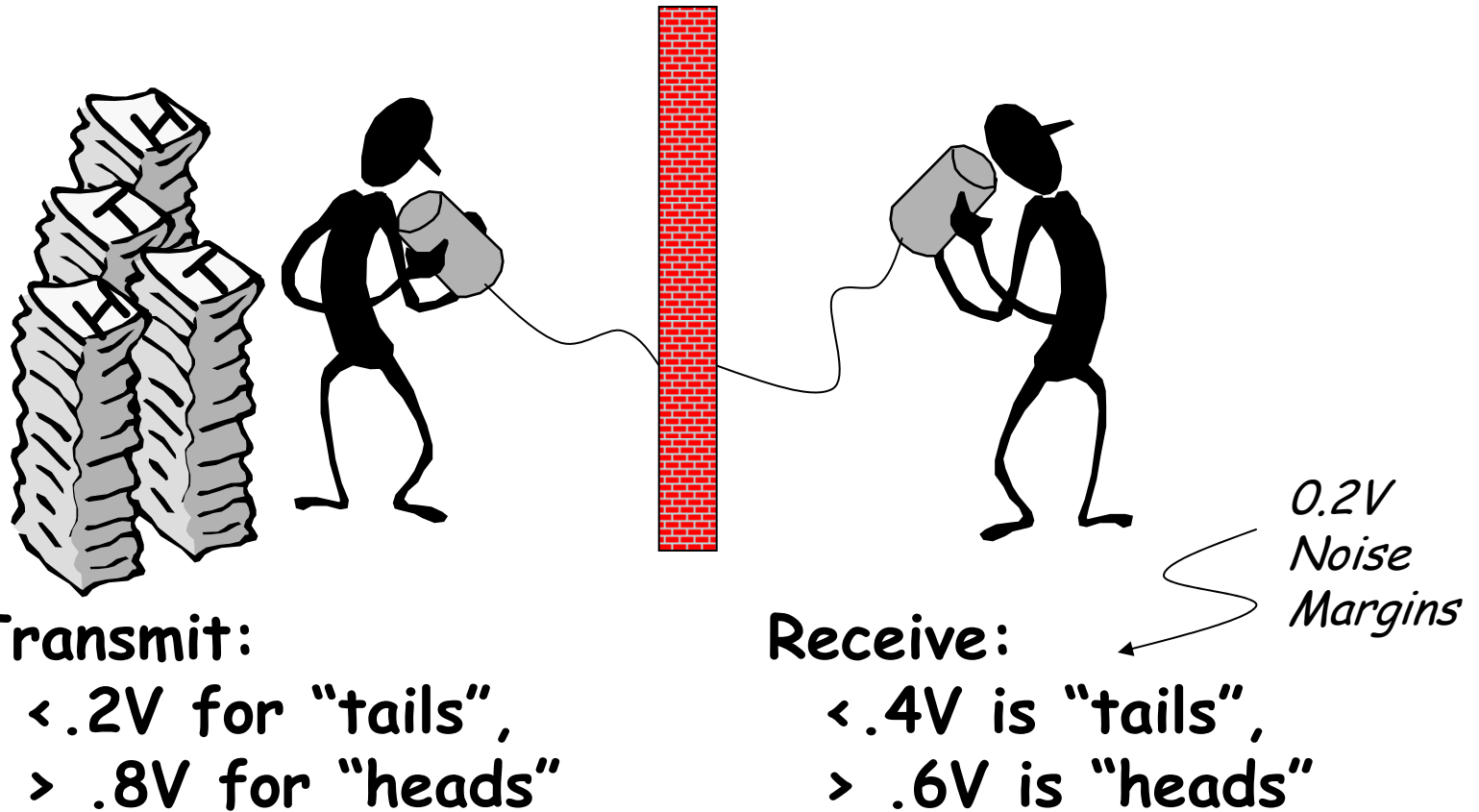


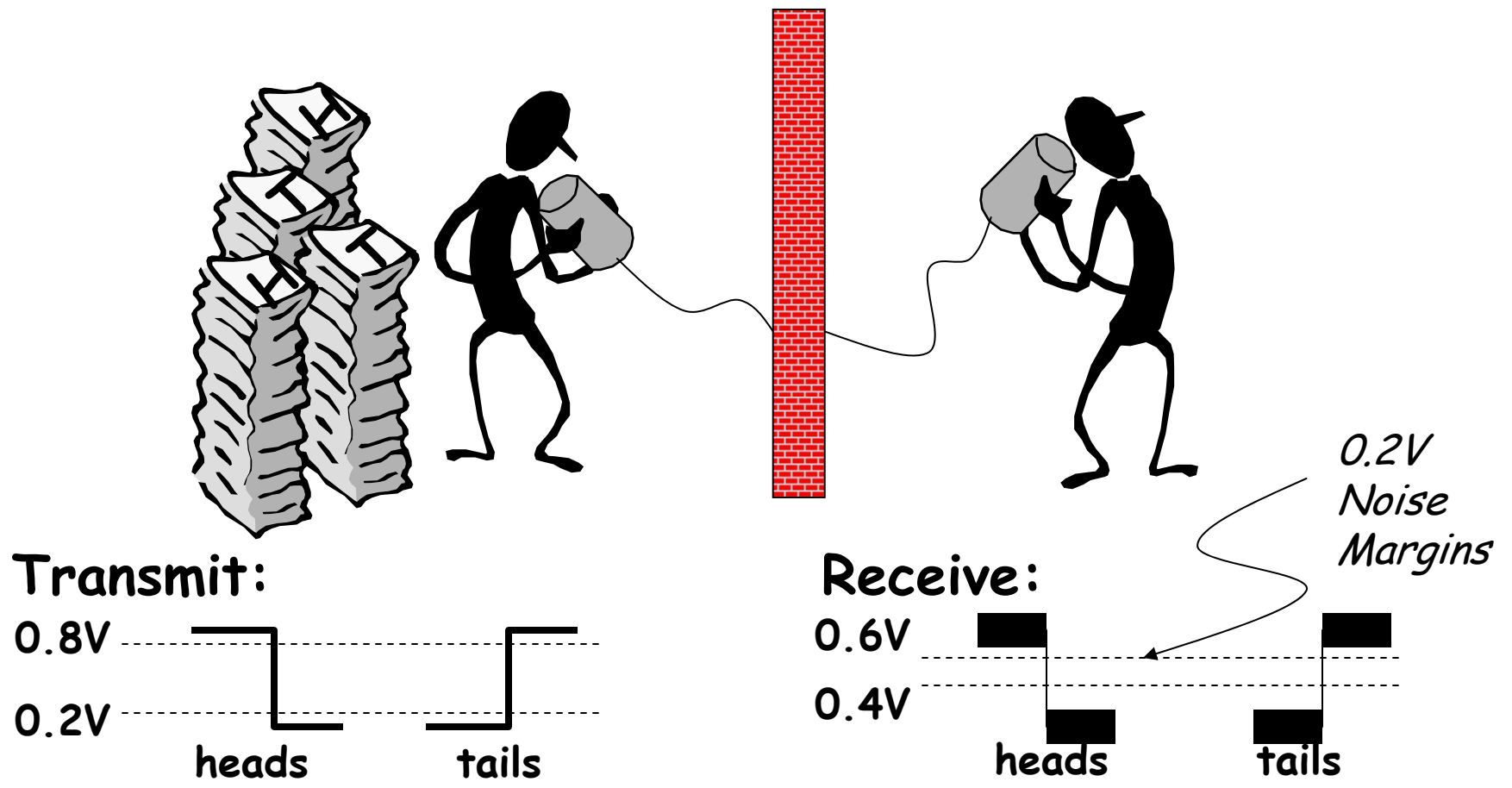
Experiment #2: Digital Encoding



100 coin flips → one transmission for each flip

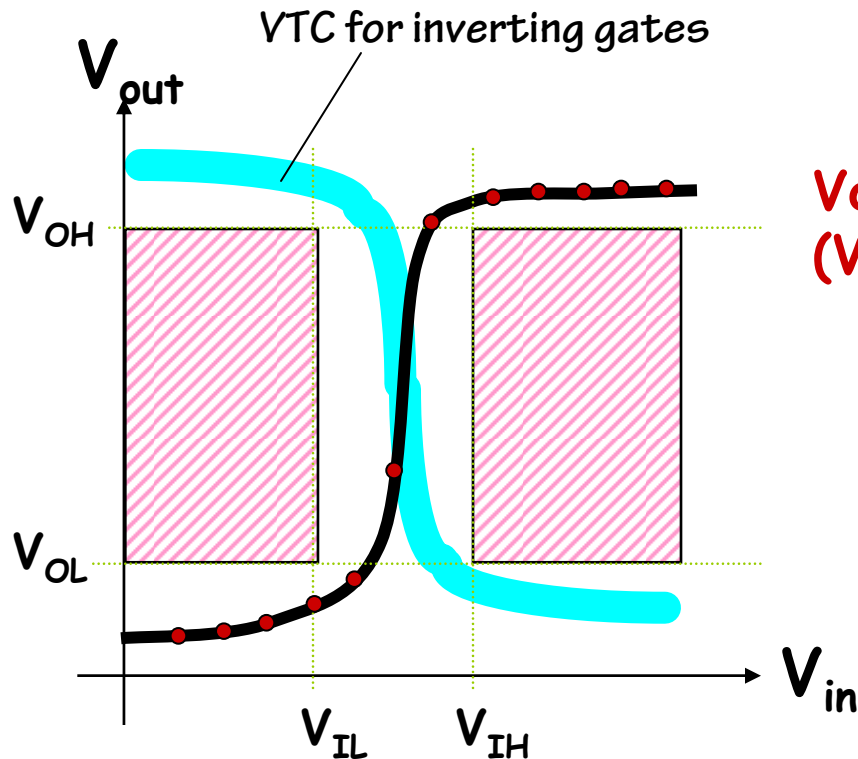
✓ But when does receiver make measurements?
Is "HT" or "HHHTTT"?

