

6.141:  
Robotics systems and science  
Lecture 15:  
Grasping and Manipulation

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Spring 2009

Reading: Chapter 3, Craig: Robotics

<http://courses.csail.mit.edu/6.141/>  
Challenge: Build a Shelter on Mars

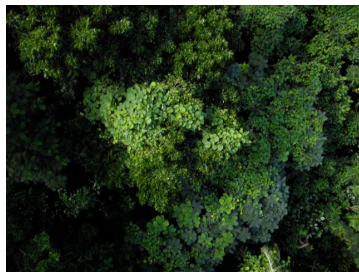
What the robot did over Spring break

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What the other robot did

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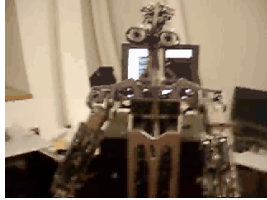
Last 2 modules were about

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- High-level planning
- Localization

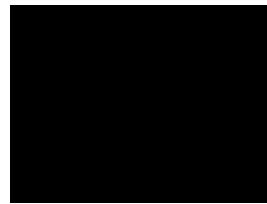
## Today

- Robot manipulation and grasping
- Applications: industrial assembly, home robots, surgery, construction, exploration, etc.
- Reading: chapters 3, 6



## What is Manipulation?

- Hayes, K.C. and Hayes, C.



## What is Robot Manipulation?

Space - in-orbit, repair and maintenance, planetary exploration anthropomorphic design facilitates collaboration with humans



**Home** - basic science - manufacturing, logistics, automated warehousing and distribution, computational models of cognitive systems, learning, human interfaces



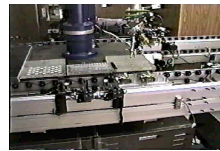
**Assistive** - clinical applications, "aging-in-place," physical and cognitive prosthetics in assisted-living facilities



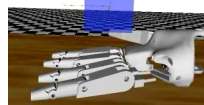
**Military** - supply chain and logistics support, re-fueling, bomb disposal



## Grasping and Manipulation Examples; why is this hard?

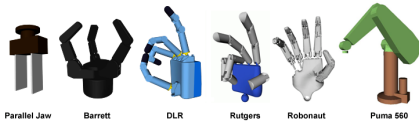


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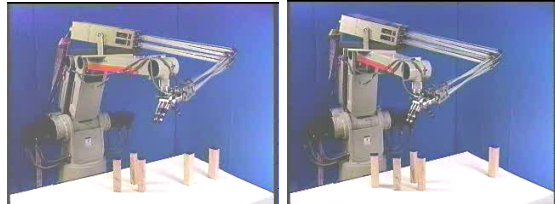


## Robot Hands

- End-effectors are the part of the robot that usually does manipulation
- Many designs...



## Problems



- How does the robot reach for the object?
- How does the robot grab the object?
- How does the robot move the object?

## Grasping

- Using end-effectors (fingers) to immobilize something relative to the hand
- Issues:
  - What contacts?
  - Where to place the contact points?
  - What grasp properties?

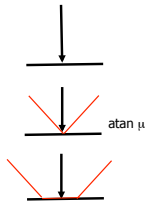


## Grasp Types

- **Force closure:** fingers resist any external force
- **Torque closure:** fingers resist any external torque
- **Equilibrium:** the contact forces can balance the object weight and external forces

## Finger types

- Point contact with friction
- Hardfinger Contact
- Softfinger Contact

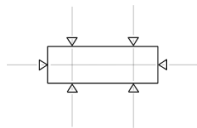


## Issues in Grasp Design

- **Existence:** given an object and constraints determine if closure exist
- **Analysis:** given an object and contacts determine if closure applies
- **Synthesis:** given an object, find contacts that result in closure

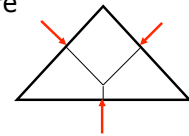
## Existence

- Given an object, does it have a force-closure grasp?
- Theorem1 (Mishra, Schwartz, Sharir): for any bounded object that is not a surface of revolution a force closure grasp exists
- Theorem2 (Mishra, Schwartz, Sharir): at most 6 fingers in 2d, 12 fingers in 3d



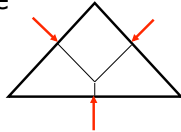
## Grasp Analysis (no friction)

- Force-direction closure

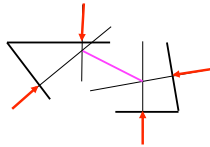


## Grasp Analysis (no friction)

- Force-direction closure



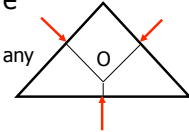
- Torque closure



## Grasp Analysis (no friction)

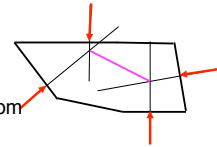
- Force-direction closure

Translate forces to O;  
they compose to generate any  
desired resultant force



- Torque closure

Translate forces to intersection  
Points; they can be adjusted to  
point at each other and away from  
each other to generate torque



