Indicate which sections of the final you will be taking. We will grade only those sections.

<table>
<thead>
<tr>
<th>Quiz 1</th>
<th>Quiz 2</th>
<th>Quiz 3</th>
<th>Quiz 4</th>
</tr>
</thead>
<tbody>
<tr>
<td>Problem 1</td>
<td>Problem 2</td>
<td>Problem 1</td>
<td>Problem 2</td>
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<tr>
<td>Problem 1</td>
<td>Problem 2</td>
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<td>Problem 2</td>
</tr>
<tr>
<td>Problem 1</td>
<td>Problem 2</td>
<td>Problem 1</td>
<td>Problem 2</td>
</tr>
</tbody>
</table>

Quiz 1 Total  
Quiz 2 Total  
Quiz 3 Total  
Quiz 4 Total  

Bonuses:

□ Bonus SRN  
□ SRN 2  
□ SRN 3  
□ SRN 4

Survey

We want to know if our front-loading policy in 6.034 makes sense. So please indicate:

Number of subjects you are taking with a final, not including 6.034

Number of subjects you are taking with a term project or paper that requires substantial effort at or near the end of the semester

There are 38 pages on this exam, not including blank pages and tear-off sheets. As always, this exam is open book, open notes, open almost everything—including a calculator—but no computers.
Quiz 1, Problem 1: Rule-based systems (50 points)

Part A: General questions (19 points)

A1 (15 points) For each of the following statements, circle the single best answer.

1. True / False: During backward chaining, at most one rule can match the current hypothesis.

2. True / False: During forward chaining, at most one rule can match per round.

3. True / False: During forward chaining, a rule may match in multiple rounds, but each rule can fire at most once.

4. True / False: In each round of forward chaining, the first rule that matches will fire.

5. True / False: In each round of forward chaining, at most one new assertion can be added to the list of assertions.

A2 (4 points) In general, which of the following conditions can cause backward chaining to short circuit? That is, which of these will cause the evaluation of subtrees to stop? (Circle ALL answers that apply)

A) A child of an AND subtree returns true.
B) A child of an AND subtree returns false.
C) A child of an OR subtree returns true.
D) A child of an OR subtree returns false.
E) The backward chainer cannot find a match for the hypothesis in the list of assertions.
F) The backward chainer cannot find a match for the hypothesis in the antecedent of any rule.
Part B: Backward chaining (8 points)

Rules:
R0  IF (OR ‘(?x) follows Rick’,
       ‘(?x) listens to Rick’),
    THEN ‘(?x) is a Morty’

R1  IF (AND ‘(?y) acts as a human shield’,
       ‘(?y) is a Morty’,
       ‘(?y) doesn't know this is true’),
    THEN ‘(?y) is the Mortiest Morty’

Assertions:
A0: Morty follows Rick
A1: Morty listens to Rick
A2: Morty acts as a human shield
A3: Morty doesn't know this is true

B1 (7 points) Suppose you are performing backward chaining with this set of rules and assertions, starting from the hypothesis “Morty is the Mortiest Morty”. Numbers indicate the order in which hypotheses are checked. Unnumbered nodes have not been explored. Which of the following trees would result at the end of backward chaining? (Circle the single best answer.)
B2 (1 point) Based on the results of backward chaining, is the hypothesis “Morty is the Mortiest Morty” true? (Circle one)

YES  NO  CAN'T TELL

Part C: Forward chaining (12 points)

Consider the following rule-based system:

Rules:
R0  IF (OR ‘(?x) follows Rick’, ‘(?x) listens to Rick’),
     THEN ‘(?x) is a Morty’
R1  IF (AND ‘(?y) acts as a human shield’, ‘(?y) is a Morty’, ‘(?y) doesn't know this is true’),
     THEN ‘(?y) is the Mortiest Morty’

Assertions:
A0: Morty follows Rick
A1: Morty listens to Rick
A2: Morty acts as a human shield
A3: Morty doesn't know this is true

Suppose you are going to perform three rounds of forward chaining using these rules and assertions. (Hint: It may help to actually perform the forward chaining.)

C1 (3 points) In the first round, which rule(s) will match? (Circle one)

Only R0  Only R1  Both R0 and R1  Neither R0 nor R1

C2 (9 points) Which rule will fire in each round? Circle the single best answer in each case.

<table>
<thead>
<tr>
<th>Round 1</th>
<th>Only R0</th>
<th>Only R1</th>
<th>Both R0 and R1</th>
<th>Neither R0 nor R1</th>
</tr>
</thead>
<tbody>
<tr>
<td>Round 2</td>
<td>Only R0</td>
<td>Only R1</td>
<td>Both R0 and R1</td>
<td>Neither R0 nor R1</td>
</tr>
<tr>
<td>Round 3</td>
<td>Only R0</td>
<td>Only R1</td>
<td>Both R0 and R1</td>
<td>Neither R0 nor R1</td>
</tr>
</tbody>
</table>
Part D: More Forward Chaining (11 points)
These are independent questions about unrelated rule-based systems. Assume there are no DELETE statements in any system.

D1 (3 points) Suppose a rule matches in the first round of forward chaining and does not contain any “NOT”s in its antecedent. Is this rule guaranteed to match in every subsequent round? (Circle one)

YES \hspace{1cm} NO

D2 (3 points) Suppose a rule matches in the first round of forward chaining and contains a “NOT” in its antecedent. Is this rule guaranteed to match in every subsequent round? (Circle one)

YES \hspace{1cm} NO

D3 (5 points) Consider the following rule and possible sets of assertions. If you were to perform forward chaining, which of the sets would cause the statement ‘Rick says “This is Rickdiculous!”’ to be added to the list of assertions? Circle all that apply.