Experiment #3: Manchester Encoding



100 coin flips → one transmission for each flip
Receiver can tell when new information is present.

Example device: A Buffer



Voltage Transfer Characteristic (VTC):

Plot of V_{out} vs. V_{in} where each measurement is taken after any transients have died out.

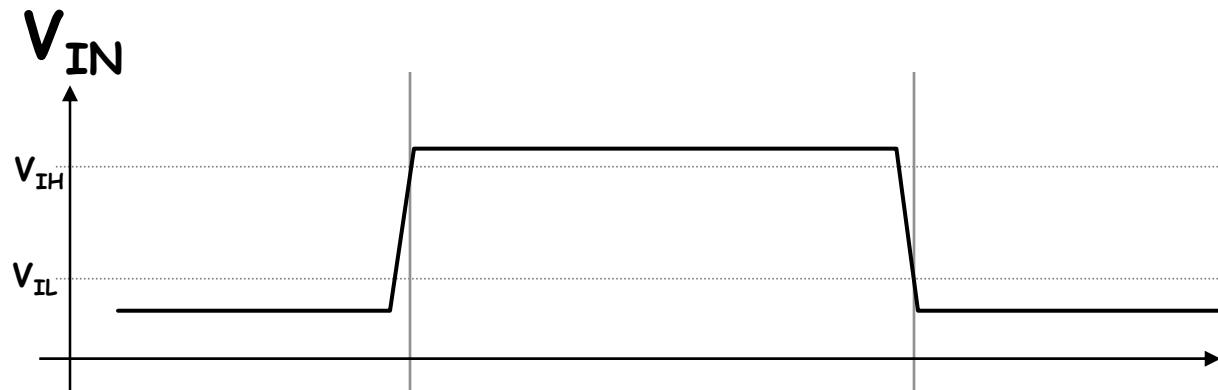
Note: VTC does not tell you anything about how fast a device is—it measures static behavior not dynamic behavior

Static Discipline requires that we avoid the shaded regions aka “forbidden zones”), which correspond to *valid* inputs but *invalid* outputs. Net result: combinational devices must have **GAIN > 1** and be **NONLINEAR**.

Due to unavoidable delays...

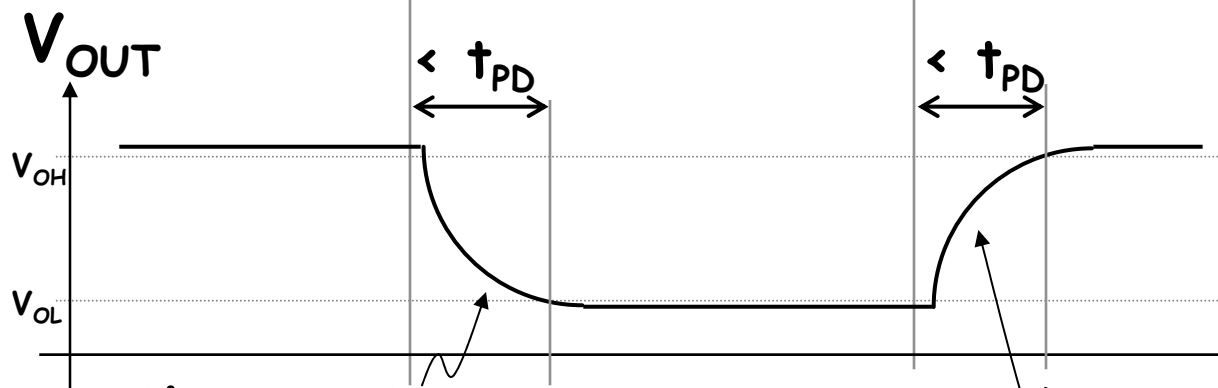
Propagation delay (t_{PD}):

An **UPPER BOUND** on the delay from valid inputs to valid outputs.



GOAL:

minimize
propagation
delay!



ISSUE:

keep
Capacitances
low and
transistors
fast

time constant

$$\tau = R_{PD} \cdot C_L$$

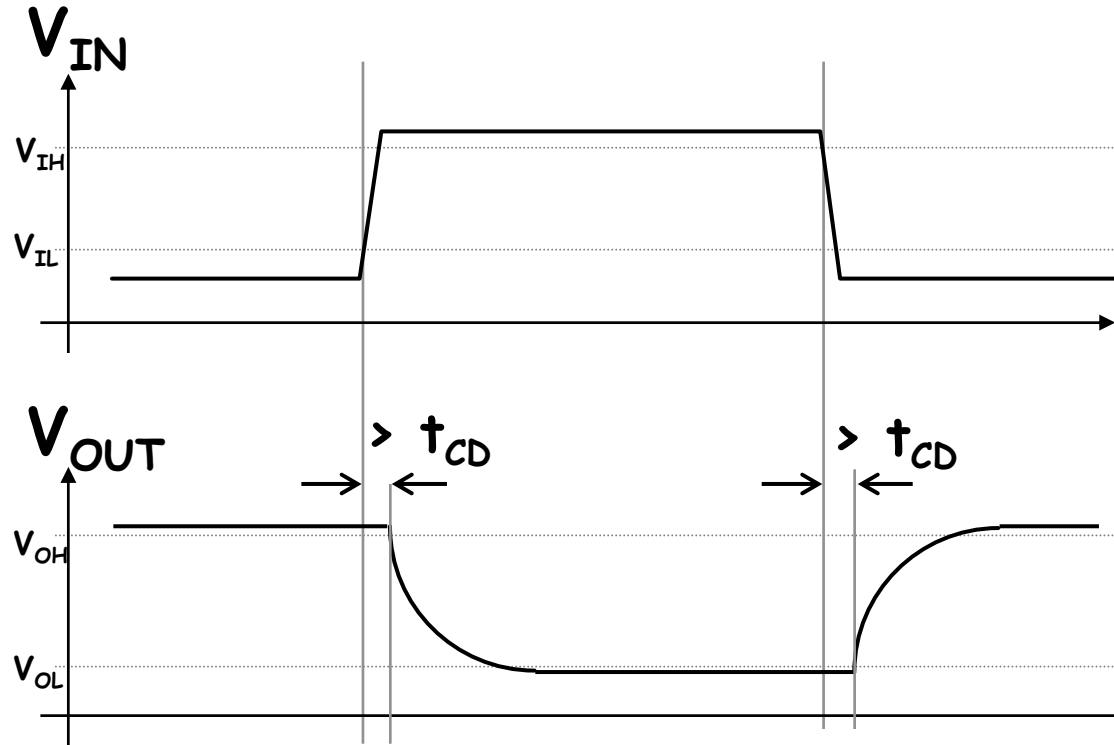
time constant

$$\tau = R_{PU} \cdot C_L$$

Contamination Delay

an optional, additional timing spec

INVALID inputs take time to propagate, too...



Do we really need t_{CD} ?

