

Figure 1

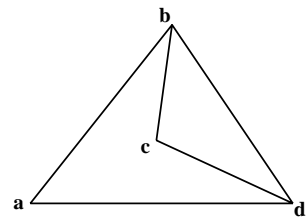


Figure 2

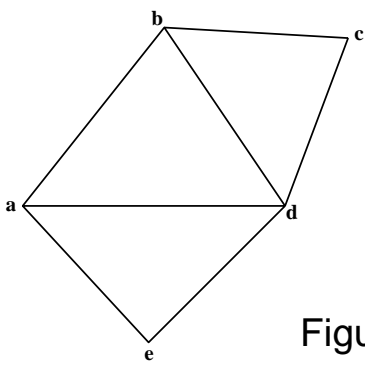


Figure 3

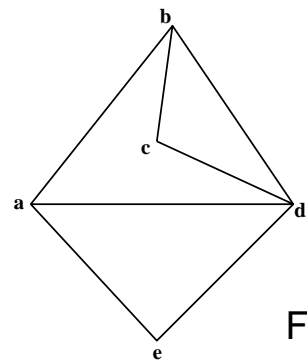


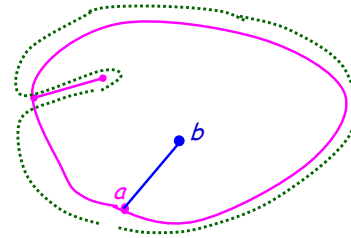
Figure 4

## Adding an edge to an embedding

- Two constructor cases:
- 1) Attach edge from vertex on a face to a new vertex.
  - 2) Attach edge between vertices on a face.

### Face Creation Rules

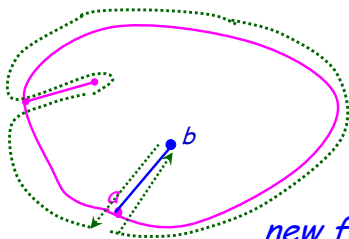
- 1) choose **face**: path  $\vec{p}$  from  $a$  to  $a$



add **edge** to **new vertex**  $b$

### Face Creation Rules

- 1) choose **face** = path  $\vec{p}$  from  $a$  to  $a$

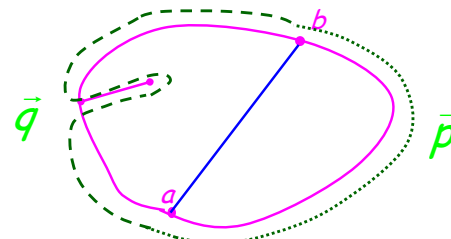


add **edge** to **new vertex**  $b$

**new face:**  
 $b\vec{p}b$

### Face Creation Rules

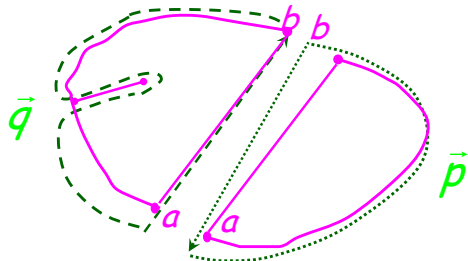
- 2) choose **face** = path  $a\vec{p}b\vec{q}a$



add **edge** across it

### Face Creation Rules

- 2) choose **face** = path  $a\vec{p}b\vec{q}a$



splits into 2 faces:  $a\vec{p}ba, ab\vec{q}a$