R0 \hspace{1cm} IF \hspace{1cm} AND(‘(?x) is lost’,
\hspace{1cm} NOT ‘(?x) is going to find Morty’)
\hspace{1cm} THEN ‘(?x) says “This is Rickdiculous!”’

Set 1: \hspace{1cm} A0: Rick is lost

Set 2: \hspace{1cm} A0: Rick is lost
\hspace{1cm} A1: Rick is not going to find Morty

Set 3: \hspace{1cm} A0: Rick is going to find Morty
\hspace{1cm} A1: Rick is lost

Set 4: \hspace{1cm} A0: Rick is lost
\hspace{1cm} A1: Rick says “This is Rickdiculous!”

Set 5: \hspace{1cm} A0: Rick says “This is Rickdiculous!”
Quiz 1, Problem 2: Search and Games (50 points)
Part A: Search Questions (27 points)

Here's a list of search algorithms and questions. Each question is worth 3 points. For each question, list ALL of the search algorithms (A,B,C,D,E,F,G,H) that apply. If none of the search algorithms apply, write NONE instead. Some algorithms may be used more than once, and some may not be used at all.

<p>| | | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>A* search</td>
<td></td>
</tr>
<tr>
<td>B</td>
<td>Branch and bound (no heuristic, no extended set)</td>
<td></td>
</tr>
<tr>
<td>C</td>
<td>Depth-first search (with backtracking)</td>
<td></td>
</tr>
<tr>
<td>D</td>
<td>Branch and bound with a heuristic (no extended set)</td>
<td></td>
</tr>
<tr>
<td>E</td>
<td>Branch and bound with an extended set (no heuristic)</td>
<td></td>
</tr>
<tr>
<td>F</td>
<td>Breadth-first search</td>
<td></td>
</tr>
<tr>
<td>G</td>
<td>Best-first search</td>
<td></td>
</tr>
<tr>
<td>H</td>
<td>Hill-climbing (with backtracking)</td>
<td></td>
</tr>
</tbody>
</table>

① Which of these algorithms add children to the front of the agenda like a stack (without sorting the agenda)?

② Which of these algorithms add children to the back of the agenda like a queue (without sorting the agenda)?

③ Which of these algorithms will need to know the weights of the edges in the graph?
④ Which of these algorithms will need a heuristic estimate of remaining distance to the goal?

⑤ Which of these algorithms will always find the shortest path to the goal? (If an algorithm uses a heuristic, do not assume that the heuristic is admissible or consistent.)

⑥ Which of these algorithms can use a consistent heuristic to always find the shortest path to the goal (if one exists)? Think carefully.

⑦ Which of these algorithms have a built-in limit on the size of the agenda?

⑧ Which of these algorithms use some kind of cost function to determine which path to extend next?

⑨ Which of these algorithms may continue searching even after finding a path to the goal?
Part B (14 points)
In this problem, you will evaluate how alpha-beta pruning performs in the best case and in the worst case.

B1 (7 points) Suppose you perform alpha-beta pruning on the above game tree. List all of the leaf nodes you would have to statically evaluate in the best case, i.e. if the static values in the tree cause alpha-beta to prune the greatest possible number of nodes.

B2 (7 points) Suppose you perform alpha-beta pruning on the above game tree. List all of the leaf nodes you would have to statically evaluate in the worst case, i.e. if the static values in the tree cause alpha-beta to prune the least possible number of nodes.
Part C (9 points)
While performing alpha-beta pruning with progressive deepening, you generate this game tree that looks two moves ahead.

In the next round of progressive deepening, you will look three moves ahead.

C1 (5 points) How should you reorder this tree to maximize the possibility of pruning in the next round if MAX will make the first move?

List the leaf nodes (A, B, C, D) in left-to-right order as they appear in the rearranged tree.

C2 (4 points) How should you reorder this tree to maximize the possibility of pruning in the next round if MIN will make the first move?

List the leaf nodes (A, B, C, D) in left-to-right order as they appear in the rearranged tree.

\[ \text{MAX} \]
\[ \text{MIN} \]
\[ A \quad 2 \]
\[ B \quad 0 \]
\[ C \quad 1 \]
\[ D \quad 4 \]
Quiz 2, Problem 1: Constraint satisfaction problems (50 points)

Here is a constraint satisfaction problem with three variables $A$, $B$, $C$. Their initial domains are shown here:

<table>
<thead>
<tr>
<th>Variable</th>
<th>Domain</th>
</tr>
</thead>
<tbody>
<tr>
<td>$A$</td>
<td>0, 1</td>
</tr>
<tr>
<td>$B$</td>
<td>0, 1</td>
</tr>
<tr>
<td>$C$</td>
<td>0, 1, 2</td>
</tr>
</tbody>
</table>

The variables have the following constraints:

1. $A$ and $C$ must be equal.
2. $B$ and $C$ must be equal.
3. Either $A$ must be 1, or $B$ must be 1, or both. They can't both be zero.

To help you visualize these constraints, we have depicted them in the constraint graph here.

**Note:** For your convenience, a copy of this constraint graph is provided on a tear-off sheet after the last page of the final.

Part A: Value Assignments (5 points)

Part A1. How many possible assignments of values to variables are there?

YOUR ANSWER: 

Part A2. How many of those possible assignments satisfy all the constraints – that is, how many different solutions does this problem have? (You may use your intuition, or figure the answer out using the later parts of the problem.)