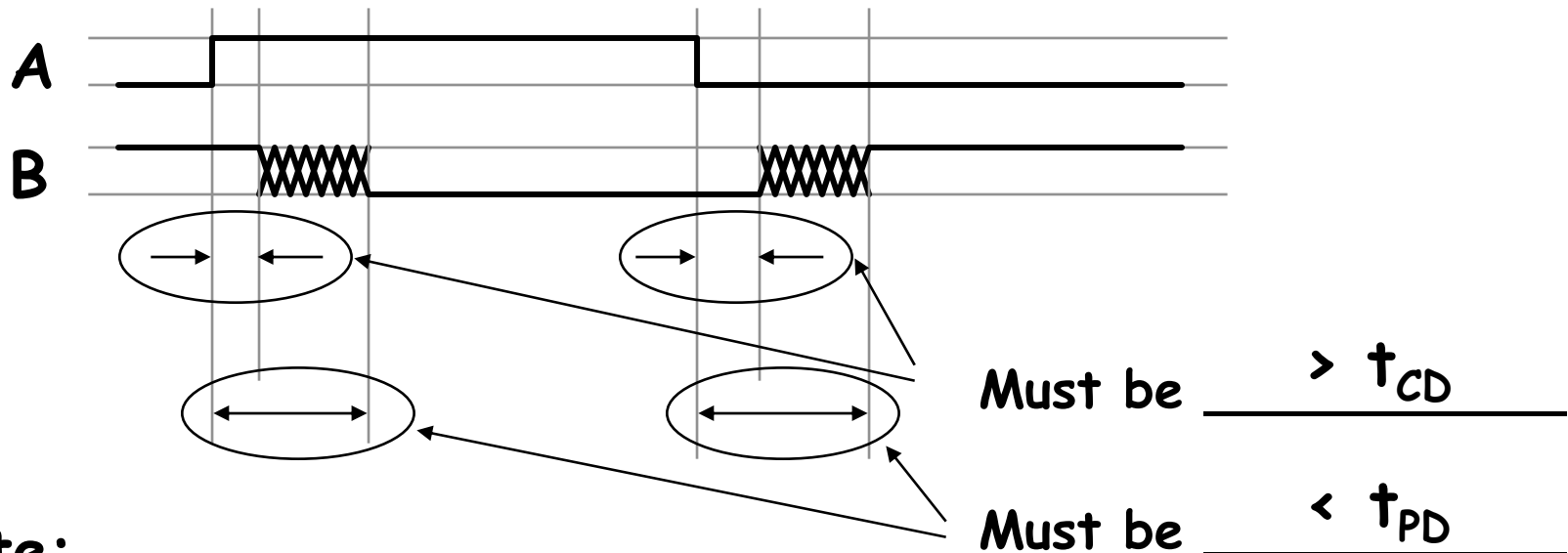
Usually not... it'll be important when we design circuits with registers (coming soon!)

If t_{CD} is not specified, safe to assume it's 0.

CONTAMINATION DELAY, t_{CD}

A LOWER BOUND on the delay from any invalid input to an invalid output

The Combinational Contract



Note:

1. *No Promises* during XXXXXX
2. Default (conservative) spec: $t_{CD} = 0$

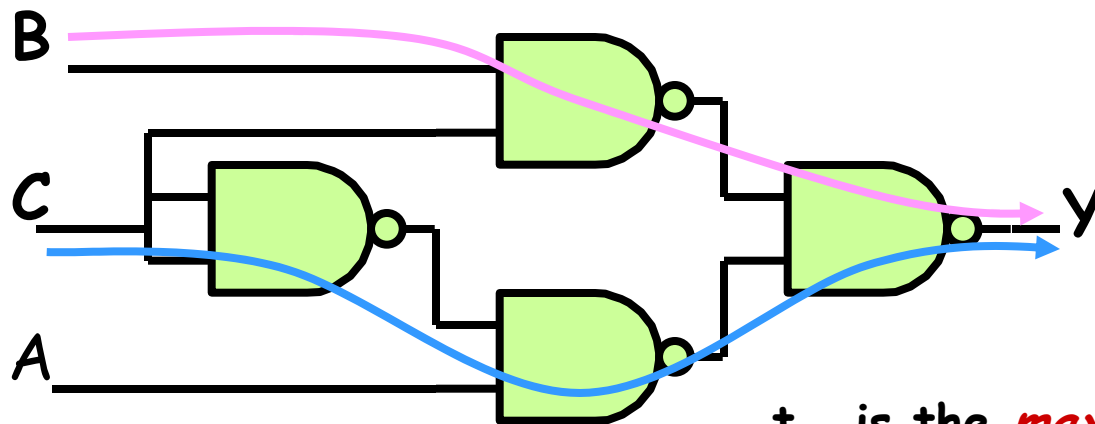
Example: Timing Analysis

If NAND gates have a $t_{PD} = 4\text{nS}$ and $t_{CD} = 1\text{nS}$

t_{CD} is the *minimum* cumulative contamination delay over all paths from inputs to outputs

$$t_{PD} = \underline{12} \text{ nS}$$

$$t_{CD} = \underline{2} \text{ nS}$$

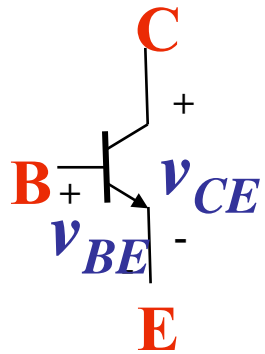


t_{PD} is the *maximum* cumulative propagation delay over all paths from inputs to outputs

The “perfect” logic family

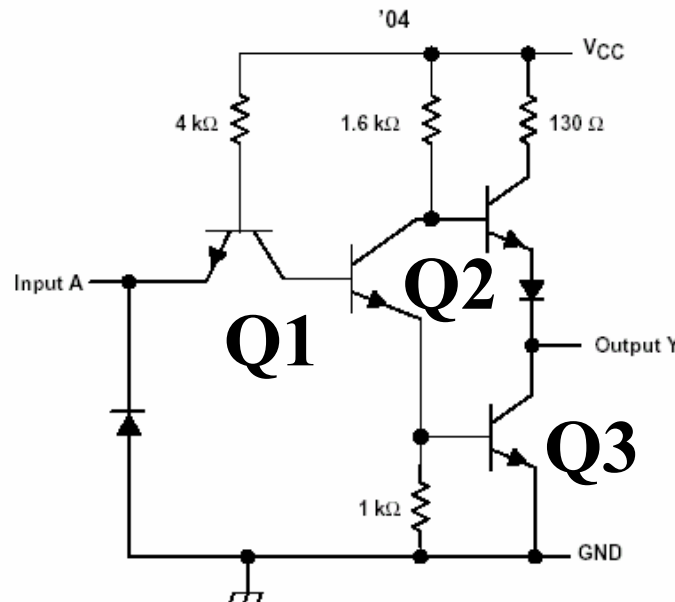
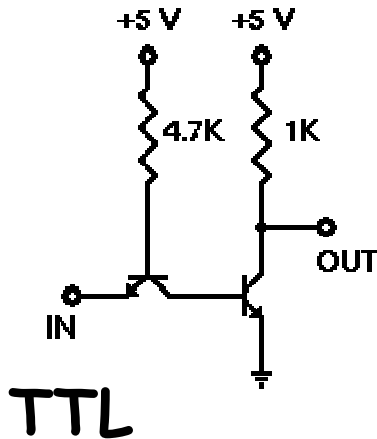
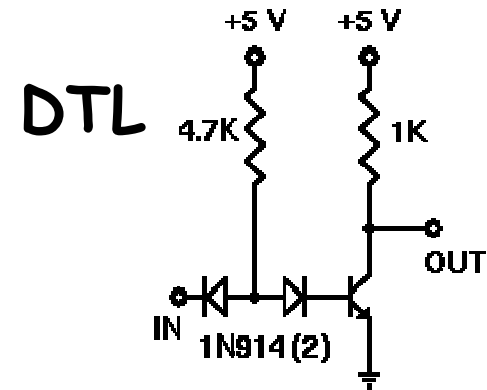
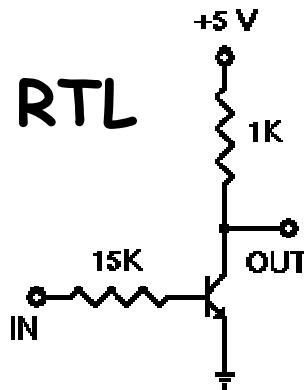
- **Good noise margins (want a “step” VTC)**
- **Implement useful selection of (binary) logic**
 - INVERTER, NAND, NOR with modest fan-in (4? Inputs)
 - More complex logic in a single step? (minimize delay)
- **Small physical size**
 - Shorter signal transmission distances (faster)
 - Cost proportional to size (cheaper)
- **Inexpensive to manufacture**
 - “print” technology (lithographic masks, deposition, etching)
 - Large-scale integration
- **Minimal power consumption**
 - Portable
 - Massive processing without meltdown

Transistor-transistor Logic (TTL)

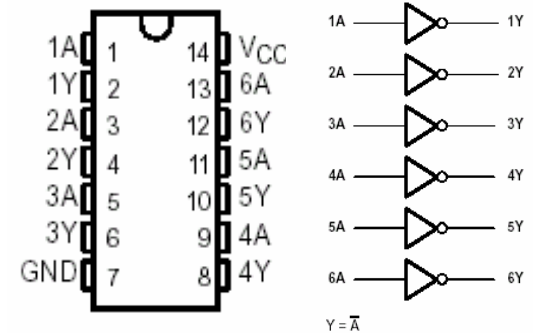


NPN BJT

$$I_{CE} = \beta I_{BE}$$



TTL w/ totem pole outputs
("on" threshold = 2 diode drops)



74LS04
(courtesy TI)

