

6.034 Midterm Quiz 2, Spring 2012

April 17, 2012

Name:

1 (xx pts)	
2 (xx pts)	
3 (xx pts)	
4 (xx pts)	
Total	

1 Morsels (xx points)

To enable more efficient communication among the residents, your living group is developing a new form of communication – tapping on the walls. Your job is to develop an automated decoding algorithm for this communication channel. Let’s assume that our code has 3 symbols:

- **0** – a short tap on the wall
- **1** – a more prolonged scrape on the wall.
- **#** – a delay of a second which indicates an end of word.

So, a communication could be:

000000#0101000100#

This is “hi all” in our language.

The problem, of course, is that this communication channel is “noisy”: the 0 and 1 symbols may be mistaken for each other. We’ll assume that there’s a 75% chance that you will hear the correct symbol and a 25% chance that you will hear the wrong symbol.

Let’s make some simplifying assumptions: We can reliably detect the end of word (#) symbol. We never miss a symbol and we can always tell when one symbol ends and another begins. So, basically, we see a stream of 0, 1 and # symbols and we need to translate them into the most likely words using a dictionary.

Assume that we have a dictionary with N words, w_0 through w_{N-1} . For each word w_i , we have $w_i[k]$ for the k^{th} symbol (one of 0 or 1) of the i^{th} word. Furthermore, $w_i[k]$ for any k beyond the end of the word is #.

1.1 HMM

We'll define an HMM that will help us decode each word. Since the # symbol is not noisy, we can just divide the message into words and decode each word separately.

We'll assume that we can access the value of t , the current number of symbols we have seen in the word.

The state of the HMM is defined by the variable W_t , which has possible values $0, \dots, N-1$, representing the words in the dictionary. Note that the state does not change over time, because the underlying word is constant regardless of which character we are observing; W_r and W_s have the same value for any two times r and s , but we treat them as different variables because our beliefs about W_r are based on different observations than our beliefs about W_s .

E_t is the evidence variable at time t , which is simply the observed symbol at time t .

Assume all the words w_0, \dots, w_{N-1} are equally likely, and that the probability of a word does not depend on what other words are in the message.

Fill in the values of the probabilities below, based on the description above. Each answer is a single probability, either a constant or an expression involving N .

1. The sensor model for the HMM is (for $i = 0, \dots, N - 1$):

(a) If $w_i[t] = \#$ then $P(E_t = \# \mid W_t = i) =$

(b) Otherwise, $P(E_t = w_i[t] \mid W_t = i) =$

2. The transition model for the HMM is (for $i = 0, \dots, N - 1$):

$$P(W_{t+1} = i \mid W_t = i) =$$

3. The initial state distribution for the HMM is (for $i = 0, \dots, N - 1$):

$$P(W_0 = i) =$$

1.2 Decoding

Let's consider a situation where we have the following 3 words in the dictionary:

- $w_0 = 01\#\#$
- $w_1 = 10\#\#$
- $w_2 = 110\#$

Suppose that we see the following message: **11#**. Give numerical values for the state distribution at each time step.

We prefer that you use fractions for the probabilities.

	$i = 0$	$i = 1$	$i = 2$
$P(W_0 = i)$			
$P(W_1 = i \mid E_1 = 1)$			
$P(W_2 = i \mid E_1 = 1, E_2 = 1)$			
$P(W_3 = i \mid E_1 = 1, E_2 = 1, E_3 = \#)$			

Give a **short** intuitive explanation for the probabilities that you computed.

2 Planning (xx points)

When our robot from Project 3 finishes its shift at the factory, it goes home and wants to prepare a well deserved meal. But, before it can do that, you must build the planner that enables it to do this.

There are a set of fixed objects (more like locations) that we know about: TABLE1, TABLE2, STOVE1, STOVE2, SHELF1, SHELF2.

There are a set of movable objects that we know about: PAN1, PAN2, PLATE1, PLATE2, FOOD1, FOOD2.

We have the following types of assertions in the world. First some assertions indicating the “types” of the individuals:

- `stove(x)` – x is a stove
- `shelf(x)` – x is a shelf
- `table(x)` – x is a table
- `movable(x)` – x is movable
- `food(x)` – x is food
- `plate(x)` – x is a plate
- `pan(x)` – x is a pan
- `cooked(x)` – x is cooked

Then some assertions indicating relationships

- `on(obj1,obj2)` – object obj1 is on object obj2 (only one object can be on an object and every movable object must be on some object)
- `clear(x)` – there is no object on top of x.

2.1 Rules

Write rules (by specifying the preconditions and the add and delete assertions) for the following operators (you can use the variables in the argument list of the operators in your add and delete assertions):

1. `cook(f, p, s)`: where `f` is food, `p` is a pan and `s` is a stove. If the pan is on a stove and the food is on the pan, the food becomes cooked.

`cook(f, p, s)`:

Pre:

Add:

Del:

2. `puton(o1, o2, o3)`: where `o1`, `o2` and `o3` are objects, `o1` must be movable. Used to move `o1` from on `o2` to on `o3`. You can only pick up objects that are clear and put them on clear objects. The operator should update clear assertions as necessary.

`puton(o1, o2, o3)`:

Pre:

Add:

Del:

4 MDPs

Let's consider a simple 3 state MDP with two actions (L and R) – you might want to draw a picture for yourself. The transition probabilities are:

Action L:

	State 1	State 2	State 3	(outcomes)
In state 1:	0	1/4	3/4	
In state 2:	3/4	0	1/4	
In state 3:	1/4	3/4	0	

Action R:

	State 1	State 2	State 3	(outcomes)
In state 1:	0	3/4	1/4	
In state 2:	1/4	0	3/4	
In state 3:	3/4	1/4	0	

The reward in state 2 is 1 and 0 elsewhere. The discount factor is 0.5.

The utilities (values) of the states, with discount factor = 0.5, are **approximately** $U_1 = 0.5$ and $U_2 = 1.25$.

1. Show the utility (value) estimates for the first two iterations of the value iteration algorithm. To make things simpler, assume that you keep a copy of the utility estimates from the previous iteration and use those in the new iteration.

Initial:	$U[1]=0$	$U[2]=0$	$U[3]=0$
Iteration 1:	$U[1]=$	$U[2]=$	$U[3]=$
Iteration 2:	$U[1]=$	$U[2]=$	$U[3]=$

