

# D-Forms

*Surprising New  
3-D Forms From  
Flat Curved Shapes*



**John Sharp**  
tarquin publications

*"There is no such thing as an ugly D-Form!"—Tony Wills*

**D-Form** |di'form| *n.*

1. a three-dimensional form created by joining the edges of two flat surfaces having the same perimeter length.
2. a discovery by product designer Tony Wills.
3. cut-and-assemble paper models in this book.

D-Forms are developable surfaces opening up new areas of mathematics, as well as many sculptural and design possibilities. It is surprising, given their simplicity of construction, that they have not been thought of before.

D-Forms surprise us in many ways, and you can only appreciate them by making the models. Creating D-Forms is unlike most forms of model making. A pair of shapes can be joined edge-to-edge in an infinite number of ways.

In this book you can cut and assemble ten fantastic models, and then use the templates included to make countless more.

*D-Forms surprise, confuse, and can be addictive. They are an intellectual virus; beware!*—Tony Wills, product designer

*D-Forms are the most remarkable extensions of surfaces that I have dealt with. It is surprising that such a simple idea produces such extraordinary shapes.*—David Singmaster, metagrobologist

*They are beautiful in themselves; they remind me of Brancusi's fish. It is a lovely idea.*—Michael Kidner, artist

*I can't get these shapes out of my mind. The frustrating thing is they don't need my input to be beautiful!*—Malcolm Pollard, sculptor