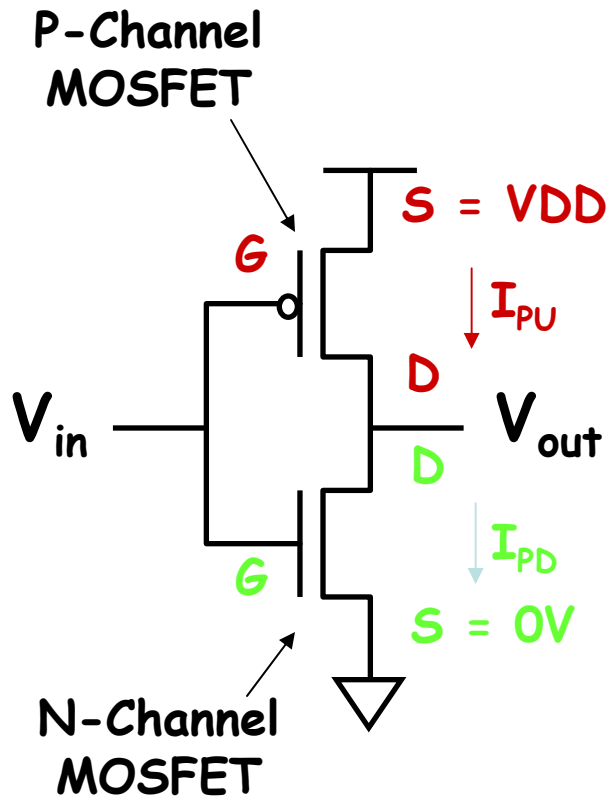
TTL Signaling

- Typical TTL signaling spec
 - $I_{OL} = 16\text{mA}$, $I_{OH} = -0.4\text{mA}$ ($V_{OL}=0.4\text{V}$, $V_{OH}=2.7\text{V}$, $V_{CC}=5\text{V}$)
 - $I_{IL} = -1.6\text{mA}$, $I_{IH} = 0.04\text{mA}$ ($V_{IL}=0.8\text{V}$, $V_{IH}=2.0\text{V}$)
 - Switching threshold = 1.3V
- Each input requires current flow (I_{IL}, I_{IH}) and each output can only source/sink a certain amount of current (I_{OL}, I_{OH}), so

Max number of inputs that can be driven by a single output is $\min(-I_{IL}/I_{OL}, -I_{IH}/I_{OH}) \approx 10$.

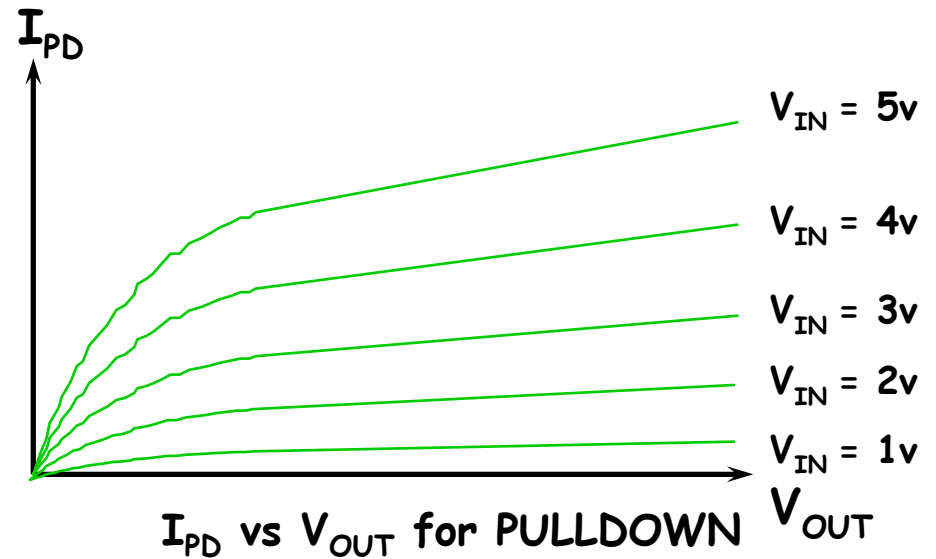
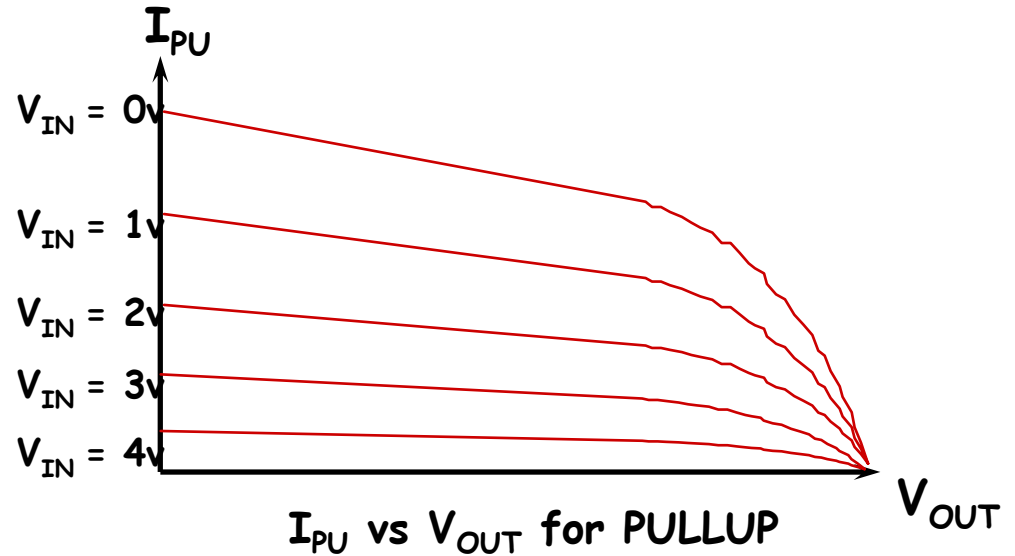
- Current-based logic \rightarrow power dissipation even in steady state.

Complementary MOS Logic

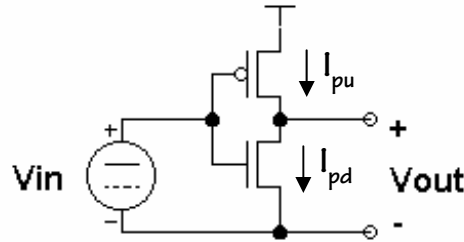
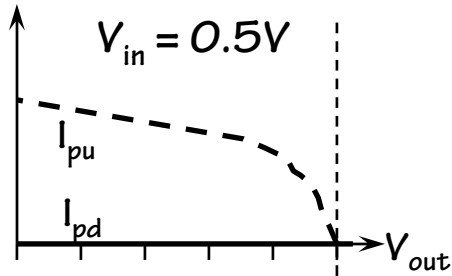


MOSFET:

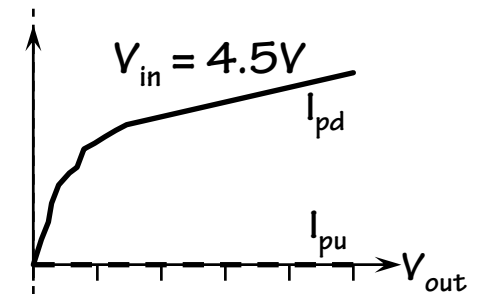
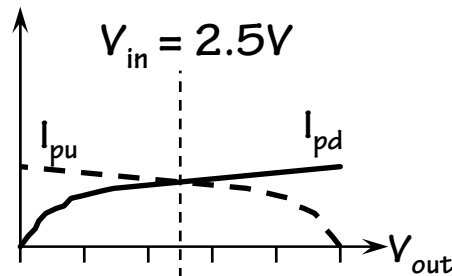
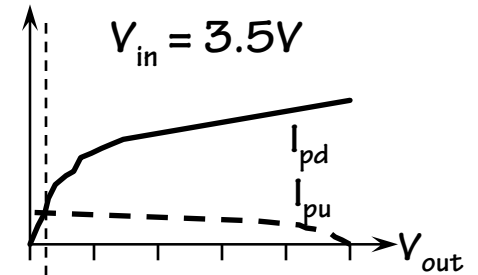
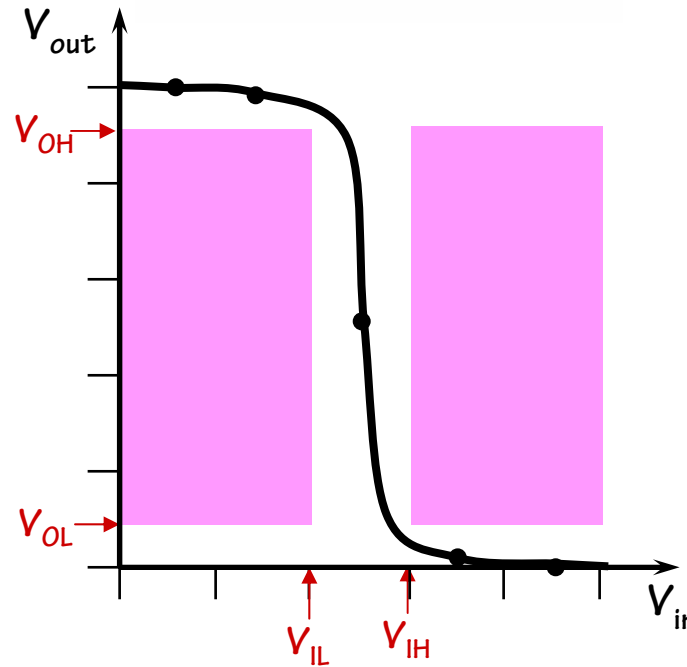
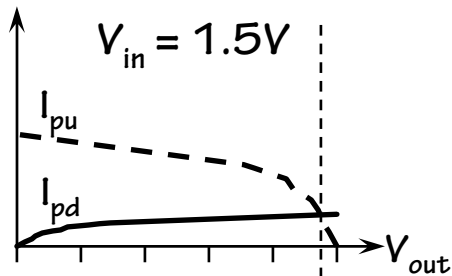
$$I_{DS} = f(V_{GS}, V_{DS})$$



CMOS Inverter VTC



Steady state reached when V_{out} reaches value where $I_{pu} = I_{pd}$.