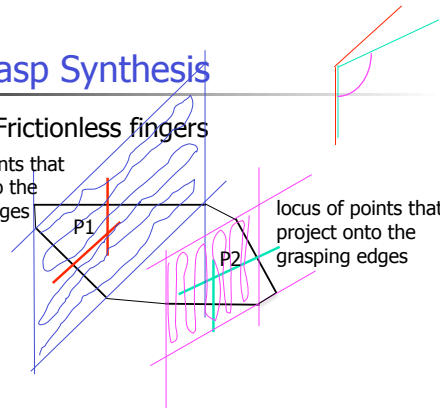
## How do we turn this into an algorithm for grasping?

- Locus of A1
- Locus of A2
- Legal directions between A1 and A2
- Then
- Pick a line
- Convert to A1, A2,
- Project to get grasping points

## Grasp Synthesis

- Frictionless fingers

locus of points that  
project onto the  
grasping edges



locus of points that  
project onto the  
grasping edges

### Grasp Synthesis

- Frictionless fingers

locus of points that project onto the grasping edges

locus of points that project onto the grasping edges

Pick P1 in blue region and P2 in pink region so that the line P1P2 has direction contained in the intersecting normal cones

### Grasp Synthesis

- Frictionless fingers

Project P1 and P2 to form grasping points f1, f2, f3, f4

### Grasp Analysis (friction)

- With friction: f1 within friction cone--stick & f1 outside friction cone--slide

Forces must be pointed at each other  
If blue force is anywhere within pink cone pink force can be pointed at it; can the blue force be pointed at pink force?

### Grasp Analysis (friction)

- With friction (stick vs slide)

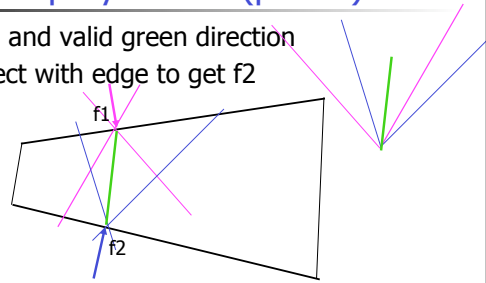
Forces must be pointed at each other  
If blue force is outside pink cone pink force can not be pointed at it because it will start slipping

### Grasp Synthesis (friction)

- 2 Finger Forces have to be within friction cones to stick
- 2 Finger Forces have to point at each other
- So...
- We need to find 2 edges with overlapping friction cones

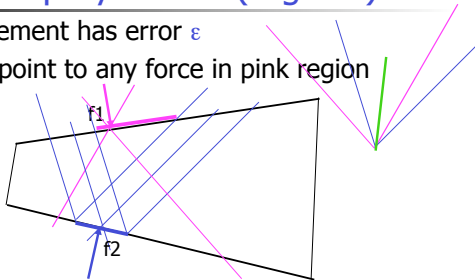
### Grasp Synthesis (points)

- Pick f1 and valid green direction
- Intersect with edge to get f2



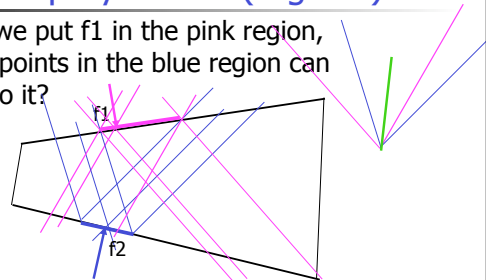
### Grasp Synthesis (regions)

- f2 placement has error  $\epsilon$
- f2 can point to any force in pink region

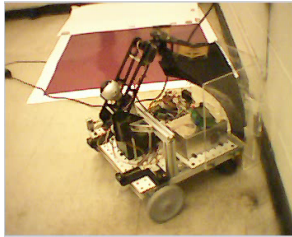


### Grasp Synthesis (regions)

- But if we put f1 in the pink region, which points in the blue region can point to it?