YOUR ANSWER: 

Part B: First attempt—depth-first search + forward checking (20 points)

**IMPORTANT:** Don’t reduce domains in advance.

Use depth-first search with forward checking (no propagation) to find a consistent assignment of values to variables. Assign variables in the order A, B, C. Break ties by assigning lower values first.

The search tree has been drawn for you, so all you need to do is fill out the worksheet below.

Fill out this worksheet. There may be more rows than you need.

1. Every time you assign a variable or remove a variable from the propagation queue, fill out a new row in the table. (The same variable might appear in more than one row, especially if you have to backtrack.)

2. In that row, indicate which variable you assigned or de-queued; write its assigned value if it has one (e.g. X=x), otherwise just write its name (X). In the second column, list the values that were just eliminated from neighboring variables as a result. If no values were just eliminated, write NONE instead.

3. If your search has to backtrack after assigning or de-queuing a variable: first, finish listing all values eliminated from neighboring variables in the current row. Next, check the “backtrack” box in that row. Then, continue with the next assignment in the following row as usual.

If you add several variables to your propagation queue at once, break ties by adding variables to your propagation queue in alphabetical order.

---

**Example row showing an assigned variable**

<table>
<thead>
<tr>
<th>Var assigned or de-queued</th>
<th>List all values just ELIMINATED from neighboring variables</th>
<th>Back track</th>
</tr>
</thead>
<tbody>
<tr>
<td>X = 3</td>
<td>Y ≠ 3, 4, Z ≠ 3</td>
<td>☐</td>
</tr>
</tbody>
</table>

**Example row showing a de-queued (propagated) variable**

<table>
<thead>
<tr>
<th>Var assigned or de-queued</th>
<th>List all values just ELIMINATED from neighboring variables</th>
<th>Back track</th>
</tr>
</thead>
<tbody>
<tr>
<td>X</td>
<td>W ≠ 1, 4</td>
<td>☐</td>
</tr>
</tbody>
</table>

---

Part C: Second attempt—propagation through singletons (20 points)
IMPORTANT: Don't reduce domains in advance.

Now repeat the process, except this time use depth first search with forward checking and propagation through domains reduced to size 1 to find a consistent assignment of values to variables. Assign variables in the order A, B, C. Break ties by assigning lower values first. The search tree has been drawn for you, so all you need to do is fill out the worksheet below. (There may be more rows than you need.)

★ ★ ★ Note: If you would add more than one variable to the propagation queue at the same time, add them to the queue in alphabetical order. ★ ★ ★
Part D: Domain Reduction (5 points)

Part D1. Suppose you reduce the domains of the variables before starting search. What would the resulting domains of the variables be? (For each variable, circle all values that would still be in the variable's domain. If the domain would be empty after domain reduction, circle EMPTY instead.)

A's domain: 0 1 EMPTY
B's domain: 0 1 EMPTY
C's domain: 0 1 2 EMPTY

Part D2. Is the following statement true or false?

Domain reduction guarantees that you won't have to do any backtracking during search, at the cost of performing more computation before search.

Circle your answer:

True False

(Hint: You may consider this problem, for example.)
Quiz 2, Problem 2: Nearest neighbors & Identification trees (50 points)

Part A: Comparing Apples to Oranges (16 points)
The 6.034 TAs have discovered a mysterious yellowish fruit on the table outside Prof. Winston's office. Before offering the fruit to Prof. Winston as a gift, Elisa points out that they should identify it using k-nearest neighbors. Dylan first makes a graph of known fruits, using each fruit's color and diameter. The resulting training data is as follows:

![Graph of known fruits](image)

Key:
A = Apple  
B = Banana  
O = Orange

A1 (8 points) Malcom wants to use cross-validation to find the best value of k for k-nearest neighbors classification. For each circled point, classify that point as if it were not part of the training data. In the table below, fill in the classification (A, B, O, or CAN'T TELL) of each circled training point for k = 1, 3, and 5. The first row has been filled in for you.

<table>
<thead>
<tr>
<th></th>
<th>(550nm, 25cm)</th>
<th>(575nm, 15cm)</th>
<th>(650nm, 20cm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>k=1</td>
<td>A</td>
<td>B</td>
<td>A</td>
</tr>
<tr>
<td>k=3</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>k=5</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

A2 (2 points) Based on your cross-validation in part A1, which is the best value of k?

k = 1  
k = 3  
k = 5
A3 (6 points) Regardless of the results of Malcom’s cross-validation, Jessica decides to use k=1 so she can draw decision boundaries. On the zoomed-in section of the graph below, draw the decision boundaries found by 1-nearest neighbors. Consider only the three training points pictured. The exact location of each point is where gridlines intersect.

Part B: No More Fruit (16 points)
The other TAs are tired of classifying fruits, so they've moved on to classifying other things. This part consists of a series of independent problems.

B1 (2 points) Pedro has some training data, which he classifies using both k-nearest neighbors and identification trees. He then realizes that some of the features don't contain useful information. Which performed better in terms of ignoring the useless tests? (Circle one)

Identification Trees  
k-Nearest Neighbors

B2 (4 points) Siyao is gathering data about ice cream. Calculate the disorder of the feature test “Flavor” in the data below. Your answer may contain logarithms. Show your work for partial credit.

