

Modelling Nuclear Reactors with Julia

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My objective

To see how well Julia fits my use cases

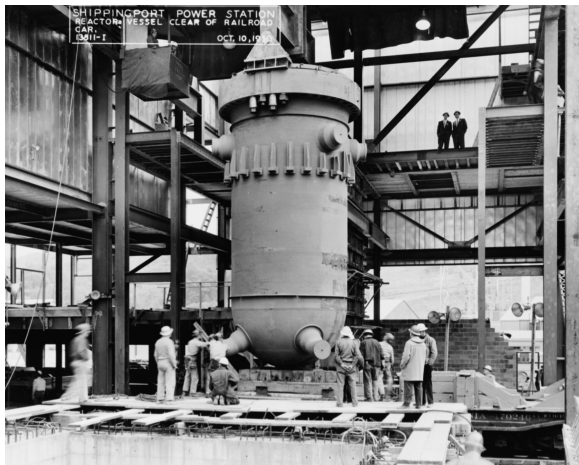
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Benchmark problem: a nuclear reactor simulator (specifically method of characteristics)

What a nuclear reactor looks like

The heart of a typical nuclear powerplant is a pressure vessel where water is heated



Credit: US DOE

What a nuclear reactor looks like

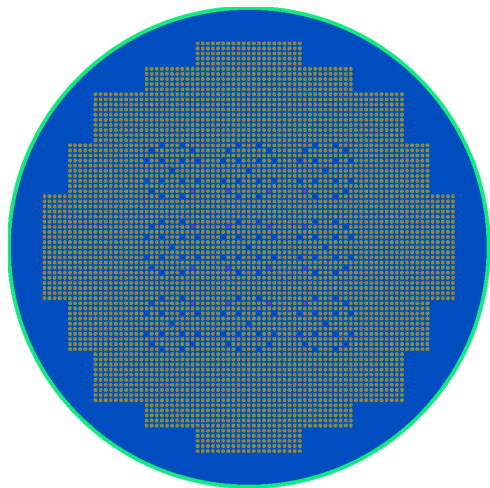
Inside that vessel are about 200 fuel assemblies—bundles of rods containing uranium



Credit: US DOE

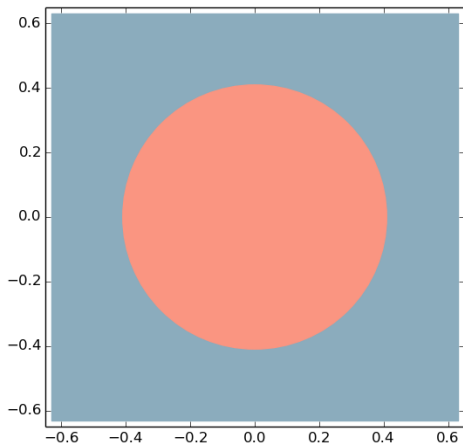
What a nuclear reactor looks like

Reactors have a lot of axial symmetry which usually allows us to model them in 2D



What my geometry looks like

For this project, I further simplified down the model to a single “pin cell” with reflective boundaries



The problem

Goal: neutron interaction rate

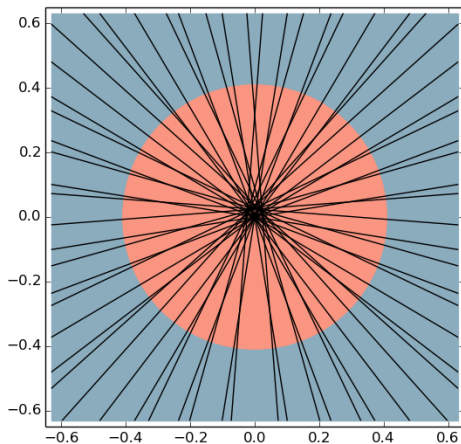
Complication: strong anisotropy

Diffusion can't solve this problem!

Solution: integrate over characteristic paths

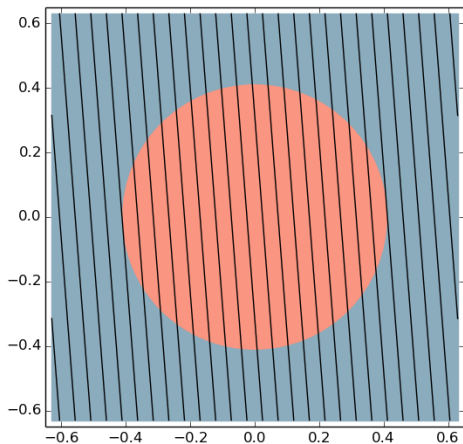
Neutron characteristics

Select a set of azimuthal angles (32 in this case)



Neutron characteristics

Repeat each azimuthal ray with a regular spacing (0.5 mm in this case)



The algorithm

Algorithm 2 Transport Sweep Algorithm

```
 $\Phi_{i,g} \leftarrow 0 \quad \forall i, g \in \{I, G\}$  # Initialize FSR scalar fluxes to zero
while  $\Phi_{i,g} \forall i$  not converged do
  for all  $m \in M$  do # Loop over azimuthal angles
    for all  $k \in K(m)$  do # Loop over tracks
      for all  $s \in S(k)$  do # Loop over segments
        for all  $g \in G$  do # Loop over energy groups
          for all  $p \in P$  do # Loop over polar angles
             $i \leftarrow I(s)$  # Get FSR for this segment
             $\Delta\Psi_{k,i,g,p} \leftarrow \left( \Psi_{k,g,p} - \frac{Q_{i,g}}{\Sigma_{i,g}} \right) (1 - e^{-\tau_{k,i,g,p}})$  # Compute angular flux change along segment
             $\Phi_{i,g} \leftarrow \Phi_{i,g} + \frac{4\pi}{A_i} \omega_m \omega_p \omega_k \sin \theta_p \Delta\Psi_{k,i,g,p}$  # Increment FSR scalar flux
             $\Psi_{k,g,p} \leftarrow \Psi_{k,g,p} - \Delta\Psi_{k,g,p}$  # Update track outgoing flux
          end for
        end for
      end for
    end for
  end for
```

Credit: Will Boyd

The codes: a three-way face-off

C++

Well developed parallel research code with many features

Python

My own homework code, slow

Julia

Similar to the Python code, but fast

	C++	Python	Julia
Baseline	2.8 s (1×)	117.0 s (41×)	14.4 s (5×)
Serial opt	-	-	-
2 Procs	-	-	-

Direct translation Python \rightarrow Julia gives 8× speed up. Awesome!

	C++	Python	Julia
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A little serial optimization gets us close the C++ reference

	C++	Python	Julia
Baseline	2.8 s (1×)	117.0 s (41×)	14.4 s (5×)
Serial opt	-	-	9.4 s (3×)
2 Procs	-	-	46.1 s (16×)

Direct translation Python \rightarrow Julia gives 8× speed up. Awesome!

A little serial optimization gets us close the C++ reference

Sadly my parallel efforts didn't turn out