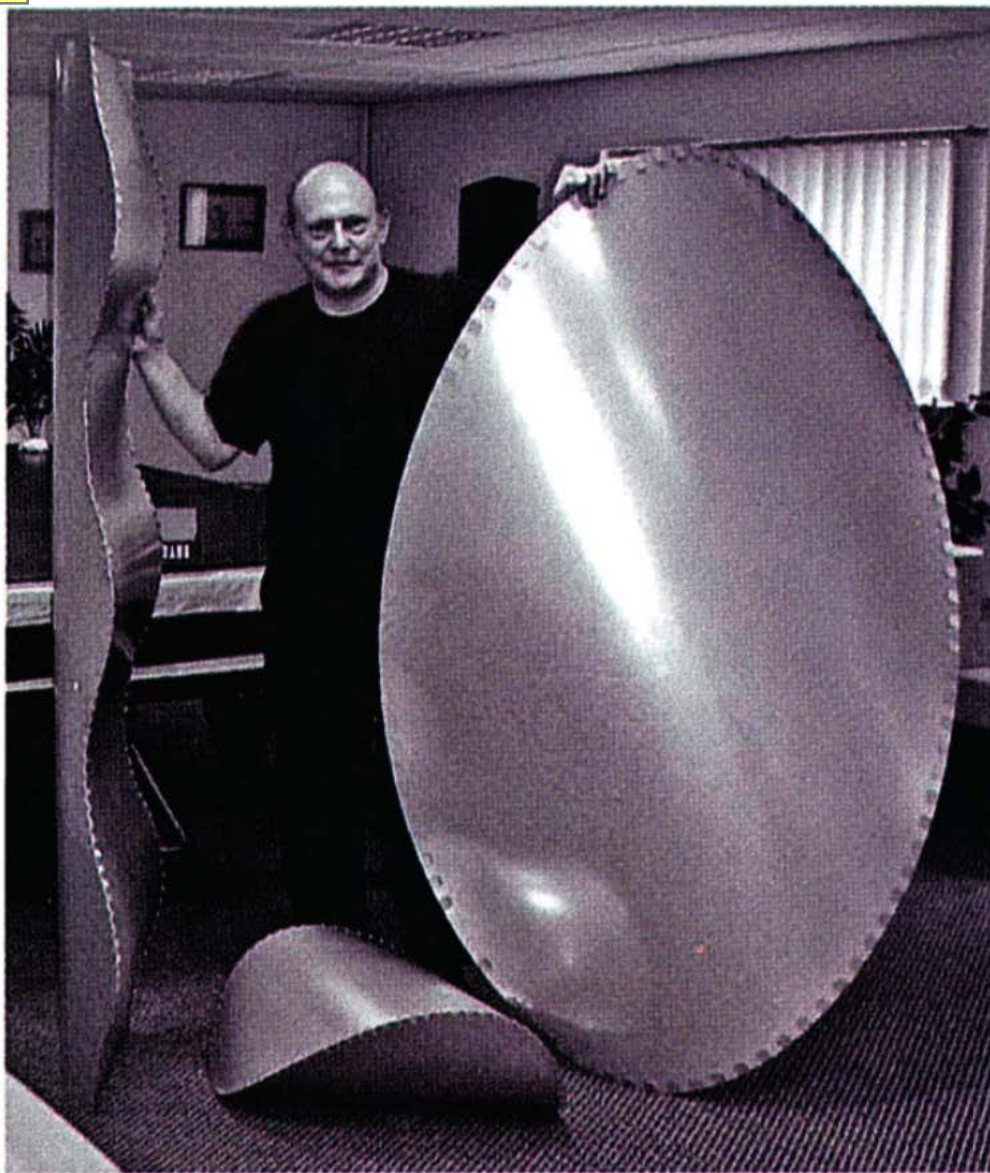


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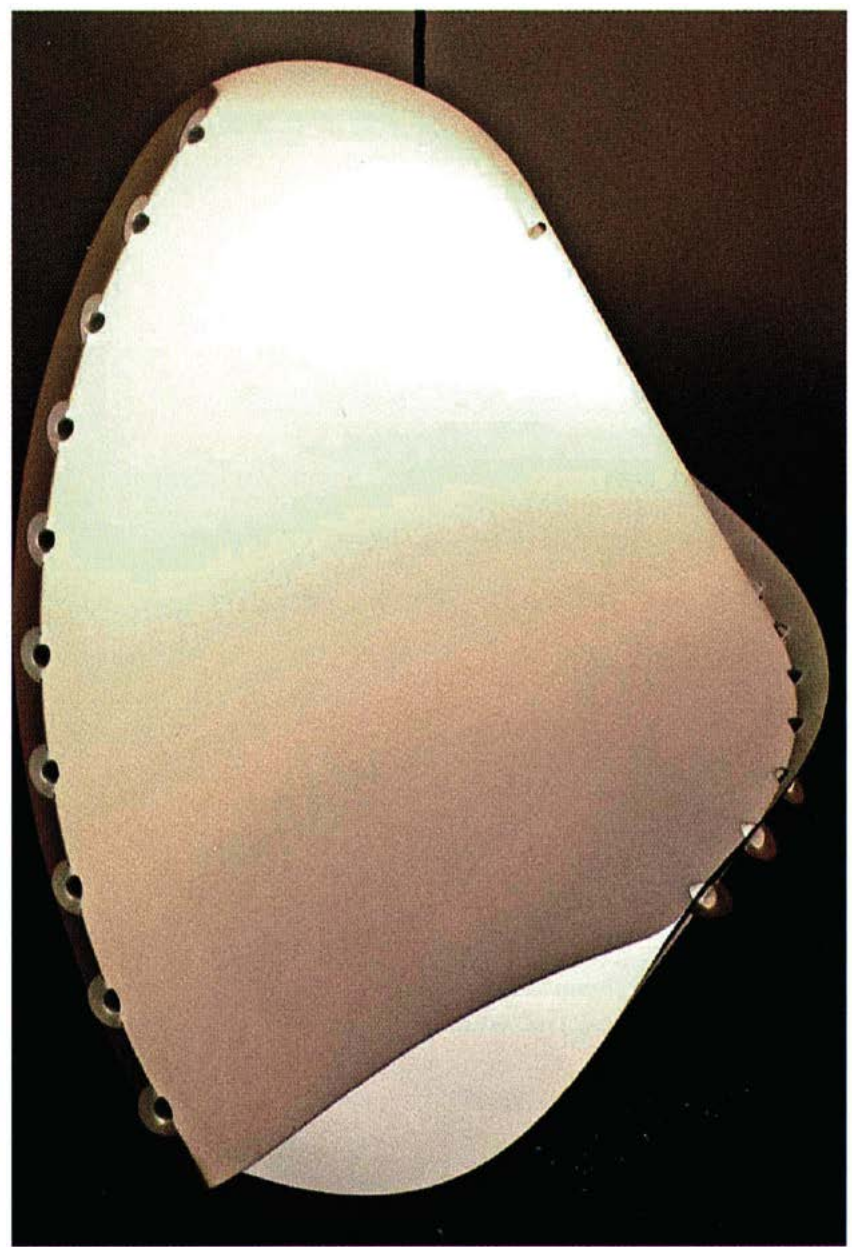
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*Tony Wills with stainless steel D-Forms.*



