

# Geometric folding algorithms







erik D. Demaine & Joseph O'Rourke

#### 幾何的なGeometric folding algorithms 折りアルゴリズム

リンケージ,折り紙,多面体

エリック・D・ドメイン & ジョセフ・オルーク\*

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上原隆平訳

LINKAGES

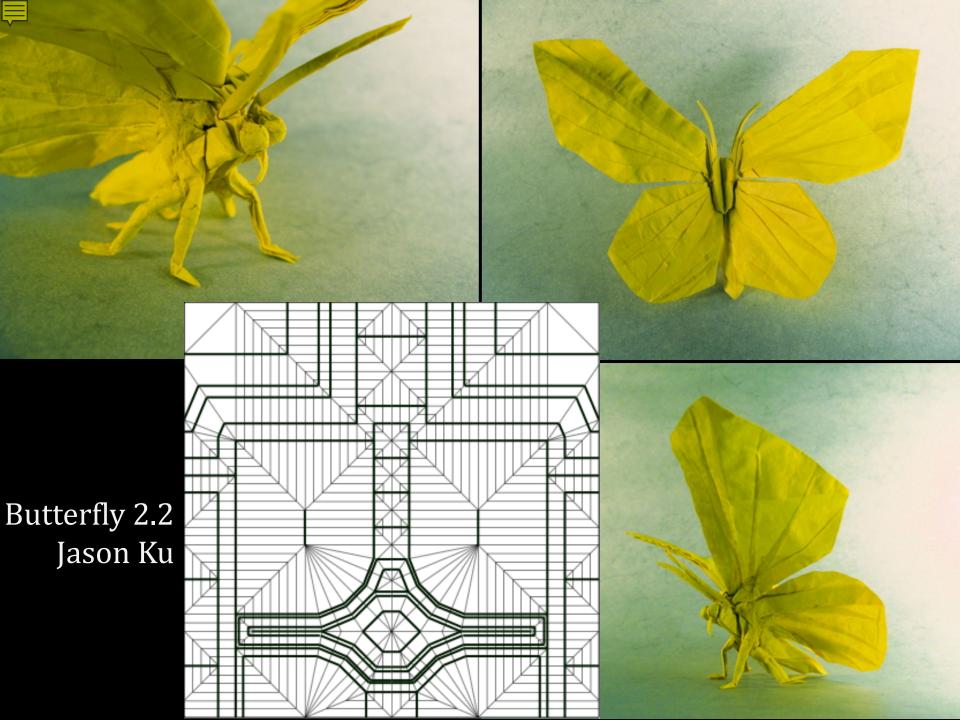


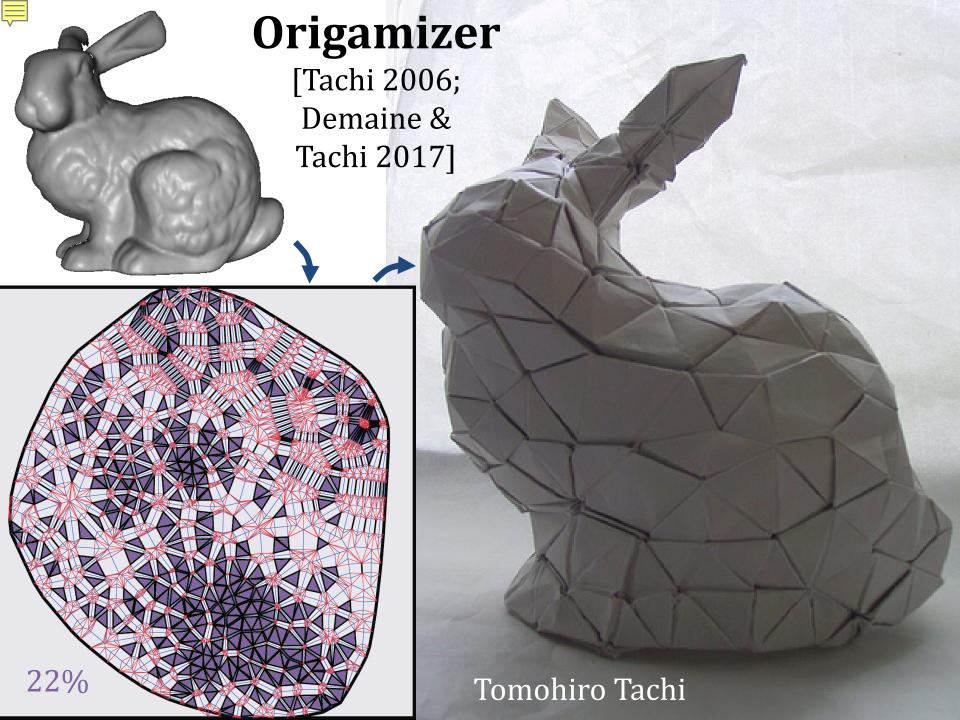
ORIGAMI,



近代科学社















## Deployable Origami Structures

5m prototype of 100m space telescope lens

[Lang & LLNL 2002]

#### Origami stent

[You & Kuribayashi 2003]

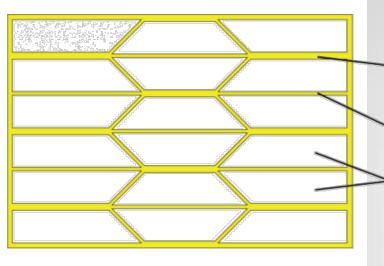






## Deployable Origami Shield

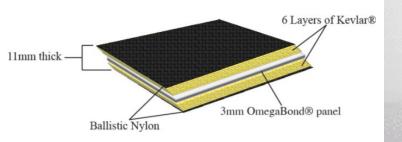
[Howell et al., BYU 2017]



Nesting Fold, Gap Size 4.5 cm