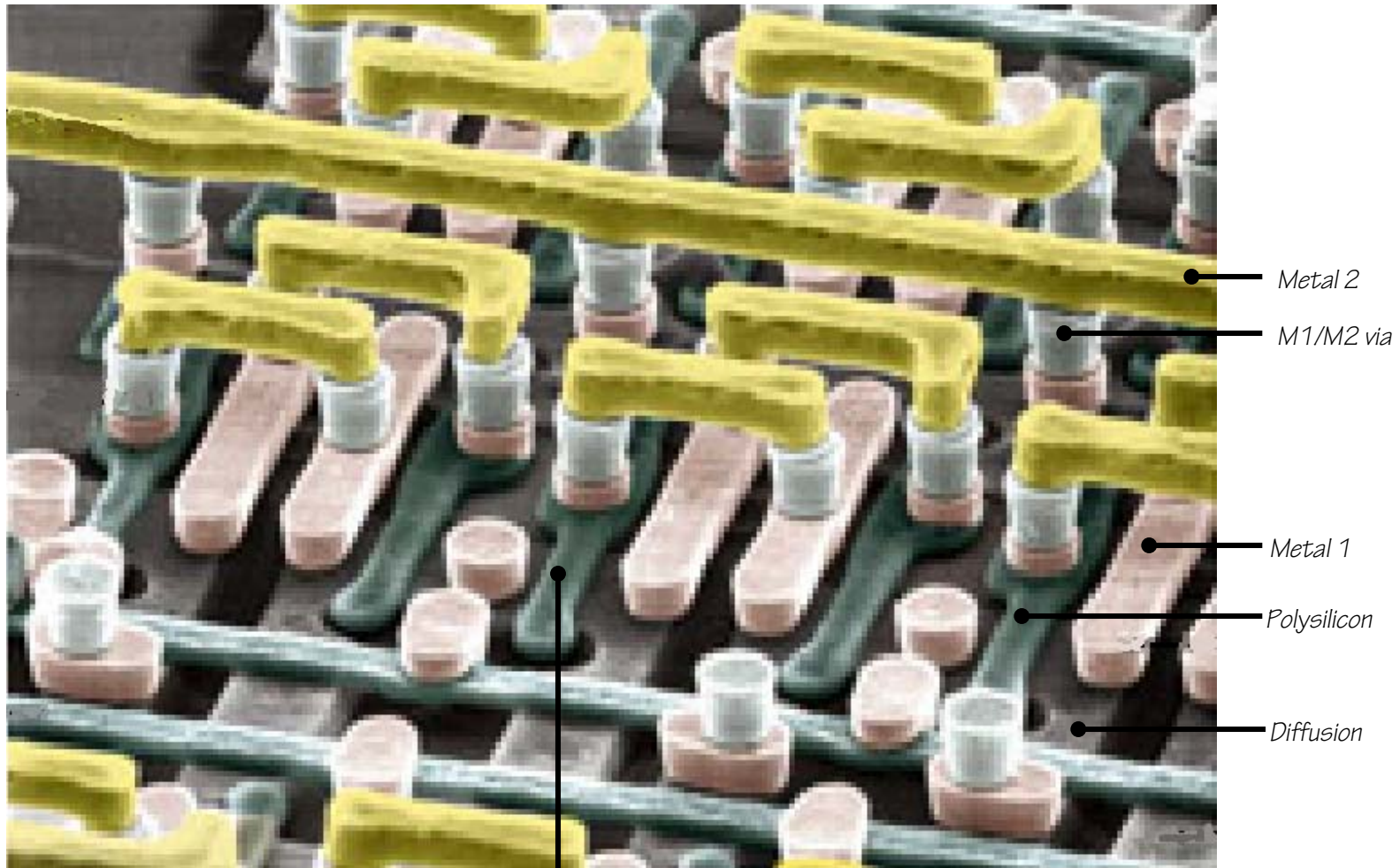
When both fets are saturated, small changes in V_{in} produce large changes in V_{out}

CMOS Signaling

- **Typical CMOS signaling specifications:**
 - $V_{OL} \approx 0, V_{OH} \approx V_{DD}$ (V_{DD} is the power supply voltage)
 - $V_{IL} \approx \text{just under } V_{DD}/2, V_{IH} \approx \text{just over } V_{DD}/2$
 - **Great noise margins! $\sim V_{DD}/2$**
- **Inputs electrically isolated from outputs:**
 - An output can drive many, many inputs without violating signaling spec (but transitions will get slower)
- **In the steady state, signals are either "0" or "1"**
 - When $V_{OUT} = 0V$, $I_{PD} = 0$ (and $I_{PU} = 0$ since pullup is off)
 - When $V_{OUT} = V_{DD}$, $I_{PU} = 0$ (and $I_{PD} = 0$ since pulldown is off)
 - **No power dissipated in steady state!**
 - **Power dissipated only when signals change (ie, power proportional to operating frequency).**

Multiple interconnect layers

IBM photomicrograph (SiO_2 has been removed!)



