## 1 FOL Proof - Rags $\vee$ Riches?

## (a) Unification

Find a most general unifier for each of the following pairs of sentences. Bob and Alice are constants.

$S_1$	$S_2$	Unifier
H(Bob)	H(x)	
Eq(f(Bob), Alice)	Eq(x,y)	
P(f(x), Bob)	P(Alice, x)	
Eq(f(f(Bob)), f(Bob))	Eq(f(x),x)	
P(y, Bob)	P(f(Bob), x)	

## (b) Proof

Say we have the following predicates:

H(x) x is an heir.

M(x) x is male.

P(y,x) y is in the Trump family and is the parent of x.

Eq(x,y) x and y are equal.

Convert the following English sentence into first	irst-order logic clausal forn	n.
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	person is an heir if and only if he or she is male, and has a parent from the Trump nily who is an heir.
2. A	person only has one parent from the Trump family.
	two people are Eq and one of them is an heir, the other is an heir. (That is, allow bstitutions for predicate H)
4. Eq	is symmetric.
specifics axioms t	next pages are a framework for conducting two proofs about Bob and Alice. A few about them have been stated along with axioms from the given knowledge base. All that we converted to clausal form have already been stated. You need only provide its. Be sure to note any unification substitutions you make.

Prove that Alice is not an heir.

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step	reason	result
1.	KB 4	$\neg Eq(x_1, y_1) \lor Eq(y_1, x_1)$
2.	KB 1	$\neg H(x_2) \lor M(x_2)$
3.	KB 1	$\neg H(x_3) \lor H(f(x_3))$
4.	KB 1	$\neg H(x_4) \lor P(f(x_4), x_4)$
5.	KB 1	$H(x_5) \vee \neg M(x_5) \vee \neg P(y_5, x_5) \vee \neg H(y_5)$
6.	KB 2	$\neg P(y_6, x_6) \lor \neg P(z_6, x_6) \lor Eq(y_6, z_6)$
7.	KB 3	$\neg H(x_7) \lor \neg Eq(x_7, y_7) \lor H(y_7)$
8.	KB	P(Alice, Bob)
9.	KB	$\neg M(Alice)$
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14.		

Assume that Alice is not an heir. Prove that Bob is not an heir.

step	reason	result
1.	KB 4	$\neg Eq(x_1, y_1) \lor Eq(y_1, x_1)$
2.	KB 1	$\neg H(x_2) \lor M(x_2)$
3.	KB 1	$\neg H(x_3) \lor H(f(x_3))$
4.	KB 1	$\neg H(x_4) \lor P(f(x_4), x_4)$
5.	KB 1	$H(x_5) \vee \neg M(x_5) \vee \neg P(y_5, x_5) \vee \neg H(y_5)$
6.	KB 2	$\neg P(y_6, x_6) \lor \neg P(z_6, x_6) \lor Eq(y_6, z_6)$
7.	KB 3	$\neg H(x_7) \lor \neg Eq(x_7, y_7) \lor H(y_7)$
8.	KB	P(Alice, Bob)
9.	KB	$\neg H(Alice)$
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