<table>
<thead>
<tr>
<th>Classification</th>
<th>Flavor</th>
</tr>
</thead>
<tbody>
<tr>
<td>Good</td>
<td>Chocolate</td>
</tr>
<tr>
<td>Good</td>
<td>Chocolate</td>
</tr>
<tr>
<td>Good</td>
<td>Vanilla</td>
</tr>
<tr>
<td>Good</td>
<td>Strawberry</td>
</tr>
<tr>
<td>Bad</td>
<td>Strawberry</td>
</tr>
</tbody>
</table>

Disorder (Flavor) =
**B3 (4 points)** Duncan is classifying locations as Safe or Dangerous. One feature he considers is “Has Railing.” Duncan has forgotten the classification of one of his training points, Location #3. Given that “Has Railing” has a disorder of 0.5, what must have been the classification of Location #3? (Circle one)

*Hint 1: It may be helpful to draw the decision stump for the “Has Railing” feature.*

*Hint 2: Or it may be helpful to calculate what the disorder of the feature test “Has Railing” would be for each classification (Safe or Dangerous) of Location #3.*

<table>
<thead>
<tr>
<th>Location #</th>
<th>Classification</th>
<th>Has Railing</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Safe</td>
<td>Yes</td>
</tr>
<tr>
<td>2</td>
<td>Safe</td>
<td>Yes</td>
</tr>
<tr>
<td>3</td>
<td>??</td>
<td>No</td>
</tr>
<tr>
<td>4</td>
<td>Dangerous</td>
<td>No</td>
</tr>
</tbody>
</table>

**SAFE**

**DANGEROUS**

**CAN’T TELL**

**B4 (6 points)** Josh is investigating some claims about identification trees and k-nearest neighbors. Circle the one best answer (True or False) for each claim.

1. After a feature test is used in an identification tree, it will always have a disorder of 0. **TRUE** **FALSE**

2. When it is impossible to perfectly classify the training data using identification trees, you can asymptotically improve the error rate by repeatedly testing whether a point has a particular feature. **TRUE** **FALSE**

3. Given the following four training points in two classifications (+ and -), identification trees and 1-nearest neighbors would both draw these boundaries: **TRUE** **FALSE**
Part C: Unshredding (18 points)
Your friend Jack, whose thesis project involves reconstructing shredded documents, has the found the pieces of what appears to be a 6.034 quiz solution! However, there are multiple ways that the pieces fit together, and Jack doesn't know which possible solutions are correct.

The original problem was to draw decision boundaries on the graph at right that perfectly classify the training data into two classifications (Q and T) using a greedy disorder-minimizing identification tree.

Jack has pieced together the following possible solutions. For each one, circle YES or NO to answer the question “Does this graph depict disorder-minimizing identification tree boundaries?”
Quiz 3, Problem 1: Neural networks (40 points)

Part A: Cutting the Plane (20 points)

Neural nets with different structures are capable of recognizing different output patterns. Consider the different ways of cutting the plane into four sections using two intersecting diagonal lines. A shaded section indicates that all the points in that area are classified as 1, while an unshaded section indicates that all the points in that area are classified as 0. Ignoring rotations, there are six shading possibilities, as shown here.

A nothing shaded  
B one shaded region  
C two shaded neighboring regions  
D two shaded opposite regions  
E three shaded regions  
F everything shaded

For each of the following neural nets, list all of the above shadings (A, B, C, D, E, F) that the neural net can produce. If a neural net can produce none of these shadings, write NONE instead. Be careful, in particular for answer choice A. Note that we are asking only if the shadings that can be produced, not the lines, because it might be possible to produce the shading but not the lines.

<table>
<thead>
<tr>
<th>Neural net</th>
<th>List ALL shadings (A, B, C, D, E, F) the neural net can produce; if none, write NONE instead.</th>
</tr>
</thead>
</table>
| X  
| Y  
| out |
| X  
| Y  
| out |
| X  
| Y  
| out |
| X  
| Y  
| out |
| X  
| Y  
| out |
Part B: Logic (20 points)

In this problem, you are trying to build neural nets that can implement certain logic functions. For each logic function, your neural net must be a single neuron with two inputs. That is, the output of the net must be:

\[
out = \begin{cases} 
1, & \text{if } w_x \cdot x + w_y \cdot y \geq T \\
0, & \text{otherwise}
\end{cases}
\]

For each row in the table, circle values for \(w_x\), \(w_y\), and \(T\) that implement the desired behavior.

<table>
<thead>
<tr>
<th>Logic Function</th>
<th>Graph of behavior (shaded = output of 1, unshaded = output of 0)</th>
<th>Weights and threshold</th>
</tr>
</thead>
<tbody>
<tr>
<td>AND(X, Y)</td>
<td><img src="image" alt="AND Graph" /></td>
<td>(w_x: -2\ 0\ 2)</td>
</tr>
<tr>
<td></td>
<td><img src="image" alt="Graph" /></td>
<td>(w_y: -2\ 0\ 2)</td>
</tr>
<tr>
<td></td>
<td><img src="image" alt="Graph" /></td>
<td>(T: -3\ -1\ 1\ 3)</td>
</tr>
<tr>
<td>OR(X, Y)</td>
<td><img src="image" alt="OR Graph" /></td>
<td>(w_x: -2\ 0\ 2)</td>
</tr>
<tr>
<td></td>
<td><img src="image" alt="Graph" /></td>
<td>(w_y: -2\ 0\ 2)</td>
</tr>
<tr>
<td></td>
<td><img src="image" alt="Graph" /></td>
<td>(T: -3\ -1\ 1\ 3)</td>
</tr>
<tr>
<td>NOT(X)</td>
<td><img src="image" alt="NOT Graph" /></td>
<td>(w_x: -2\ 0\ 2)</td>
</tr>
<tr>
<td></td>
<td><img src="image" alt="Graph" /></td>
<td>(w_y: -2\ 0\ 2)</td>
</tr>
<tr>
<td></td>
<td><img src="image" alt="Graph" /></td>
<td>(T: -3\ -1\ 1\ 3)</td>
</tr>
<tr>
<td>NAND(X, Y)</td>
<td><img src="image" alt="NAND Graph" /></td>
<td>(w_x: -2\ 0\ 2)</td>
</tr>
<tr>
<td></td>
<td><img src="image" alt="Graph" /></td>
<td>(w_y: -2\ 0\ 2)</td>
</tr>
<tr>
<td></td>
<td><img src="image" alt="Graph" /></td>
<td>(T: -3\ -1\ 1\ 3)</td>
</tr>
<tr>
<td>NOR(X, Y)</td>
<td><img src="image" alt="NOR Graph" /></td>
<td>(w_x: -2\ 0\ 2)</td>
</tr>
<tr>
<td></td>
<td><img src="image" alt="Graph" /></td>
<td>(w_y: -2\ 0\ 2)</td>
</tr>
<tr>
<td></td>
<td><img src="image" alt="Graph" /></td>
<td>(T: -3\ -1\ 1\ 3)</td>
</tr>
</tbody>
</table>
**Quiz 3, Problem 2: Support Vector Machines (60 points)**

