Problem 1. Week 4 Notes contain a proof by induction that:

$$1 + 2 + 3 + \dots + n = \frac{n(n+1)}{2}$$

But now we're going to prove a *contradictory* theorem!

False Theorem. For all $n \ge 0$,

$$2+3+4+\dots+n = \frac{n(n+1)}{2}$$

Proof. We use induction. Let P(n) be the proposition that $2 + 3 + 4 + \cdots + n = n(n+1)/2$.

Base case: P(0) is true, since both sides of the equation are equal to zero. (Recall that a sum with no terms is zero.)

Inductive step: Now we must show that P(n) implies P(n + 1) for all $n \ge 0$. So suppose that P(n) is true; that is, $2 + 3 + 4 + \cdots + n = n(n + 1)/2$. Then we can reason as follows:

$$2+3+4+\dots+n+(n+1) = [2+3+4+\dots+n] + (n+1)$$
$$= \frac{n(n+1)}{2} + (n+1)$$
$$= \frac{(n+1)(n+2)}{2}$$

Above, we group some terms, use the assumption P(n), and then simplify. This shows that P(n) implies P(n + 1). By the principle of induction, P(n) is true for all $n \in \mathbb{N}$.

Where exactly is the error in this proof?