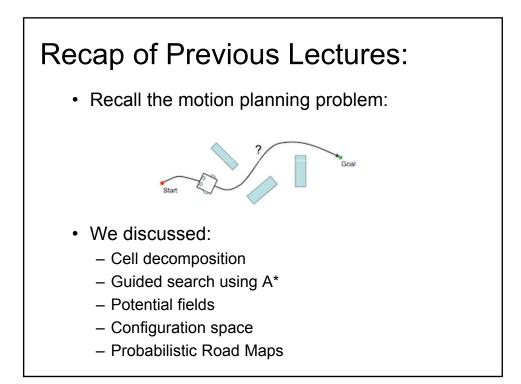
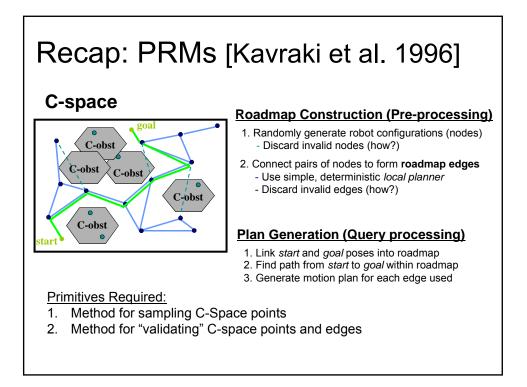
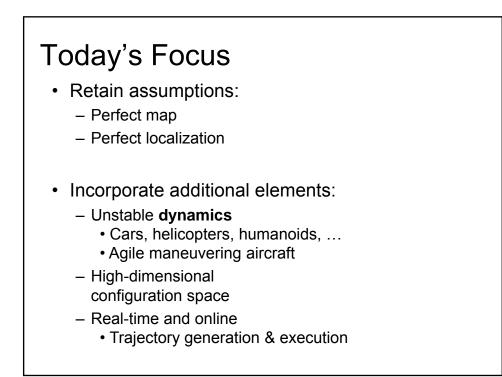


RSS Lecture 10 Monday, 10 March 2014 Prof. Seth Teller (Thanks to Sertac Karaman for animations)







Motion Planning Revisited

• Given:

- Robot's dynamics
- A map of the environment
 (perfect information, but discovered online)
- Robot's pose in the map
- A goal pose in the map

. Find a sequence of

- Actuation commands
- (such as steer, gas/brake, transmission)
- In real time (requires efficient algorithms)

... that drive system to the goal pose

• Problem is essential in almost all robotics applications irrespective of size, type of actuation, sensor suite, task domain, etc.



Practical Challenges

- **Safety:** do not collide with anything; ensure that system is stable; etc.
- **Computational effectiveness:** problem is (provably) computationally very challenging
- **Optimize:** fuel, efficiency etc. (alternative framing: not a gross waste of resources)
- Social acceptability (in human-occupied environments): motion should seem natural; robot's presence should not be rejected by humans

Different Approaches

- Algebraic Planners
- Cell Decomposition
- Potential Fields
- Sampling-Based Methods

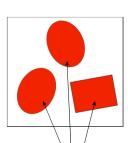
Motion Planning Approaches

Algebraic Planners

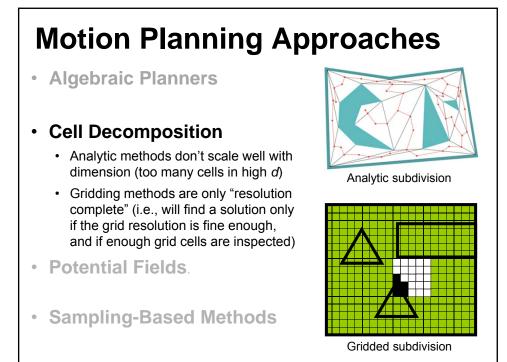
- Explicit (algebraic) representation of obstacles
- Use algebraic expressions (of visibility computations, projections etc.) to find the path
- Complete (finds a solution if one exists, otherwise reports failure)