*Applied D-Form by Tony Wills. Luminaire lamp made from Melinex polycarbonate with glass spheres.*



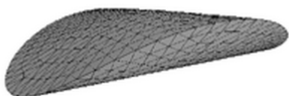
## Two ellipses

The dForm of two circles is always unexciting no matter where the initial connection is made. The next simplest shape might be considered to be two ellipses. If they are initially joined at the same position on each perimeter then the result is just a flat sheet. However if one ellipse is rotated with respect to the other before the initial join then more interesting solids result. Some computer generated examples are given below for 3 different rotation angles and two different ellipse radius ratios.

Rotation by 22.5 degrees

Ellipse radii are 0.8 and 1.0

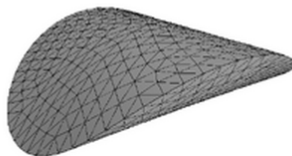
[DXF file]



Rotation by 45 degrees

Ellipse radii: 0.8 and 1.0

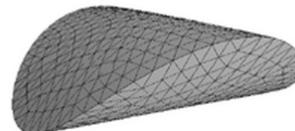
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Rotation by 90 degrees

Ellipse radii: 0.8 and 1.0

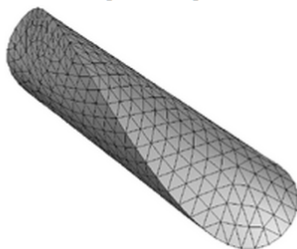
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Rotation by 22.5 degrees

Ellipse radii: 2.0 and 1.0

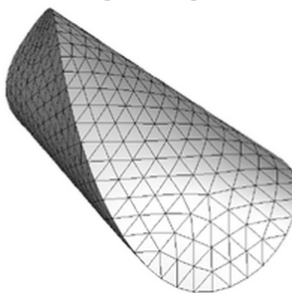
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Rotation by 45 degrees

Ellipse radii: 2.0 and 1.0

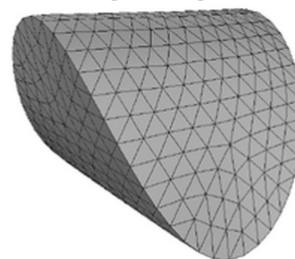
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Rotation by 90 degrees

Ellipse radii: 2.0 and 1.0

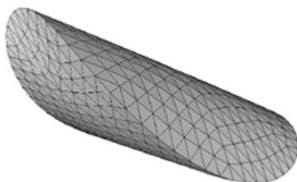
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## Ellipse and circle

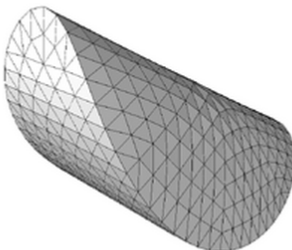
Ellipse radii ratio: 1.5 to 1

[DXF file]