**Part A: Border beyond the wall (30 points)**

The men of the Night’s Watch are trying to map the regions beyond the Wall and would like to mark the border between White Walker and Free Folk territory. White Walkers (+) and Free Folk (-) are shown on the graph below. John Snow knows nothing, except that he should use an SVM to draw the border as an SVM boundary line.

Part A1 (10 points): On the diagram above,  
- Draw the SVM boundary as a **solid line**  
- Draw the gutters as **dotted lines**  
- **Circle** the support vectors
Part A2 (8 points)

Find the values of \( \vec{w} \) and \( b \) that correspond to the SVM you drew in Part A1.

\[
\vec{w} = \quad b = 
\]

Show your work for partial credit.
Part A3 (6 points)
Circle the classification the SVM would assign to a new point \( \langle x, y \rangle = \langle 4, 4 \rangle \).

<table>
<thead>
<tr>
<th>White Walker (+)</th>
<th>Free Folk (-)</th>
<th>Can't be determined</th>
</tr>
</thead>
</table>

Circle the classification the SVM would assign to a new point \( \langle x, y \rangle \) given: \( \vec{w} \cdot \langle x, y \rangle = 1 \)

<table>
<thead>
<tr>
<th>White Walker (+)</th>
<th>Free Folk (-)</th>
<th>Can't be determined</th>
</tr>
</thead>
</table>

Part A4 (6 points)
For each training point, indicate whether its alpha value is POSITIVE, NEGATIVE, or ZERO. Circle the best answer in each case.

\[
\begin{array}{ccc}
\alpha_A & \text{POSITIVE} & \text{NEGATIVE} & \text{ZERO} \\
\alpha_B & \text{POSITIVE} & \text{NEGATIVE} & \text{ZERO} \\
\alpha_C & \text{POSITIVE} & \text{NEGATIVE} & \text{ZERO} \\
\alpha_D & \text{POSITIVE} & \text{NEGATIVE} & \text{ZERO} \\
\alpha_E & \text{POSITIVE} & \text{NEGATIVE} & \text{ZERO} \\
\alpha_F & \text{POSITIVE} & \text{NEGATIVE} & \text{ZERO} \\
\alpha_G & \text{POSITIVE} & \text{NEGATIVE} & \text{ZERO} \\
\end{array}
\]
Part B: A Lannister always separates their data (30 points)

Tyrion is trying to figure out if the other characters are honest (+) or sneaky (-). He is having trouble because the data he has is not linearly separable. A graph of Tyrion's data is shown below.

Part B1 (5 points)

Consider each of the strategies below. Circle **ALL** of the strategies that will enable Tyrion to perfectly classify this entire training dataset using a support vector machine:

1. Reduce tolerance by minimizing, rather than maximizing, the margin width.
2. Reduce training error by eliminating a redundant feature.
3. Separate the space by introducing a third feature, Z.
4. Separate the space by introducing a nonlinear kernel.
5. Perform cross-validation to identify outliers.
**Part B2 (5 points)** Instead, Tyrion decides to use kernels and transforms to separate his data. Which kernels can perfectly separate Tyrion’s data? (Circle all that apply)

- Linear
- Polynomial (Quadratic)
- Radial Basis

**Part B3 (10 points)** Tyrion considers using the following transform:

\[ \varphi(x, y) = \langle |x - 1|, y \rangle \]

Will this transform make the data linearly separable? (Circle one)

- Yes
- No

*Note: For your convenience, this blank plot is provided to optionally show your work.*
Part B4 (10 points)

In the end, Tyrion decides to use a **polar transform**, \( \varphi(x, y) = (r, \theta) \) resulting in the following transformed space:

On the diagram **above**, **sketch** the SVM boundary as a **solid line**.

**Sketch** the boundary as it would appear on the original, untransformed space on the diagram **below**.
Quiz 4, Problem 1: Adaboost (50 points)

Part A: Venture Capitalism (38 points)
Congratulations—you've just won $10,000 in this month’s lottery! You've heard that investing in startups is a good idea but aren’t sure how to predict which startups will be successful. You decide to use Adaboost to classify upcoming startups as successful or not, so that you can make lots of money and stay on the cutting edge of new technology.