Metal 2

M1/M2 via

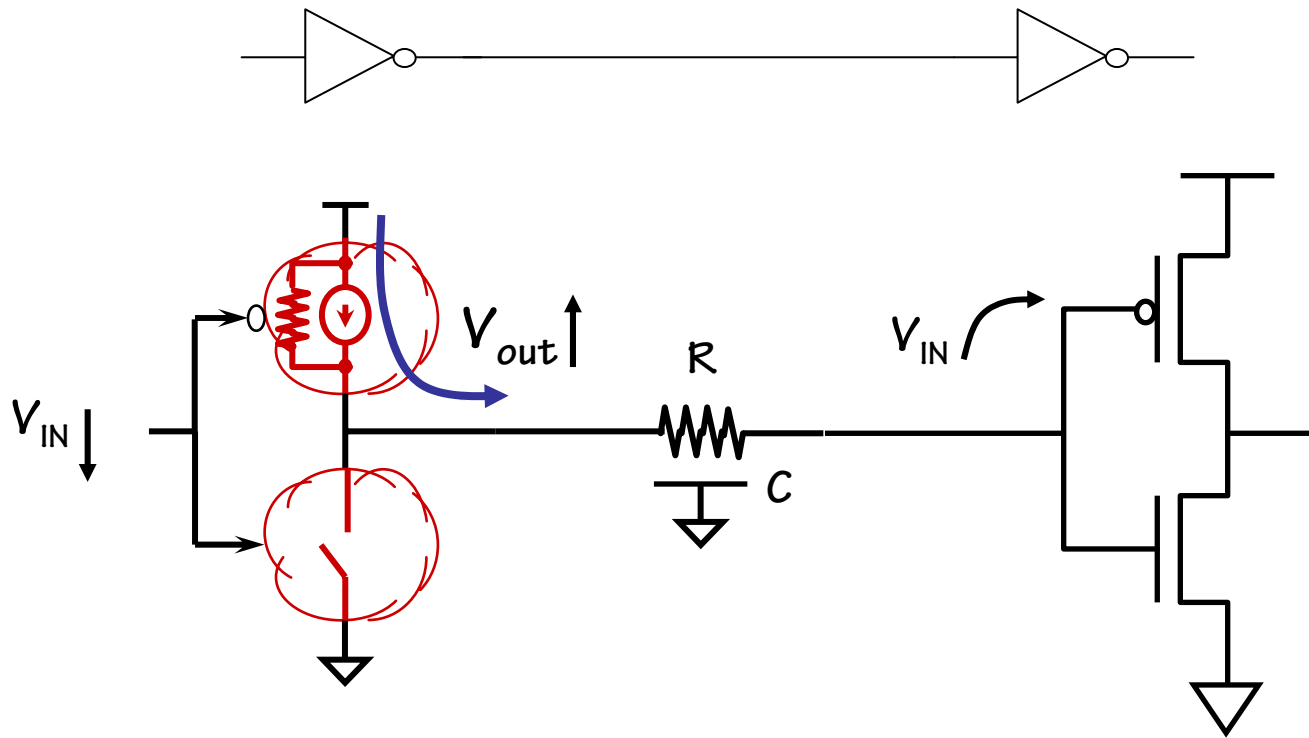
Metal 1

Polysilicon

Diffusion

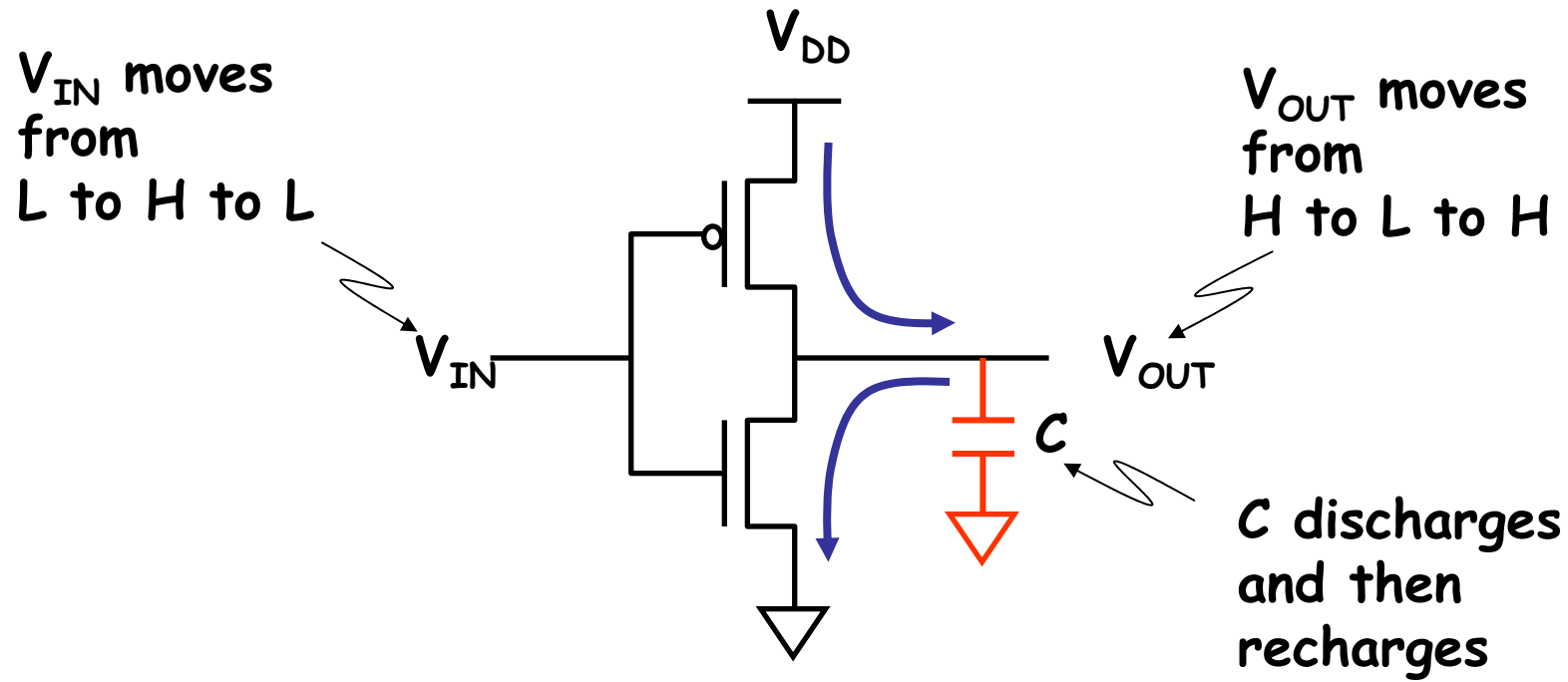
Mosfet (under polysilicon gate)

Big Issue 1: Wires



- **Today (i.e., 100nm):**
 $\tau_{RC} \approx 50\text{ps/mm}$
Implies $> 1\text{ ns}$ to traverse a $20\text{mm} \times 20\text{mm}$ chip
This is a long time in a 2GHz processor

Big Issue 2: Power



- Energy dissipated = $C V_{DD}^2$ per gate
Power consumed = $f n C V_{DD}^2$ per chip

where f = frequency of charge/discharge
 n = number of gates /chip

Unfortunately...



32 Amps (@220v)

- Modern chips (UltraSparc III, Power4, Itanium 2) dissipate from 80W to 150W with a $V_{dd} \approx 1.2V$ (Power supply current is ≈ 100 Amps)
- Cooling challenge is like making the filament of a 100W incandescent lamp cool to the touch!

•Worse yet...

- Little room left to reduce V_{dd}
- nC and f continue to grow

**MIT Computation Center
and Pizzeria**

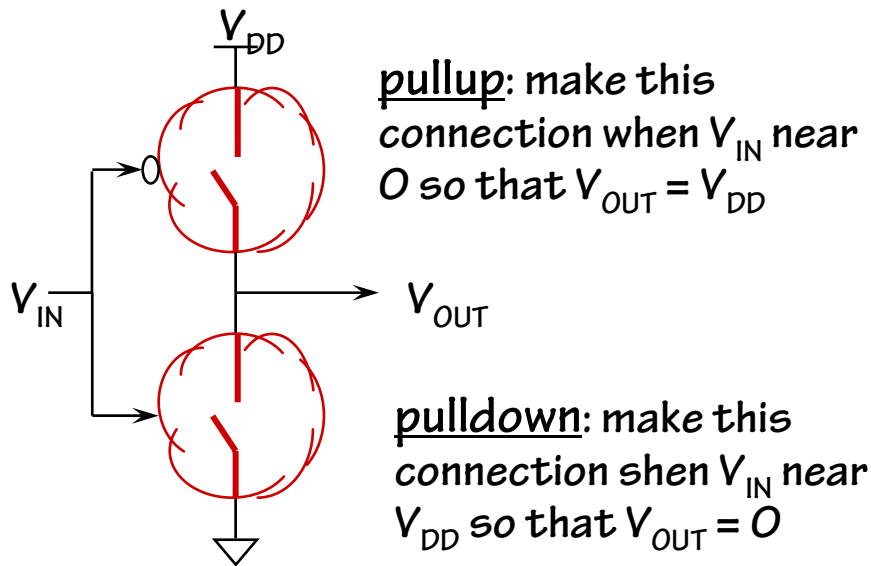
I've got the
solution!



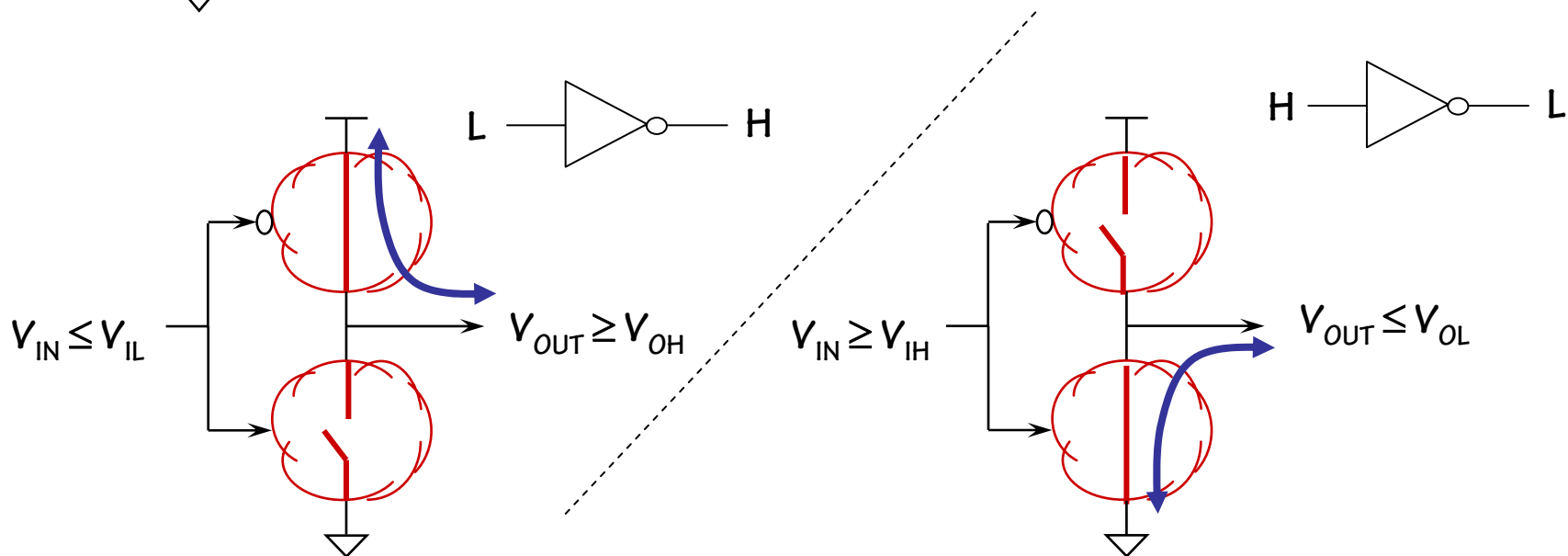
Hey: could we
somehow recycle
the charge?