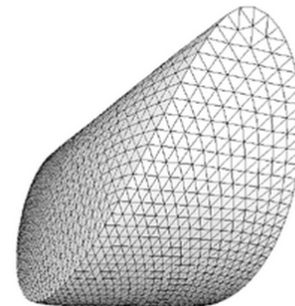
Ellipse radii ratio: 2.5 to 1

[DXF file]



Ellipse radii ratio: 4.0 to 1

[DXF file]



concept by  
Tony Wills

surface modeling  
using Evolver  
by Kenneth Brakke



# Generalized D-Forms Have No Spurious Creases

Erik D. Demaine · Gregory N. Price

Received: 21 December 2007 / Revised: 28 July 2009 / Accepted: 28 July 2009 /

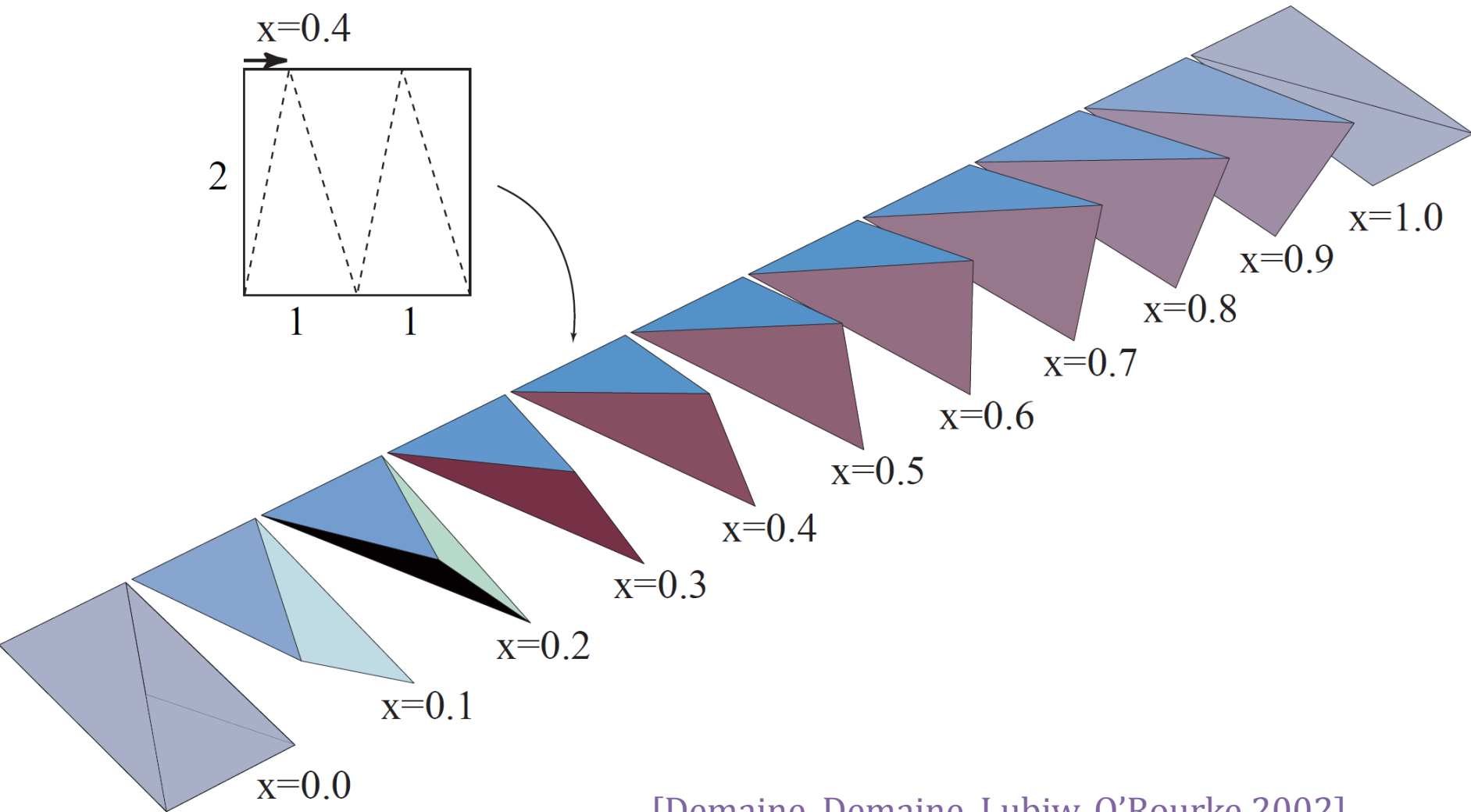
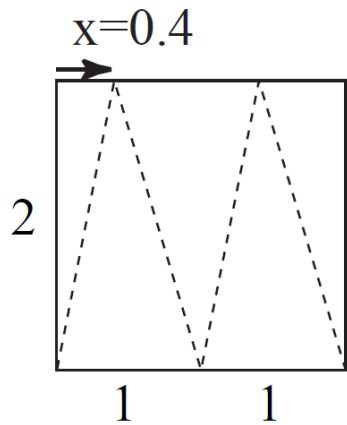
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**Abstract** A convex surface that is flat everywhere but on finitely many smooth curves (or *seams*) and points is a *seam form*. We show that the only creases through the flat components of a seam form are either between vertices or tangent to the seams. As corollaries we resolve open problems about certain special seam forms: the flat components of a D-form have no creases at all, and the flat component of a pita-form has at most one crease, between the seam's endpoints.

