## Problem Set 2, Part a

Due: Wednesday, March 15, 2006
Problem sets will be collected in class. Please hand in each problem on a separate page, with your name on it.

## Reading

Localization Aspnes et. al: Theory of localization
Time Sync Elson, Girod, Estrin: RBS paper
Karp et. al: Global synchronization in sensornets

## Reading for next week

Time sync Fan, Lynch: Gradient clock sync<br>Attiya, Hay, Welch: Optimal clock sync paper<br>Topology control Li, et. al: Cone-based topology control algorithm<br>Bahramgiri et. al: Fault tolerant distributed topology control algorithm

## Problems

1. The mobile-assisted localization paper describes an algorithm for determining the distances between 2,3 , and 4 points in 3 -space, and uses this to determine coordinates for all nodes. Now suppose that we only need these algorithms to work in 2 -space.
(a) State versions of propositions 2 and 4, as needed for use in 2D.
(b) Describe how a 2D version of MAL would work, using your propositions.
(c) Describe what a 2D version of AFL would do, based on your new version of MAL.
2. A complete bipartite graph $K_{x, y}$ is a graph whose vertices can be partitioned into two sets $S_{1}$ and $S_{2}$, such that $\left|S_{1}\right|=x,\left|S_{2}\right|=y$, an edge connects each vertex in $S_{1}$ to each vertex in $S_{2}$, and there are no edges between vertices in $S_{1}$ or between vertices in $S_{2}$. Let $G=K_{2,3}$ be a complete bipartite graph.
(a) Is the graph $G$ generically rigid in two dimensions? Why or why not?
(b) Provide an example of a rigid formation in two dimensions with graph $G$.
3. In this problem, we use RBS to compute the velocity of an object tracked by a field of sensors. Consider a simple scenario consisting of four nodes, $i, j, k$ and $\ell$, as depicted below. Edges connect nodes which can directly communicate with each other. Suppose that $j$ observes an object when its clock value is 8 , and $k$ observes the same object when its clock is 18 . After this, node $\ell$ sends two reference signals. The first signal is heard by $i$ when its clock is 10 , by $j$ when its clock is 16 , and by $k$ when its clock is 24 . The second signal is heard by $i$ at $12, j$ at 18.2 , and $k$ at 25.8 . Nodes $i, j$ and $k$ use the signals to synchronize their clocks via RBS. If nodes $j$ and $k$ send $i$ their clock values when they observe the object, and $i$ knows the distance between $j$ and $k$ is 10 meters, then what does $i$ compute for the object's velocity?


Figure 1: Network for problem 2
4. Consider the method for modeling an execution of RBS as a bipartite graph, as described in the Karp paper. Let the graph shown below be the bipartite graph corresponding to some execution of RBS. Here, each circle represents a node, and each triangle represents a signal. Each edge has a variance of 1 . Compute the variance of the minimum variance unbiased estimator of $T_{p}-T_{q}$, as described in Section 3.2 of the Karp paper.


Figure 2: Graph for problem 3