Non-Nesting Fold Gap Size 2.0 cm

Rigid Panels





# Energy **Absorbtion** [Calisch 2019] 2000 Specific Load (N/g) Al Honeycomb, 7.35 J/g500 Corrugated Al Curved Crease, 60 $^{\circ}$ , .001, 11.61 J/gCorrugated Al Curved Crease, 70 $^{\circ}$ , .001, 13.22 J/gCorrugated Al Curved Crease, 60 $^{\circ}$ , .002, 15.47 J/gDisplacement (mm)





## Printable Robots [MIT, Harvard, Penn]

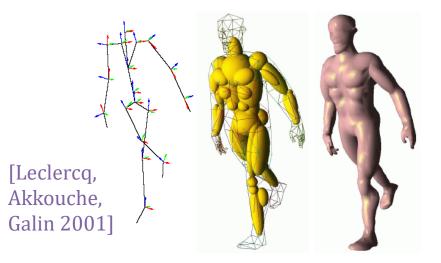




### **Applications of Linkage Folding**



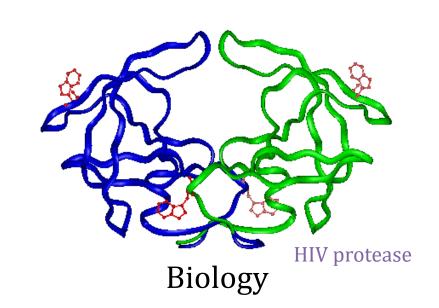
Mechanics



Graphics



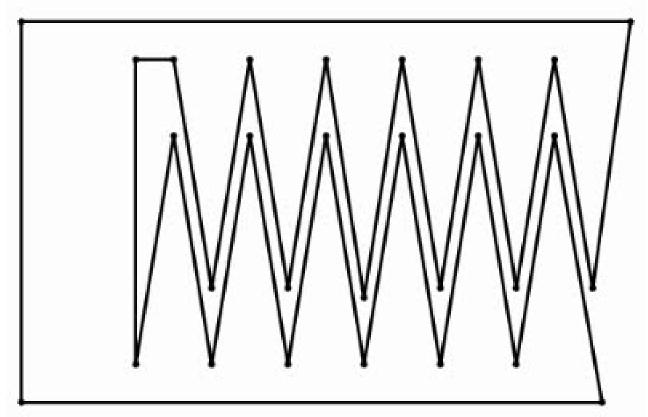
**Robotics** 





# Carpenter's Rule Theorem

[Connelly, Demaine, Rote 2000]