CMOS Gate Recipe: Think Switches



One power supply \rightarrow
 Two voltages (V_{DD} , GND) \rightarrow
 Binary signaling



Beyond Inverters: Complementary pullups and pulldowns

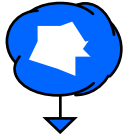
Now you know what the "C"
in CMOS stands for!

We want **complementary** pullup and pulldown logic, i.e., the pulldown should be "on" when the pullup is "off" and vice versa.

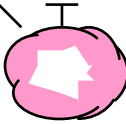
pullup	pulldown	$F(A_1, \dots, A_n)$
on	off	driven "1"
off	on	driven "0"
on	on	driven "X"
off	off	no connection

Since there's plenty of capacitance on the output node, when the output becomes disconnected it "remembers" its previous voltage - at least for a while. The "memory" is the load capacitor's charge. Leakage currents will cause eventual decay of the charge (that's why DRAMs need to be refreshed!).

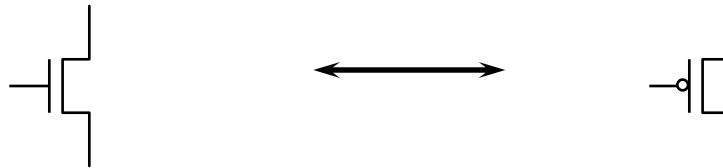
What a nice V_{OH} you have...



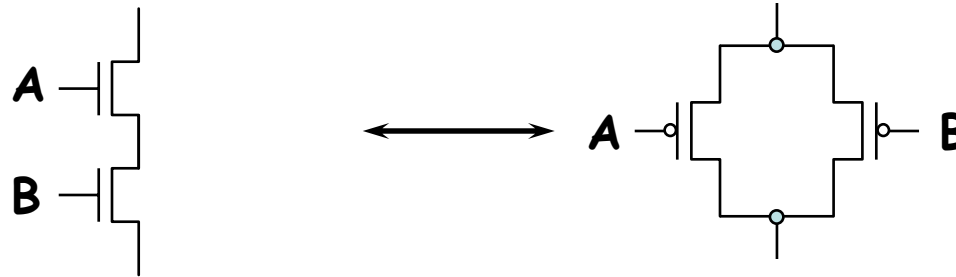
Thanks. It runs in the family...



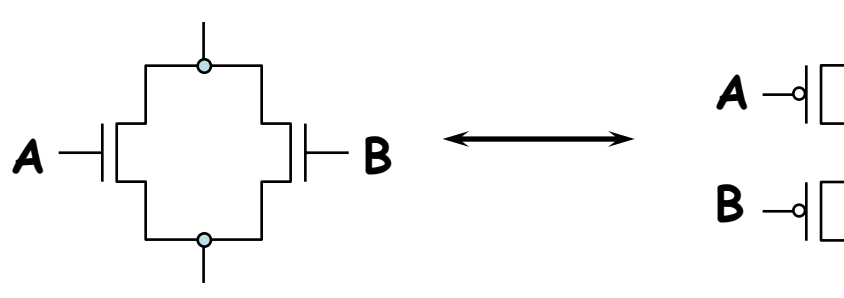
CMOS complements



conducts when V_{GS} is high conducts when V_{GS} is low

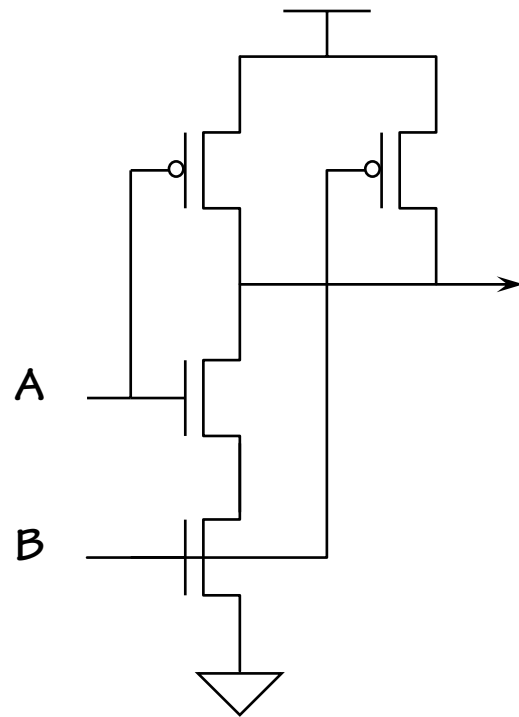
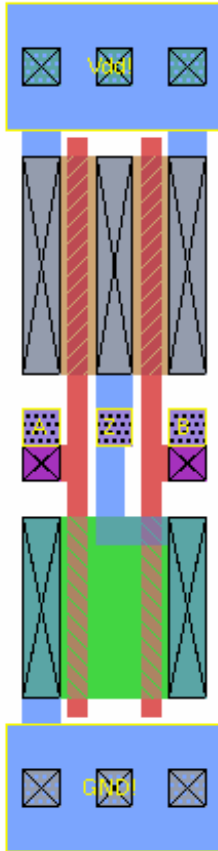


conducts when A is high and B is high: $A \cdot B$ conducts when \overline{A} is low or \overline{B} is low: $\overline{A+B} = \overline{A \cdot B}$



conducts when A is high or B is high: $A+B$ conducts when \overline{A} is low and \overline{B} is low: $\overline{A \cdot B} = \overline{A+B}$

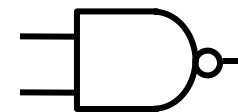
A pop quiz!



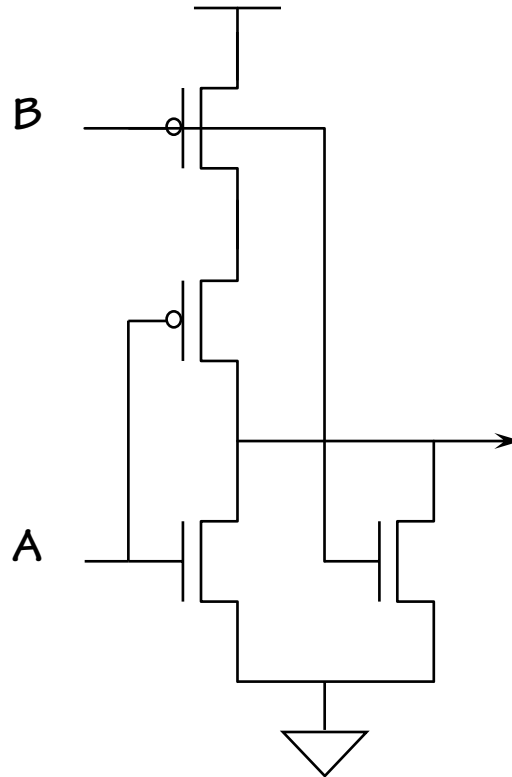
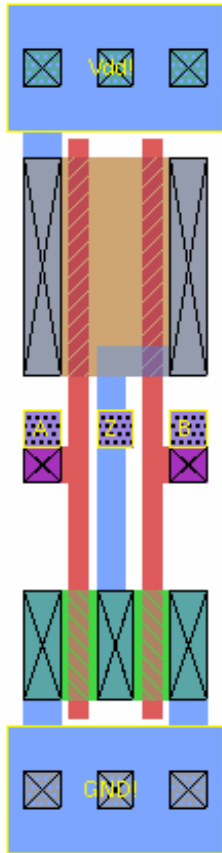
What function does this gate compute?

A	B	C
0	0	1
0	1	1
1	0	1
1	1	0

NAND



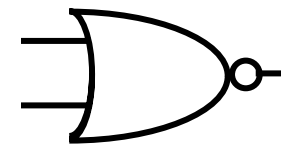
Here's another...



What function does this gate compute?

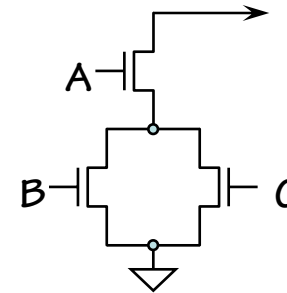
A	B	C
0	0	1
0	1	0
1	0	0
1	1	0

NOR

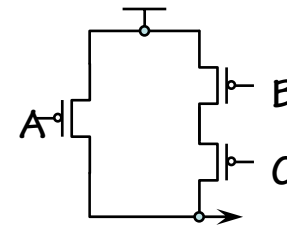


General CMOS gate recipe

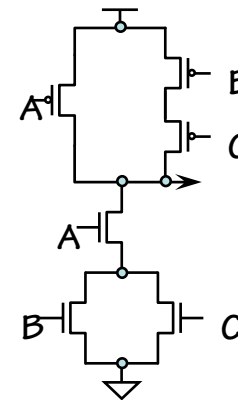
Step 1. Figure out pulldown network that does what you want, *e.g.*, $F = A*(B+C)$
(What combination of inputs generates a low output)



Step 2. Walk the hierarchy replacing nfets with pfets, series subnets with parallel subnets, and parallel subnets with series subnets



Step 3. Combine pMOS pullup network from Step 2 with nMOS pulldown network from Step 1 to form fully-complementary CMOS gate.