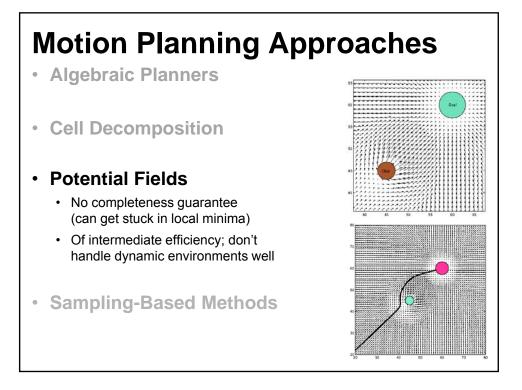
Sampling-Based Methods

- Computationally very intensive impractical
- Cell Decomposition
- Potential Fields.



- 1. Represent with polynomial inequalities
- Transform inequalities to c-space
 Solve inequalities in c-space to check feasibility and find a plan



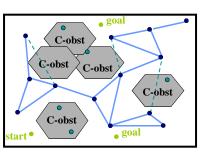


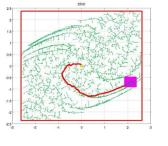
Motion Planning Approaches

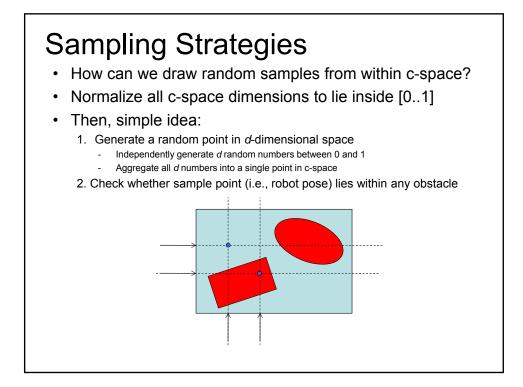
- Algebraic Planners
- Cell Decomposition
- Potential Fields

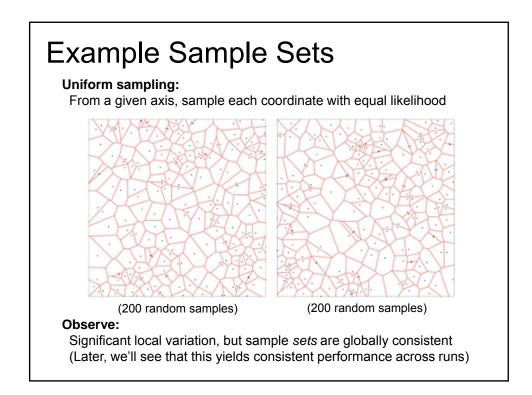
Sampling-Based Methods

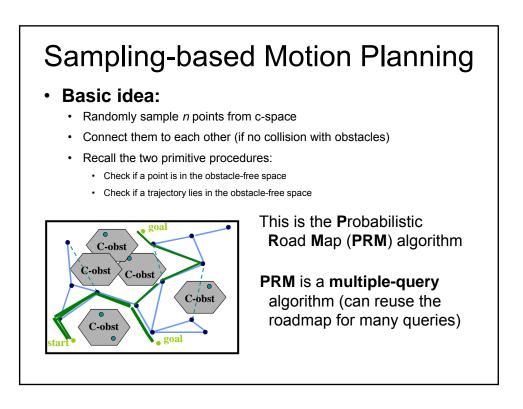
- (Randomly) construct a set of feasible (that is, collision-free) trajectories
- "Probabilistically complete" (if run long enough, very likely to find a solution)
- Quite efficient; methods scale well with increasing dimension, # of obstacles