To begin, you look at six recent startups, noting some of their characteristics and whether they've become successful:

<table>
<thead>
<tr>
<th>Startup ID</th>
<th>Name</th>
<th>Successful</th>
<th>Hires Business Majors</th>
<th># of Team Members</th>
<th>Reached Kickstarter Goal</th>
<th>Founder from MIT</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>FaceStalk</td>
<td>Yes</td>
<td>Yes</td>
<td>5</td>
<td>Yes</td>
<td>No</td>
</tr>
<tr>
<td>2</td>
<td>CouchSurfer</td>
<td>Yes</td>
<td>No</td>
<td>6</td>
<td>No</td>
<td>Yes</td>
</tr>
<tr>
<td>3</td>
<td>Freeloader</td>
<td>No</td>
<td>Yes</td>
<td>4</td>
<td>No</td>
<td>Yes</td>
</tr>
<tr>
<td>4</td>
<td>MyFace</td>
<td>No</td>
<td>No</td>
<td>1</td>
<td>No</td>
<td>No</td>
</tr>
<tr>
<td>5</td>
<td>Googoo</td>
<td>Yes</td>
<td>No</td>
<td>3</td>
<td>No</td>
<td>Yes</td>
</tr>
<tr>
<td>6</td>
<td>NapApp</td>
<td>No</td>
<td>Yes</td>
<td>5</td>
<td>No</td>
<td>Yes</td>
</tr>
</tbody>
</table>

A1 (6 points) You've come up with several feature tests to help you predict whether a startup will succeed. For each of the tests in the table below, circle all the training points that the test misclassifies.

<table>
<thead>
<tr>
<th>Test (if True, startup is Successful)</th>
<th>Misclassified Training Points (Circle all that apply)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Hires Business Majors = Yes</td>
<td>1 2 3 4 5 6</td>
</tr>
<tr>
<td># of Team Members &gt; 3.5</td>
<td>1 2 3 4 5 6</td>
</tr>
<tr>
<td># of Team Members &gt; 4.5</td>
<td>1 2 3 4 5 6</td>
</tr>
</tbody>
</table>
A2 (4 points) You've decided to use a different set of feature tests as weak classifiers to perform Adaboost. The classifiers and the errors they make are listed here.

<table>
<thead>
<tr>
<th>Test ID</th>
<th>Test (if True, startup is Successful)</th>
<th>Misclassified Training Points</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>Reached Kickstarter Goal = Yes</td>
<td>2 5</td>
</tr>
<tr>
<td>B</td>
<td># of Team Members &lt; 3.5</td>
<td>4 5</td>
</tr>
<tr>
<td>C</td>
<td>Founder from MIT = Yes</td>
<td>1 3 6</td>
</tr>
<tr>
<td>D</td>
<td>Founder from MIT = No</td>
<td>2 4 5</td>
</tr>
</tbody>
</table>

If you run Adaboost choosing the weak classifier with the lowest error rate in each round and breaking ties randomly, which tests from the table above would you never choose? (Circle all answers that apply)

A       B       C       D

NONE OF THESE

(space to show work for Adaboost, part A3)
**A3 (24 points)** Perform two rounds of boosting using only the four weak classifiers (A, B, C, D) from part A2. In each round, choose the weak classifier with the **lowest error rate**. In case of a tie, choose the weak classifier that comes first **alphabetically**.

<table>
<thead>
<tr>
<th></th>
<th>Round 1</th>
<th>Round 2</th>
</tr>
</thead>
<tbody>
<tr>
<td>weight₁</td>
<td></td>
<td>1/6</td>
</tr>
<tr>
<td>weight₂</td>
<td></td>
<td></td>
</tr>
<tr>
<td>weight₃</td>
<td></td>
<td></td>
</tr>
<tr>
<td>weight₄</td>
<td></td>
<td></td>
</tr>
<tr>
<td>weight₅</td>
<td></td>
<td></td>
</tr>
<tr>
<td>weight₆</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Error rate of A</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Error rate of B</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Error rate of C</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Error rate of D</td>
<td></td>
<td></td>
</tr>
<tr>
<td>weak classifier (h)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>weak classifier error rate (ε)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>voting power (α)</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

**A4 (4 points)** Here are the characteristics of a new startup called Glassr:

<table>
<thead>
<tr>
<th>Name</th>
<th>Reached Kickstarter Goal</th>
<th># Team Members</th>
<th>Founder from MIT</th>
</tr>
</thead>
<tbody>
<tr>
<td>Glassr</td>
<td>No</td>
<td>3</td>
<td>Yes</td>
</tr>
</tbody>
</table>

According to the classifier you obtained from two rounds of boosting, should you invest in this startup? (That is, is it classified as Successful by your ensemble classifier?) (Circle one)

**YES**  **NO**
Part B: Perfect Classifier (12 points)
Suppose you have six training points ($P_1, P_2, P_3, P_4, P_5, P_6$) and four weak classifiers ($h_1, h_2, h_3, h_4$), which make the following errors:

<table>
<thead>
<tr>
<th>Classifier</th>
<th>Misclassified training points</th>
</tr>
</thead>
<tbody>
<tr>
<td>$h_1$</td>
<td>$P_1, P_3, P_4, P_6$</td>
</tr>
<tr>
<td>$h_2$</td>
<td>$P_2, P_5$</td>
</tr>
<tr>
<td>$h_3$</td>
<td>$P_3$</td>
</tr>
<tr>
<td>$h_4$</td>
<td>$P_4, P_6$</td>
</tr>
</tbody>
</table>

**B1 (5 points)** Ben claims that by combining **three** of the weak classifiers above, he can construct an ensemble classifier $H(x)$ that will correctly classify all the training data. If Ben is correct, list the three weak classifiers and assign them **integer voting powers** ($\alpha$) to make a perfect ensemble classifier. If Ben is wrong, circle “CAN'T BE DONE” instead.