[Cantarella, Demaine, Iben, O'Brien 2004]



### **Hoberman Associates**





## **Applications of Polyhedron Folding**

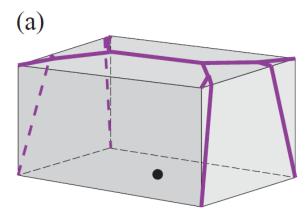


Sheet-metal manufacturing

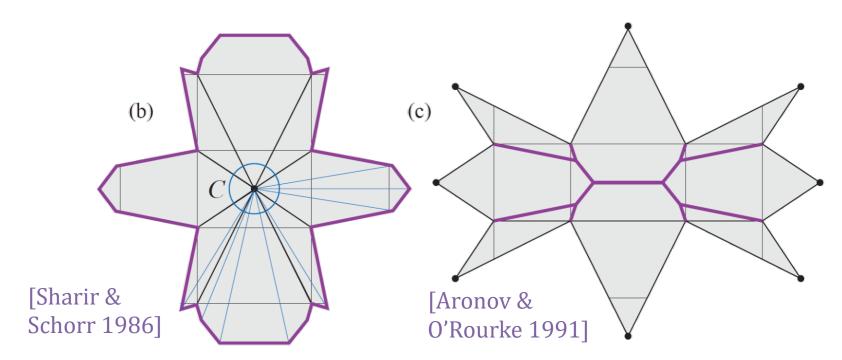


#### Theory of Unfolding Polyhedra

- Convex polyhedra always have a one-piece unfolding
- OPEN: Do general polyhedra?

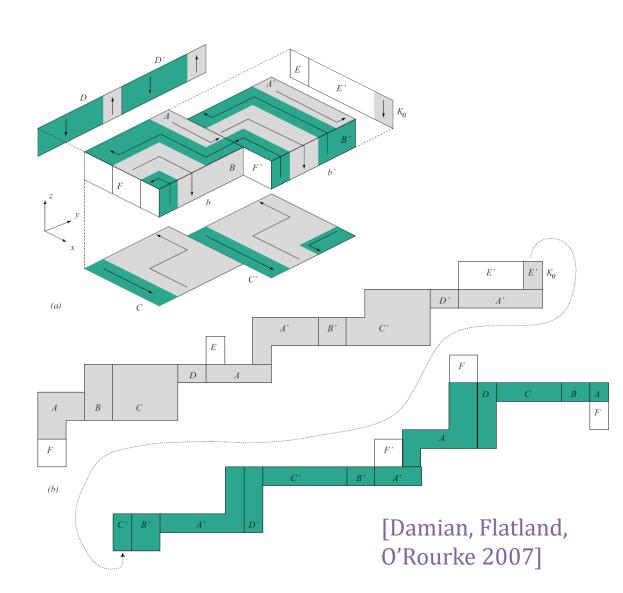


[Demaine & Lubiw 2011]



#### Theory of Unfolding Polyhedra

- Orthogonal polyhedra always have a one-piece unfolding
- OPEN: Do general polyhedra?

