

## 6.857 - Network & Computer Security

2/15/12  
L3.1

Reminders: Mon = 66-110 Wed = 56-114  
<http://courses.csail.mit.edu/6.857>

Administrivia: Sign up on line if you haven't yet.  
Pset #1 now posted.  
No recitation this week.

Today:

- Finish material from lecture 1 (notes L1.5-L1.8)
- Encryption
- Perfect secrecy
- One-time pad (OTP)

News:

- "Traveling Light in a Time of Digital Threats" NYT 2/11/12
- "Ron was wrong, Whit is right" (Lenstra et al.)  
IACR eprint 2012/064, 2/14/12
- "Freedom to Tinker: There's no need to panic over factorable keys" 2/15/12 by N. Heninger

Reading: (highly recommended)  
Katz/Lindell chapters 1, 2, 3

Who is adversary? (Know your enemy!)

L1.5

= may be insider/outsider, vendor, ...

Examples:  
Voter may wish to sell her vote.  
Election official may be corrupt.  
Vendor may install "back door" in system.  
Eavesdropper may manipulate communications.

- what does adversary know?

Examples: system design & implementation details  
passwords  
facebook profiles of all personnel

- what resources does adversary have?

Examples:

- large computers
- ability to intercept & modify all communications
- ability to corrupt some participants  
(e.g. pay TV subscriber, voter, server, ...)

We typically make generous assumptions about adversary's abilities.

## Vocab:

L1.6

"vulnerability" = weakness that might be exploited by an adversary  
(e.g. poor password, buffer overflow possibility)

"threat" = potential violation of security policy  
(e.g. by exploiting a vulnerability)

"risk" = likelihood that threat will materialize

"risk management" = balancing one risk against another, or  
other factors, such as cost, ease-of-use,  
understandability, availability, ...

No mechanism is perfect — we build fences, not  
impenetrable walls  
(how high is fence?)

Security mechanisms may involve:

- identification of principals (e.g. "user name")
- authentication of principals (e.g. password, biometric)
- authorization: checking to see if principal is authorized for requested action
- physical protection: locks, enclosures
- cryptography: math in service of security (hard computational problems)
- economics: (note model change here: parties are self-interested, e.g. spammer, ...)
- deception: to get adversary to reveal himself or waste his efforts (e.g. honeypot)
- randomness, unpredictability: e.g. for passwords & crypto keys

## Some principles:

L1.8

- be sceptical & paranoid
- don't aim for perfection  
("there are no secure systems, only degrees of insecurity...")
- tradeoff cost / security  
("to halve the risk, double the cost... " - Adi Shamir)
- be prepared for loss
- "KISS" ("keep it simple, stupid!")
- ease of use is important
- separation of privilege - require 2 people to perform action
- defense in depth (layered defense)
- complete mediation (all requests checked for authorization)
- least privilege (don't give some more permissions than they need)
- education
- transparency (no security through obscurity)

Encryption

Goal: confidentiality of transmitted (or stored) message

Parties: Alice, Bob "good guys"  
Eve "eavesdropper", "adversary"



M = transmitted message

In basic picture above, there is nothing to distinguish Bob from Eve; they both receive message.

Could have dedicated circuits (e.g. helium-filled pipes containing fiber optic cable, ... ?) or steganography.

Crypto approach:

- Bob knows a key K that Eve doesn't
- Alice can encrypt message so that knowledge of K allows decryption.
- Eve hears ciphertext, but learns "nothing" about M.

### L3.3

With classical (non public key) crypto, Alice & Bob both know key  $K$ .

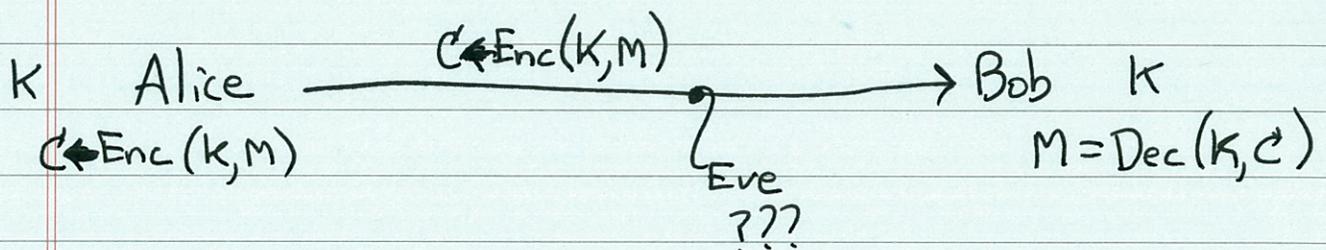
Algorithms:

$K \leftarrow \text{Gen}(1^\lambda)$	generate key of length $\lambda$ ( $\lambda$ given in <u>unary</u> )
$C \leftarrow \text{Enc}(K, M)$	encrypt message $M$ with key $K$ , result is ciphertext $C$
$M = \text{Dec}(K, C)$	decrypt $C$ using $K$ to obtain $M$

(Note Katz/Lindell convention: " $\leftarrow$ " for randomized operations,  
"=" for deterministic ones  
Often  $\xleftarrow{R}$  or  $\xleftarrow{\$}$  is used for randomized operation.)

Setup: Someone computes  $K \leftarrow \text{Gen}(1^\lambda)$   
(Someone may be Alice, or Bob)  
Ensures that Alice & Bob both have  
 $K$  (and Eve doesn't) (how!?)

Communication:



Security objective:

|| Eve can't distinguish  $\text{Enc}(k, M_1)$  from  $\text{Enc}(k, M_2)$ ,  
|| even if she knows (or chooses)  $M_1$  and  $M_2$  ( $M_1 \neq M_2$ )  
|| (of the same length).

(Encryption typically does not hide message length.)

Attacks: known ciphertext  
known CT/PT pairs } assumes K is re-used  
chosen PT  
chosen CT  
...

One-Time Pad (OTP)

- Vernam 1917 paper-tape based. Patent.
- Message, key, and ciphertext have same length ( $\lambda$  bits)
- Key  $K$  also called pad; it is random & known only to Alice & Bob.  
(Note: used by spies, key written on small pad...)

- Enc: 
$$\begin{array}{r} M = 101100\dots \quad (\text{binary string}) \\ \oplus K = 011010\dots \quad (\text{mod-2 each column}) \\ \hline C = 110110\dots \end{array}$$

- Dec: Just add  $K$  again:  $(m_i \oplus k_i) \oplus k_i = m_i$

Joke: (Desmet Crypto rump session)

OTP is weak, it only encrypts  $\frac{1}{2}$  the bits! leakage!  
Better to change them all!

Theorem: OTP is unconditionally secure.

(Secure against Eve with unlimited computing power.)

a.k.a. information-theoretically secure.

L3.6

$P(M)$  = probability of message  $M$   
(Eve's prior probability, in Bayesian sense)

$P(M|C)$  = probability of message  $M$ , having seen  $C$   
(Eve's posterior probability, in Bayesian sense)

security of OTP  $\equiv (P(M) = P(M|C))$

Adversary learned nothing about  $M$  by having seen  $C$ .

so:  $P(K) = 2^{-\lambda}$  for  $\lambda$ -bit key

$P(C)$  = probability of a given ciphertext  $C$

$$= \sum_M P(C|M) \cdot P(M)$$

$$= \sum_M 2^{-\lambda} \cdot P(M)$$

$$= \left( \sum_M P(M) \right) \cdot 2^{-\lambda} = 2^{-\lambda} \quad \text{uniform.}$$

Lemma:  $P(C|M)$  = prob of  $C$ , given  $M$   
 $= P(K = C \oplus M)$   
 $= 2^{-\lambda}$

L3.7

Now  $P(M|C) = \text{Prob of } M, \text{ given } C$

$$= \frac{P(C|M) \cdot P(M)}{P(C)}$$

Bayes' Rule

$$= \frac{2^{-\lambda} \cdot P(M)}{2^{-\lambda}}$$

$$= P(M)$$

QED

This is perfect secrecy! (except for length  $\lambda$  of  $M$ )

Compare to computational security: assumes adversary has limited computational power (e.g. can't factor large numbers)

Users need to:

- generate large secrets

- share them securely

- keep them secret

- avoid re-using them!

(google "Venona")

$$\begin{aligned} C_1 \oplus C_2 &= (M_1 \oplus K) \oplus (M_2 \oplus K) \\ &= M_1 \oplus M_2 \end{aligned}$$

Also: OTP is malleable!

Changing bit  $i$  of  $C$  causes decrypted bit  $i$  to change.