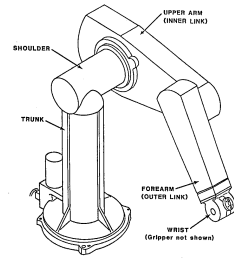


## Example: 6.141 robot



## Arm Control to Reach

- Mechanism design
- Forward kinematics
- Inverse kinematics



## Kinematic Mechanisms

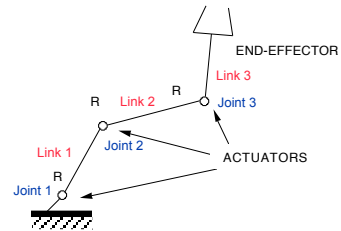
Link: rigid body  
Joint: constraint  
on two links

Kinematic mechanism:  
links and joints



## The Planar 3-R manipulator

- Planar kinematic chain
- All joints are revolute

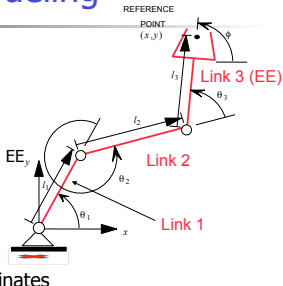




## Kinematic modeling

- Link
- Actuated joint
- End effector (EE)
  - Reference point on EE

- Joint coordinates  
 $\theta_1, \theta_2, \theta_3$
- End effector coordinates  
 $x, y, \phi$
- Link lengths ( $l$ )



## Kinematic transformations

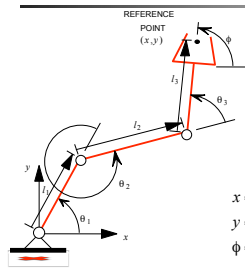
### Direct kinematics

- Joint coordinates to end effector coordinates
  - Sensors are located at the joints. DK algorithm is used to figure out where the robot is in 3-D space.
  - Robot "thinks" in joint coordinates. Programmer/engineer thinks in "world coordinates" or end effector coordinates.

### Inverse kinematics

- End effector coordinates to joint coordinates
  - Given a desired position and orientation of the EE, we want to be able to get the robot to move to the desired goal. IK algorithm used to obtain the joint coordinates.
  - Essential for control.

## Direct kinematics



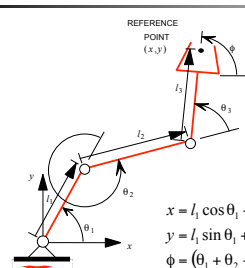
- Transform joint coordinates to end effector coordinates

$$x = l_1 \cos \theta_1 + l_2 \cos(\theta_1 + \theta_2) + l_3 \cos(\theta_1 + \theta_2 + \theta_3)$$

$$y = l_1 \sin \theta_1 + l_2 \sin(\theta_1 + \theta_2) + l_3 \sin(\theta_1 + \theta_2 + \theta_3)$$

$$\phi = (\theta_1 + \theta_2 + \theta_3)$$

## Inverse kinematics



- Transform end effector coordinates to joint coordinates

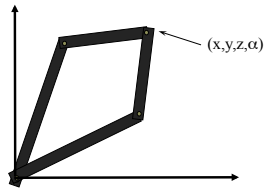
$$x = l_1 \cos \theta_1 + l_2 \cos(\theta_1 + \theta_2) + l_3 \cos(\theta_1 + \theta_2 + \theta_3)$$

$$y = l_1 \sin \theta_1 + l_2 \sin(\theta_1 + \theta_2) + l_3 \sin(\theta_1 + \theta_2 + \theta_3)$$

$$\phi = (\theta_1 + \theta_2 + \theta_3)$$

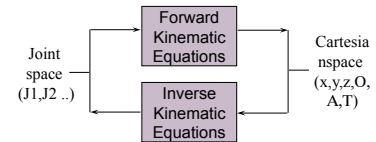
Given  $x, y, \phi$ , solve for  $\theta_1, \theta_2, \theta_3$

## Inverse kinematics has multiple solutions



Which is the correct robot pose ?

## Kinematics Summary

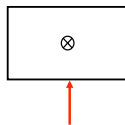


Robot kinematic calculations deal with the relationship between joint positions and an external fixed Cartesian coordinate frame.

Dynamics, force, momentum etc. are not considered.

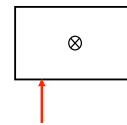
## Pushing

- Straight-line motion



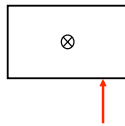
## Pushing

- Clockwise rotation



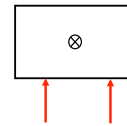
## Pushing

- Counter-clockwise rotation



## Pushing

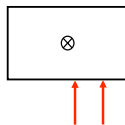
- Robust translation



What if we do not know where the center of mass is?

## Pushing

- Robust translation



Push and sense: if clockwise rotation, move right  
if counterclockwise rotation move left

## Grasping and manipulation summary

- Reaching: forward and inverse kinematics
- Grasping: analysis and synthesis of closure grasps
- Manipulation: prehensile and non-prehensile