<table>
<thead>
<tr>
<th>Weak classifier</th>
<th>Voting power</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\alpha$</td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
</tr>
</tbody>
</table>

**B2 (4 points)** Alyssa claims that by combining **two** of the weak classifiers above, she can construct an ensemble classifier $H(x)$ that will correctly classify all the training data. If Alyssa is correct, list the two weak classifiers and assign them **integer voting powers** ($\alpha$) to make a perfect ensemble classifier. If Alyssa is wrong, circle “CAN'T BE DONE” instead.

<table>
<thead>
<tr>
<th>Weak classifier</th>
<th>Voting power</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\alpha$</td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
</tr>
</tbody>
</table>

**B3 (3 points)** What is the minimum number of rounds of boosting to produce a perfect ensemble classifier? If boosting will loop forever or terminate without producing a perfect classifier, circle “CAN'T BE DONE” instead.

Number of rounds: 30

CAN'T BE DONE
Quiz 4, Problem 2: Bayesian inference (50 points)

Part A: Senioritis relapse (30 points)

Senioritis is a rare and treatable condition in general—however, here at MIT, it is positively epidemic, affecting 50% of the population. Experts have developed a cheap test for senioritis—the HACK scan—which is 80% sensitive and 60% specific. (This means that 80 out of 100 people with senioritis correctly test positive, and 60 out of every 100 people without senioritis correctly test negative. The HACK scan always reports either “positive” or “negative”.)

Assume you are a typical member of the MIT population. For notation, we can let \( D \) be the variable “You have senioritis” and let \( T \) be the variable “You test positive for senioritis”. Then the information above is:

\[
\begin{align*}
P(D) &= \frac{1}{2} \\
P(T | D) &= \frac{80}{100} \\
P(\bar{T} | \bar{D}) &= \frac{60}{100}
\end{align*}
\]

Part A1 (10 points) What is the probability of obtaining a negative test result, regardless of whether you have senioritis?

The marginal probability of a negative test result is approximately (circle one):

0% 5% 10% 15% 20% 25% 30% 35% 40% 45% 50%

For credit, you must show your work. Write down the equations you intend to solve, if any, and indicate what values you’re plugging in. You probably won’t need a calculator, because you only need an approximate final answer.
Part A2 (10 points) Suppose your HACK scan returns a negative result. In this case, the probability that you indeed don't have senioritis is most nearly (circle one):

- 50%
- 55%
- 60%
- 65%
- 70%
- 75%
- 80%
- 85%
- 90%
- 95%
- 100%

For credit, you must show your work. Write down the equations you intend to solve, if any, and indicate what values you're plugging in. You probably won't need a calculator, because you only need an approximate final answer.

Part A3 (10 points) Out of a random sample of 100 MIT students, about how many of them are expected to be false negatives—that is, how many of them will both have senioritis and also test negative?

- 0
- 10
- 20
- 30
- 40
- 50
- 60
- 70
- 80
- 90
- 100

For credit, you must show your work. Write down the equations you intend to solve, if any, and indicate what values you're plugging in. You probably won't need a calculator, since you only need an approximate final answer.
Part B: This again, but different  (16 points)
In the figure below, there are two Bayes nets and some independence statements. For each of the statements below and each Bayes net, circle TRUE if the statement is true for the net, and FALSE if the statement is false for the net.

Note: Assume that the only independence statements that are true are the ones enforced by the shape of the network.

<table>
<thead>
<tr>
<th></th>
<th>Net 1</th>
<th>Net 2</th>
</tr>
</thead>
<tbody>
<tr>
<td>A is independent of C.</td>
<td>TRUE</td>
<td>TRUE</td>
</tr>
<tr>
<td>Given C, A is independent of D.</td>
<td>TRUE</td>
<td>TRUE</td>
</tr>
<tr>
<td>$P(B</td>
<td>DAC) = P(B</td>
<td>AC)$</td>
</tr>
</tbody>
</table>

Assuming all of the variables are boolean, how many parameters does each Bayes net have?
(The number of parameters is the total number of entries in all probability tables.)

<table>
<thead>
<tr>
<th># of parameters</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
</tr>
</tbody>
</table>

Part C: What are the parameters in a binary net? (4 points)
Suppose you have training data, each with one feature X, and a classification Y. Both X and Y are boolean variables, meaning they can be either true or false. Consider the Naive Bayes classifier for this problem—which of the following probabilities are the parameters of the Naive Bayes model? (Circle ALL answers that apply, or circle “NONE OF THESE” instead.)

Hint: It may help to draw the Bayes net that corresponds to the Naive Bayes classifier for this problem.

$$P(X) \quad P(X|Y) \quad P(Y|X) \quad P(X|Y) \quad P(Y|X) \quad P(X,Y) \quad P(X,Y) \quad P(Y) \quad P(Y|X) \quad P(Y|X) \quad P(Y|X) \quad P(X,Y) \quad P(X,Y)$$

NONE OF THESE
Spiritual and Right-Now bonus points

Circle the one best answer for each of the following questions. There is no penalty for wrong answers, so it pays to guess in the absence of knowledge.

1. A key goal of the programmers apprentice project is to:
   1. Make better use of multiple-core computers.
   2. Provide convenient, natural-language access to useful code libraries.
   3. Capture the rationale behind coding choices.
   4. Provide tools for tracking the flow from specification to design to implementation to test.
   5. Use crowd sourcing to connect programmers with idle time to projects that are behind schedule.

