6.141: Robotics systems and science Lecture 11: Configuration Space and Motion Planning

Lecture Notes Prepared by Daniela Rus EECS/MIT Spring 2009 Figures by Nancy Amato, Rodney Brooks, Vijay Kumar Reading: Chapter 3, and Craig: Robotics

http://courses.csail.mit.edu/6.141/
Challenge: Build a Shelter on Mars

#### Announcements

- Sign up for debates by Wed April 1 by sending email to <u>bryt@csail.mit.edu</u>
- Great Debaters (and pizza): Wed April 1 at 5:30pm (save date, location 32-D463, rsvp to Bryt)
- Read about 8 course debates at
   <u>http://courses.csail.mit.edu/6.141/sprinq2009/pub/
   debates/Debates.html
   }
  }
  </u>

Note: See Syllabus for Debate Slots





## During the last module we saw

- Control architectures: reactive, behavior, deliberative
- Visibility Graphs for Motion Planning
- Configuration Space
- Localization

## Today

- Understand c-space
- Motion planning with grids
- Probabilistic motion planning















## How do we compute C-space

- Identify dimensions
- Compute all c-obstacles















## Motion Planning Algorithm

- (1) Compute c-obstacle for each obstacle (Reflect points, Minkowsky sums, convex hull)
   (2) Find path from start to goal for point robot
- The robots DOF dictate (1)
- The method for (2) differentiates among motion planning algorithms





### How hard is this to compute? The Complexity of Motion Plannin

# Most motion planning problems are PSPACE-hard [Reif 79, Hopcroft et al. 84 & 86]

The best deterministic algorithm known has running time that is exponential in the dimension of the robot's C-space [Canny 86]

C-space has high dimension - 6D for rigid body in 3-space
 simple obstacles have complex C-obstacles minimum impractical to compute
explicit representation of freespace for high dof robots

So ... attention has turned to approximation and randomized algorithms which

- trade full completeness of the planner
- for a major gain in efficiency









#### Probabilistic Road Maps (PRM) for finding paths [Kavraki at al 96] C-space Roadmap Construction (Pre-processing) 1. Randomly generate robot configurations (nodes) - discard nodes that are invalid C-obs 2. Connect pairs of nodes to form **roadmap** - simple, deterministic *local planner* (e.g., straightline) - discard paths that are invalid C-obst C-obst C-obst C-obst Query processing 1. Connect start and goal to roadmap Find path in roadmap between start and goal regenerate plans for edges in roadmap Primitives Required: 1. Method for Sampling points in C-Space

- 2. Method for 'validating' points in C-Space









