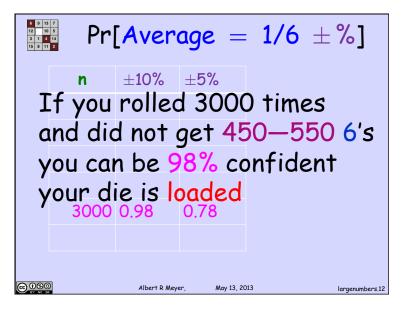


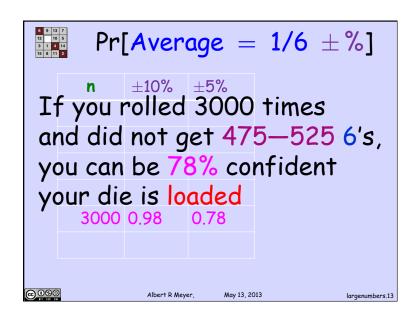


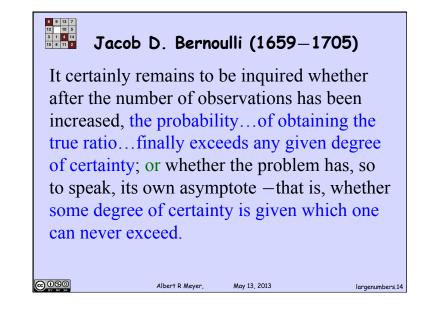


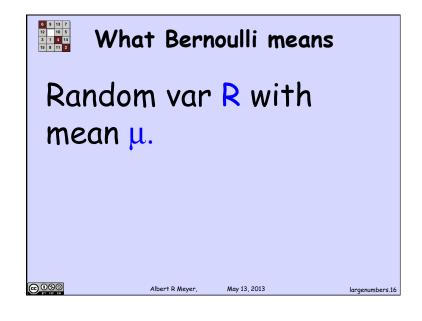


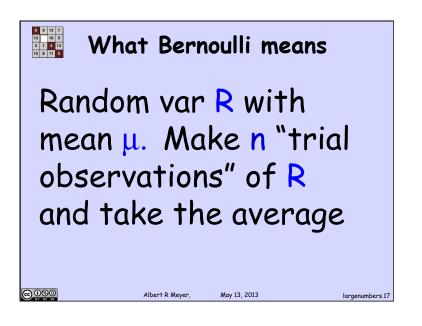


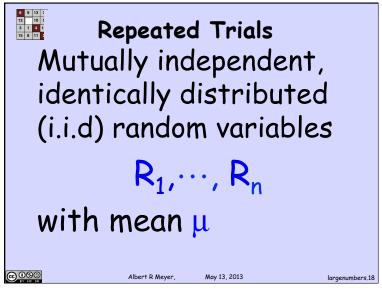


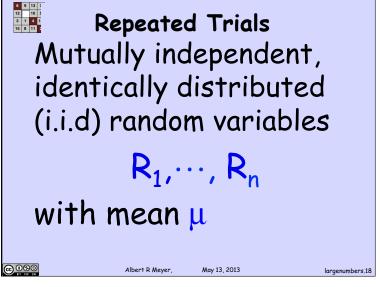


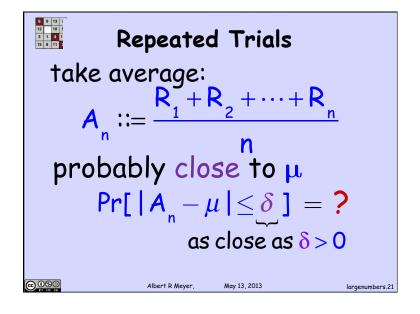


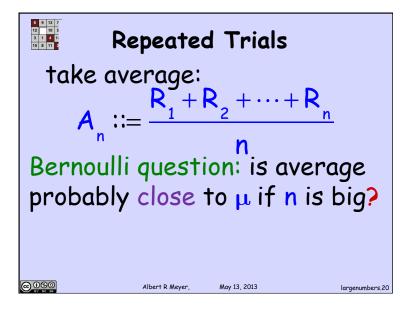














Therefore, this is the problem which I now set forth and make known after I have pondered over it for twenty years. Both its novelty and its very great usefulness, coupled with its just as great difficulty, can exceed in weight and value all the remaining chapters of this thesis.