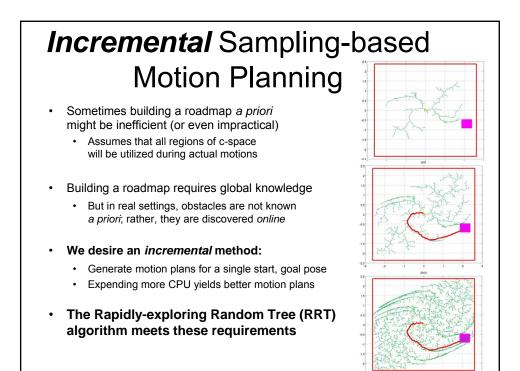


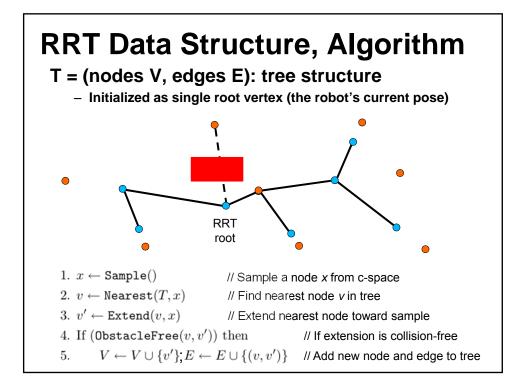








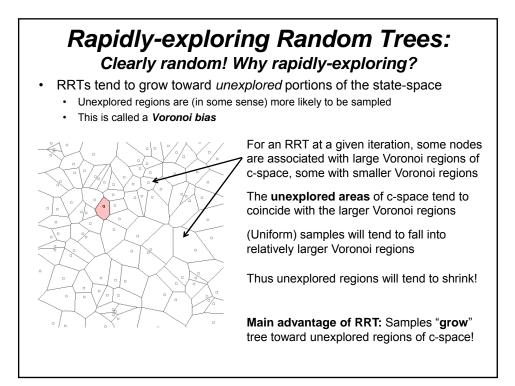


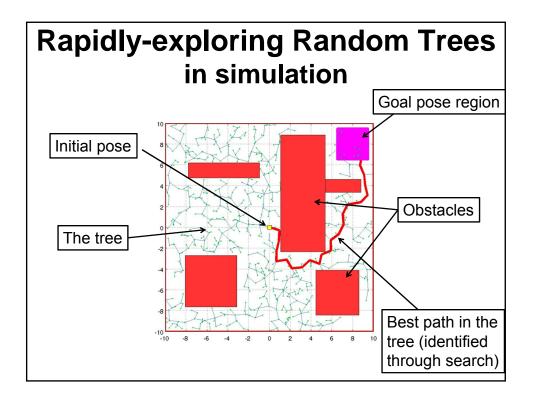


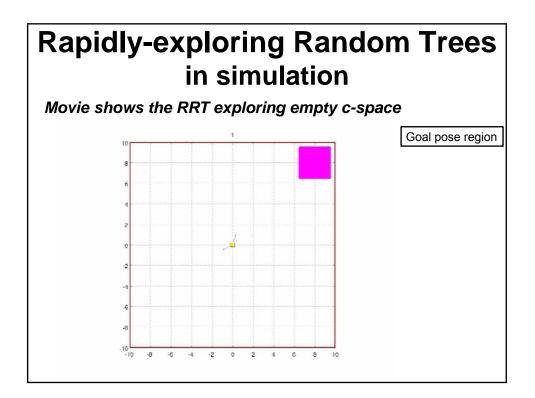
Digression: Voronoi Diagrams

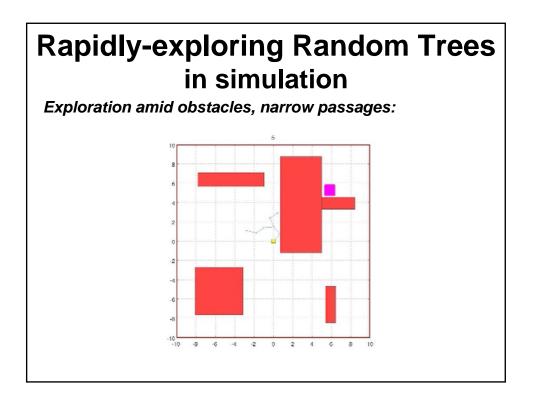
Given *n* sites in *d* dimensions, the Voronoi diagram of the sites is a partition of \mathbf{R}^d into regions, one region per site, such that all points in the interior of each region lie closer to that region's site than to any other site