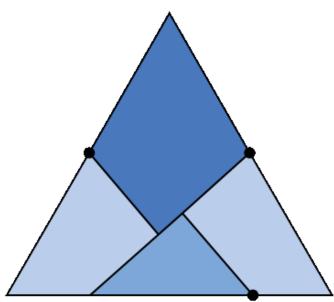


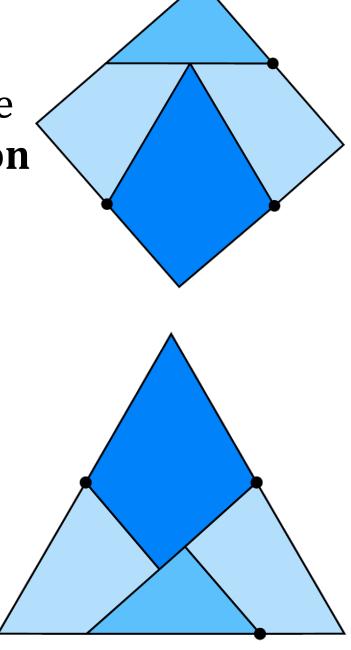


## **Hinged Dissections**

 Any two polygons of the same area have a hinged dissection

[Abbott, Abel, Charlton, Demaine, Demaine, Kominers 2008]





### http://courses.csail.mit.edu/6.849/fall20/

Mondays at 4:00pm-5:30pm Eastern and/or

Thursday, September 3, 2020 at 7:00–8:30pm Eastern

Tuesday, September 8, 2020 at 4:00–5:30pm Eastern

Alternatively, permission from the instructor.

H-level and AAGS credit

Thursdays at 7:00–8:30pm Eastern

online, using custom software

3-0-9

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**Specifics** 

**Class Time:** 

**Synchronous** Class Room:

**First Class:** 

**Units:** 

**Credit:** 

**Prerequisites:** 

**Requirements:** 

**Second Class:** 

Second Class.	raesaay, september 6, 2020 at 1.00 3.30pm Lastern
Professor:	Erik Demaine, edemaine at mit.edu
Co-lecturer:	Martin Demaine, mdemaine at mit.edu
TAs:	Yevhenii Diomidov, diomidov <i>at</i> mit.edu Klara Mundilova, kmundil <i>at</i> mit.edu
Staff Email:	6849-staff at csail.mit.edu

6.046 or equivalent background in discrete mathematics and algorithms.

• Watch all video lectures, measured by filling out Completion Forms.

(For-credit students must attend at least one. You are encouraged to attend both if possible.)

(Fill out the sign-up form and join the mailing list (see below) to get the link to the class.)

#### • Watch recorded portions of synchronous classes that you didn't attend. • Participation in synchronous classes, at least one per week (email 6849-staff about exceptions). • Participation in discussion, measured as posting or being @mentioned in at least one Coauthor post each week • Project write-up and presentation.

• Problem sets roughly weekly. The approximate breakdown of your grade is 50% project, 20% project presentation, 15% psets, and 15% partic

Grading scheme: But you cannot pass the class without participating (according to the fairly minimal requirements above).

#### http://courses.csail.mit.edu/6.849/fall20/

**Project** 

The project is the most important requirement of the course. It can take several forms:

- **Design/create** artwork, furniture, architecture, sculpture, tool, illustration, or other object based on the ideas in the class. Your work should be both aesthetically compelling and technically grounded (though the latter need not be explicitly visible). You may use any medium you wish, including virtual; the challenge of working with your format will be taken into consideration.
- Theoretical contribution to the field: tackle/solve a problem, formulate interesting open problems or conjectures, etc. You should not feel pressure in terms of grades to produce results, but you should spend substantial time thinking and trying to solve the problem. On the other hand, from past experience, we expect many such results to be produced during class time, and you are encouraged to turn those results into your project(s).
- Survey a few papers on a related topic (not already well-covered by the class or textbook).
- Design a possible new **lecture** for a future edition of this class.
- Write/record an accessible **tutorial** for teaching folding to a broad audience.
- Substantially improve the **Wikipedia** articles for several topics related to the class. Recommended only if you have existing experience editing Wikipedia and with <u>its guidelines</u>. In this case, your project write-up and presentation should summarize the changes you made, why you made the decisions you did, and any challenges you ran into, in addition to linking to new articles and change diffs.
- **Implement/visualize** one or more algorithms or results, or make a tool to help explore an open problem, from this class or on related topics. We encourage such implementations to be designed as web pages, with code written in <u>CoffeeScript</u> (see <u>our guide for Python programmers</u>) or <u>JavaScript</u>.

You are encouraged to relate the final project to your research interests, and you will not be limited to the topics discussed in class.