So, whats the big deal?



Basic Gate Repertoire

Are we sure we have all the gates we need?
Just how many two-input gates are there?

AND		OR		NAND		NOR	
AB	Y	AB	Y	AB	Y	AB	Y
00	0	00	0	00	1	00	1
01	0	01	1	01	1	01	0
10	0	10	1	10	1	10	0
11	1	11	1	11	0	11	0



Hmmmm... all of these have 2-inputs (no surprise)
... each with 4 combinations, giving 2^2 output cases

How many ways are there of assigning 4 outputs? $2^{2^2} = 2^4 = 16$

There are only so many gates

There are only 16 possible 2-input gates

... some we know already, others are just silly

I N P U T	Z	A	A	B	X	N	X	N	A	N	B	N	O	O	
AB	O	D	B	A	A	B	R	R	R	'B'	B	'A'	A	D	E
00	0	0	0	0	0	0	0	0	1	1	1	1	1	1	1
01	0	0	0	0	1	1	1	1	0	0	0	0	1	1	1
10	0	0	1	1	0	0	1	1	0	0	1	1	0	0	1
11	0	1	0	1	0	1	0	1	0	1	0	1	0	1	1

How many of these gates can be implemented using a single CMOS gate?



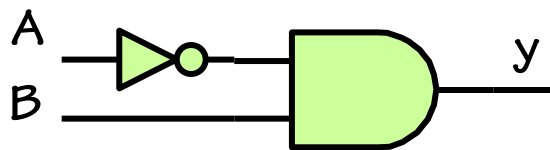
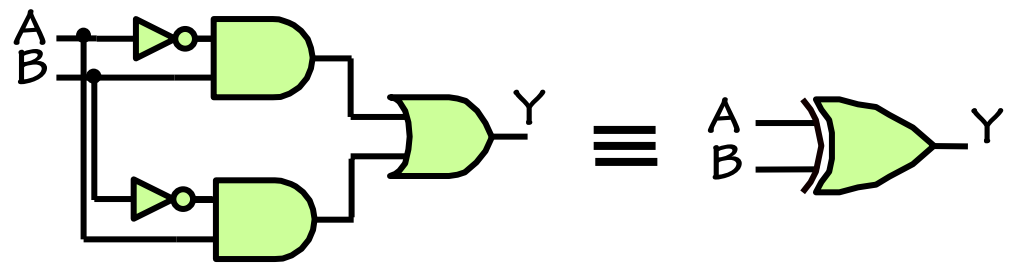
CMOS gates are inverting; we can always respond positively to positive transitions by cascaded gates. But suppose our logic yielded cheap *positive* functions, while inverters were expensive...

Fortunately, we can get by with a few basic gates...

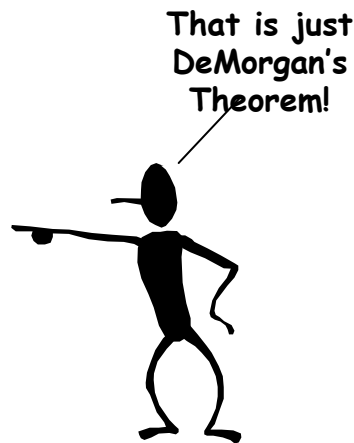
AND, OR, and NOT are sufficient... (cf Boolean Expressions):

B > A		Y
AB		
00		0
01		1
10		0
11		0

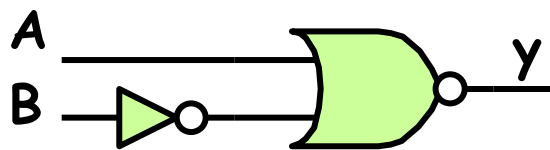
XOR		Y
AB		
00		0
01		1
10		1
11		0



$$\overline{AB} = \overline{A+B}$$



$$\overline{\overline{A}\overline{B}} = \overline{\overline{A+B}}$$



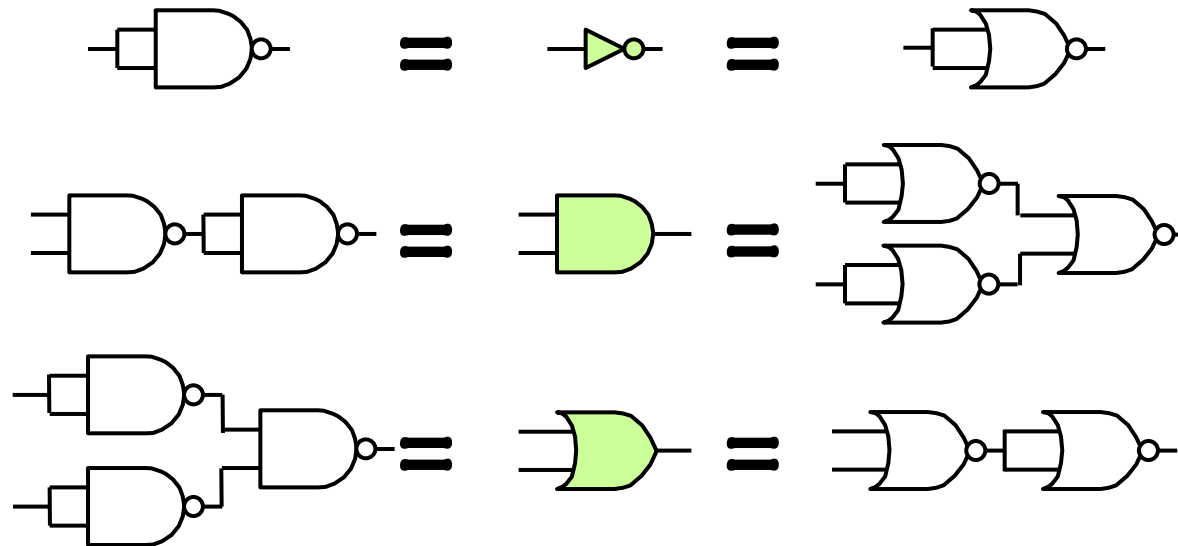
$$\overline{A+B} = \overline{AB}$$



How many different gates do we *really* need?

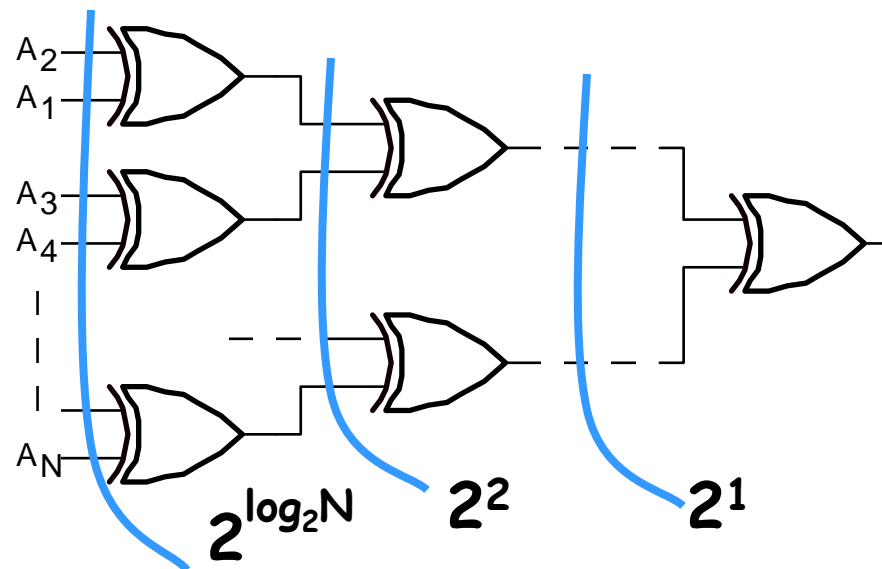
One will do!

NANDs and NORs are universal:



Ah!, but what if we want more than 2 inputs?

**I think that I shall never see
a circuit lovely as...**



N-input TREE has $O(\underline{\log N})$ levels...

Signal propagation takes $O(\underline{\log N})$ gate delays.

Question: Can EVERY N-Input Boolean function be implemented as a tree of 2-input gates?

Here's a Design Approach

Truth Table

C	B	A	Y
0	0	0	0
0	0	1	1
0	1	0	0
0	1	1	1
1	0	0	0
1	0	1	0
1	1	0	1
1	1	1	1

- 1) Write out our functional spec as a truth table
- 2) Write down a Boolean expression for every '1' in the output

$$Y = \overline{C}BA + \overline{C}B\overline{A} + C\overline{B}\overline{A} + CBA$$

- 3) Wire up the gates, call it a day, and declare success!

This approach will always give us Boolean expressions in a particular form:

SUM-OF-PRODUCTS

- it's systematic!
- it works!
- it's easy!
- are we done yet???



Straightforward Synthesis

We can implement
SUM-OF-PRODUCTS
with just three levels of
logic.

INVERTERS/AND/OR

Propagation delay --

No more than "3" gate delays
(well, it's actually $O(\log N)$ gate delays)