2. Minsky seems to believe:
   1. Work on neural modeling is going better now with advances in fMRI and TMS.
   2. Work on neural modeling has succeeded during the past decade because of funding shifts.
   3. Work on neural modeling is the key to understanding why we are smarter than chimps.
   4. Work on neural modeling is needed to explain autism and other disorders.
   5. Work on neural modeling is a waste of time.

3. Cross modal coupling makes use of:
   1. Resonances that determine when two clusters have similar frequency-response parameters.
   2. Support-vector machines to separate clusters.
   3. Euclidean distances between cluster means to determine cluster distances.
   4. Dot products to determine cluster distances.
   5. Deep neural nets to merge clusters.

4. The lateral geniculate relays information from the retina to V1 (primary visual cortex). Most of its input comes from
   1. The retina
   2. Auditory cortex.
   3. The cochlea of the ear.
   4. The limbic system.
   5. V1.
SRN, Quiz 2, Constraint propagation

In this question, you get 2 points for the first correct answer and 1 point for each additional correct answer.

You have attended Winston's lecture on line-drawing analysis and dutifully recorded the table of legal junction arrangements for three-faced vertexes:

Remember: junctions may be rotated however you like, but not mirrored.

Through a window you see the following fragment. T junctions provide no constraint.
Part A

You are to perform pure constraint propagation. That is, you pile up all possible junction labels on each junction and then eliminate those junction labels that are not compatible with at least one junction label at each neighbor.

Of the 3 arrow labels in the junction library, how many are left at A after constraint propagation?

Of the 6 L labels in the junction library, how many are left at B after constraint propagation?

Of the 5 fork labels, how many are left at C in the drawing after constraint propagation?

Part B

After performing pure constraint propagation, you decide to perform a search for consistent ways to label the drawing with just one label on each junction. How many such ways are there?

36
SRN, Quiz 3, Miscellaneous

Circle the one best answer for each of the following questions. There is no penalty for wrong answers, so it pays to guess in the absence of knowledge.

1. The General Problem Solver:
   1. Uses constraint propagation to find solutions.
   2. Chooses operators to reduce differences.
   3. Uses naïve Bayesian calculations as a uniform approach to solving problems.
   4. Can be viewed as a generalization of procedural abstraction in programming.
   5. Is the key technology in the Jeopardy playing program.

2. The SOAR architecture:
   1. Is an AI based programming environment for aerospace engineers.
   2. Is an AI based programming environment for grade school pupils.
   4. Attempts to model insect level problem solving.
   5. Attempts to model the primate vision system.

3. The Subsumption architecture:
   1. Uses constraint propagation to find solutions.
   2. Chooses operators to reduce differences.
   3. Uses naïve Bayesian calculations as a uniform approach to solving problems.
   4. Can be viewed as a generalization of procedural abstraction in programming.
   5. Is the key technology in the Jeopardy playing program.

4. Minsky's Society of Mind discusses:
   1. Multiple levels of reasoning, including reflection on what is done at lower reasoning levels.
   2. A universal representation for capturing common sense knowledge.
   3. A plan for research aimed at passing the Turing test.
   4. Why Artificial Intelligence is the daemon that will lead to the self destruction of the species.
   5. Why the Jeopardy playing program isn't really intelligent.

5. Learning phonological rules using the Sussman-Yip method:
   1. Uses a big data approach to explain how children learn vowel sounds.
   2. Uses the McGurk effect to determine which words to use in learning.
   3. Uses the mistakes made by non native speakers to group phonemes into hierarchies.
   4. Uses dot product calculations to determine distances between phonemes.
   5. Uses beam search to learn recognition patterns based on distinctive features.

6. Arch learning demonstrates:
   1. Nothing definite can be learned from individual examples no matter how a sequence is crafted.
   2. Something definite can be learned from each example in a carefully crafted example sequence.
   3. How a program can form clusters using a cosine based distance metric.
   4. How a program can both generalize and specialize from a single example.
   5. How a program can learn without supervision.
SRN, Quiz 4, Miscellaneous

Circle the one best answer for each of the following questions. There is no penalty for wrong answers, so it pays to guess in the absence of knowledge.

1. The Genesis story understanding system offers an explanation for
   1. Why stories evolve over time.
   2. Why someone from another culture may see the world in a different light.
   4. Why lack of sleep makes us stupid.
   5. Why used-car salespeople talk fast.

2. The central goal of the Genesis story understanding system is to:
   1. Improve internet searches.
   4. Take fantasy computer games to another level.
   5. Facilitate human-computer cooperation.

3. Probabilistic programming:
   1. Provides tools for filling in missing data in tables.
   2. Uses random number generators to simulate neural behavior.
   3. Constrains programs such that the probability of a bug is less than $\varepsilon$.
   4. Provides programmers with drawing tools for constructing Bayes nets.
   5. Compiles Bayesian nets into joint probability tables for computation.

4. The START natural language system translates English into:
   1. French.
   2. Parse trees.
   5. Images for which the English provides a reasonable caption.

5. While sleeping, hippocampus activity suggests that rats are thinking about:
   1. Food.
   2. Mazes.
   4. Predators.
   5. Nothing.

6. When a plain, old-fashioned neural net, 5 layers deep, is given a multiclass identification problem
   1. The weights in all layers will change at about the same rate.
   2. The layers closest to the output will go quickly and strongly positive.
   3. The layers closest to the output will go quickly and strongly negative.
   4. The layers closest to the input will go quickly and strongly positive.
   5. The layers closest to the input will go quickly and strongly negative.
Tear off sheets—you need not hand these in

Q2, Problem 1

Q2, Problem 2