**Can you explain rolling belts again? I am still confused about what exactly they are.**





[Demaine, Demaine, Lubiw, O'Rourke 2002]



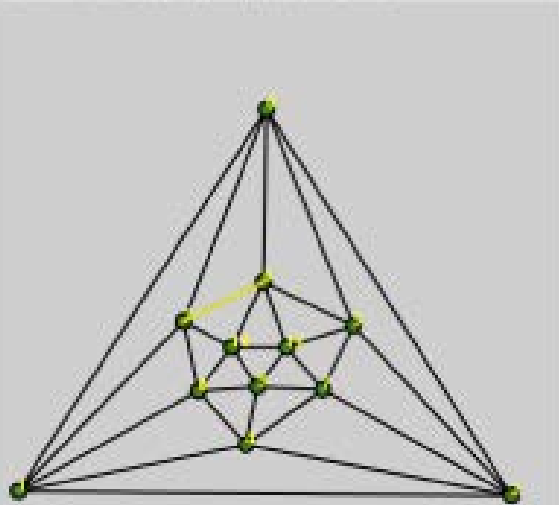
**Does that broken applet  
work now?**



Alcubierre Polypipe Solver

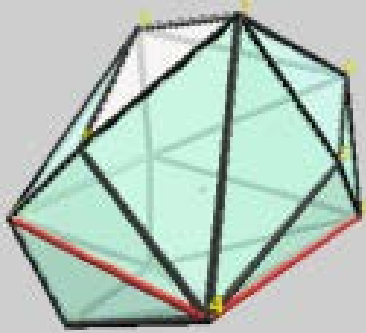
File Mode Export Help

Graph Editor



Polypipe View

Edge Length Editor



View Options

View Options	Geometry Options
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Intensity: [slider]	Alpha: [slider]
<input checked="" type="checkbox"/> Light 2	<input checked="" type="checkbox"/> Outline
Intensity: [slider]	Tubes: [slider]
	<input checked="" type="checkbox"/> Show Flipped Edges
	<input checked="" type="checkbox"/> Show Vertex Indices
	<input type="checkbox"/> Show Edge Lengths

polytop successfully calculated.

**Wait, is the convex case  
actually harder here? Can  
we hear about why the  
nonconvex case is solved?**