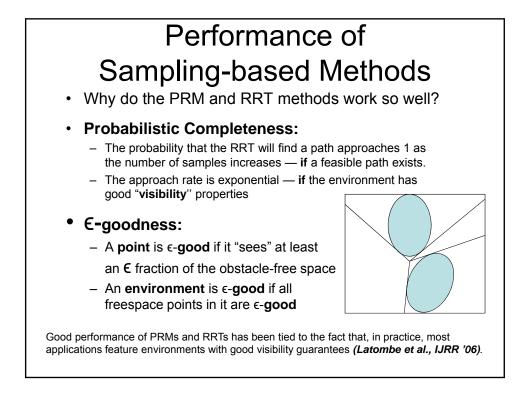
(AKA Dirichlet tesselations, Wigner-Seitz regions, Thiessen polygons, Brillouin zones, ...)

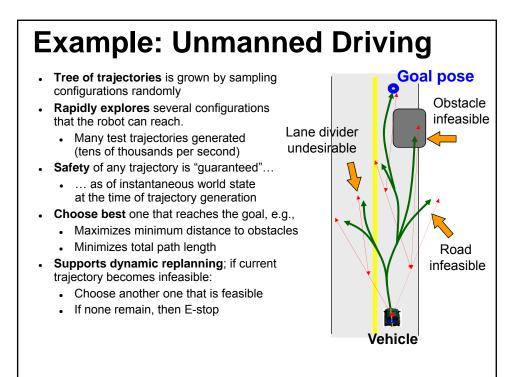










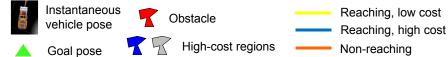


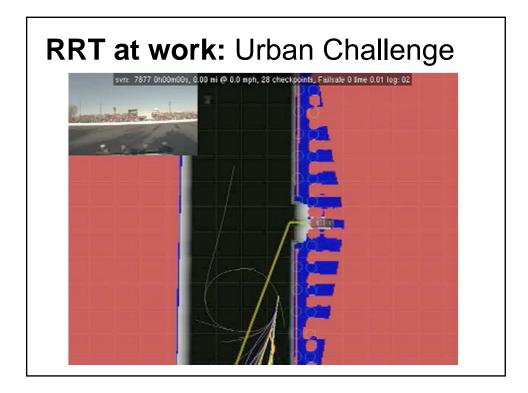
Real-world Implementation

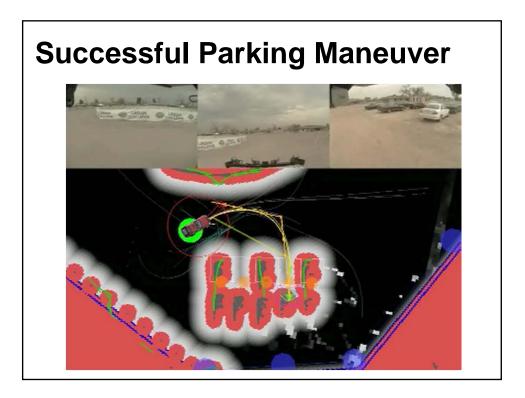
A few details:

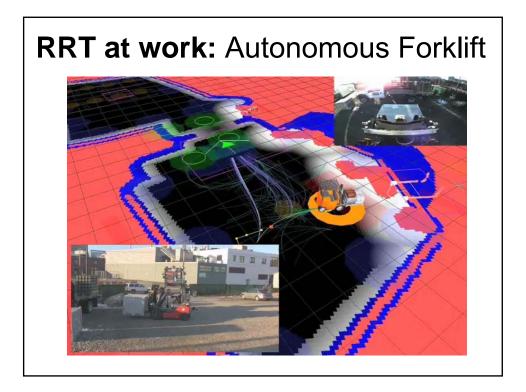
- CPU limitations and sampling method
- Dynamical feasibility constraints
- Grid map with local obstacle awareness
- Stop nodes for safety











Summary

- The Rapidly-exploring Random Tree (RRT) algorithm
- Discussed challenges for motion planning methods in real-world applications
- Intuition behind good performance of sampling-based methods
- Two applications:
 - Urban Challenge vehicle, Agile Robotics forklift