

MASSACHUSETTS INSTITUTE OF TECHNOLOGY  
Department of Electrical Engineering and Computer Science  
6.01—Introduction to EECS I  
Spring Semester, 2008

**NanoQuiz Week #5 (sections 1 and 2)**

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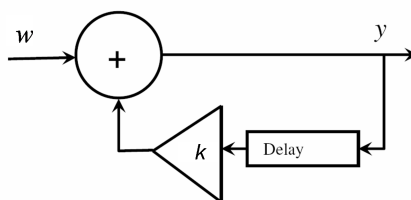
**This quiz is due promptly 15 minutes after the start of the lab period.**

You may use the weekly assignment handout, but the quiz is otherwise closed book and closed computer.

Let  $H_1$  be the LTI system with input  $x$  and output  $w$  described by

$$w[n] = 0.5w[n-1] + x[n]$$

and let  $H_2$  be the LTI system with input  $w$  and output  $y$  described by the following block diagram, where  $k$  is some constant (positive or negative):



Let  $H_3$  be the system formed by cascading  $H_2$  after  $H_1$ , with input  $x$  and output  $y$ .

1. What is the system function for  $H_1$  and what are its poles?
2. What is the system function for  $H_2$  and what are its poles?
3. What is the system function for  $H_3$  and what are its poles?

**Additional questions on the reverse side...**

4. For which values of  $k$  is the cascaded system  $H_3$  unstable (i.e., the output grows arbitrarily large)?
5. Give a single difference equation that describes  $H_3$  and directly relates  $y$  to  $x$ .